

Hadrons in hot and dense matter I

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Outline

- 1 Plan of the lectures and motivation
- 2 The phase diagram of strongly interacting matter
- 3 QCD and chiral symmetry
 - Particles and forces in the Standard Model
 - Quantum Electrodynamics (QED)
 - Quantum Chromodynamics (QCD) and chiral symmetry
 - Chiral effective models for hadrons
- 4 Strongly interacting matter: QCD/hadronic models at finite T, μ
- 5 References
- 6 Quiz

Plan of the lectures

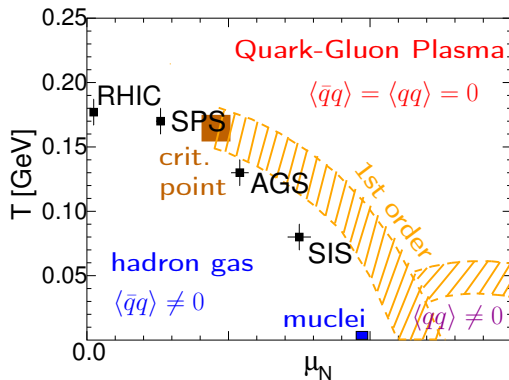
- **Lecture I: Fundamentals**
 - symmetries and conservation laws in (quantum) field theory
 - the Standard Model in a nutshell
 - QCD, chiral symmetry, and effective models for hadrons
- **Lecture II: electrodynamic probes in heavy-ion collisions (fundamentals)**
 - transport and hydrodynamics
 - collective flow
 - radiation of electromagnetic probes from a thermal transparent medium (McLerran-Toimela formula)
 - effective hadronic models for vector mesons

- **Lecture III: Dileptons in heavy-ion collisions (SIS@GSI)**
 - hadronic models for transport models: baryon resonances
 - Gießen Boltzmann-Uehling-Uhlenbeck (GiBUU)
 - Ultrarelativistic Quantum Molecular Dynamics (UrQMD)
 - medium modifications:
“transport-hydro hybrid” and “coarse-graining” approach
- **Lecture IV: Electromagnetic probes in heavy-ion collisions (SPS@CERN, RHIC@BNL, LHC@CERN)**
 - hard-thermal-loop approved dilepton rates (emission from QGP)
 - hadronic many-body theories (emission from hadron gas)
 - dileptons at SPS and RHIC
 - access to the phase diagram?

Phase diagram, HICs, dileptons

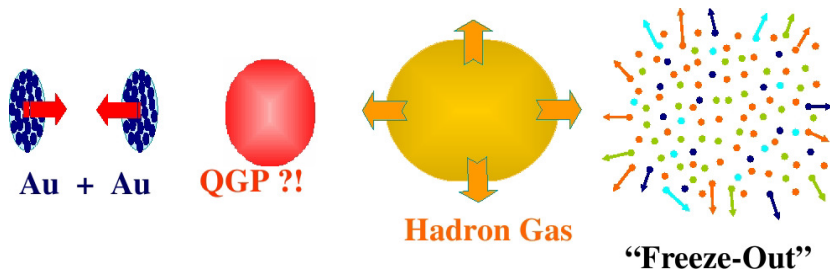
The phase diagram of strongly interacting matter

- hot and dense matter: **quarks and gluons** inside hadrons compressed
- highly energetic scatterings \Rightarrow **deconfinement/chiral phase transition**
- **quarks** and **gluons** relevant d.o.f. \Rightarrow **Quark-Gluon Plasma**
- still strongly couples: **fast thermalization!**
- in the vacuum quark condensate $\langle \bar{q}q \rangle \neq 0$
- at high T, μ_B : **chiral phase transition** $\langle \bar{q}q \rangle = 0$



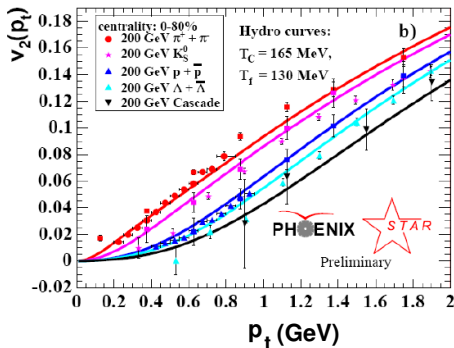
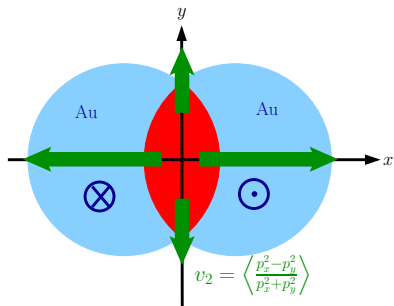
Ultra-relativistic heavy-ion collisions

- highly energetic collisions of (heavy) nuclei
- many collisions of **partons** inside the nucleons
- creation of many particles \Rightarrow **hot and dense fireball**
- generation of the **Quark-Gluon Plasma** (QGP)?
- properties of QGP and/or **compressed baryonic matter**?
- signatures of **1st-order phase transition** (critical end point)?



Hydrodynamical behavior

- particle spectra compatible with collective motion of an **ideal fluid** \Rightarrow **small viscosity**
- Medium in **local thermal equilibrium** (after short formation time $\lesssim 1$ fm/c)



Why Electromagnetic Probes?

- γ, l^\pm : only e. m. interactions
- reflect whole “history” of collision
- chance to see chiral symm. rest. directly?

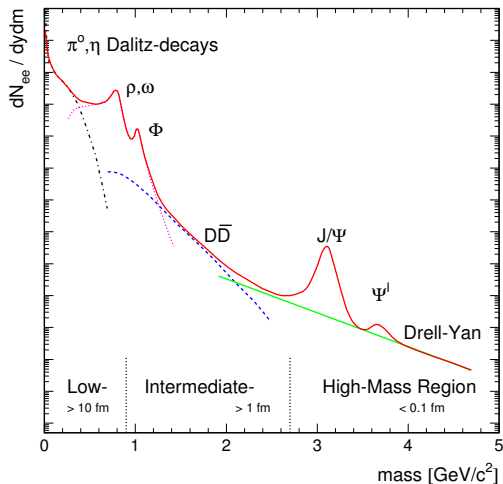
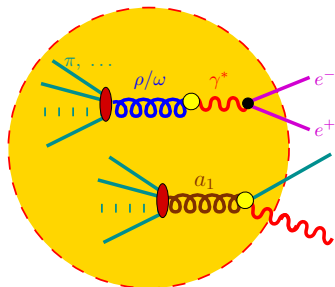
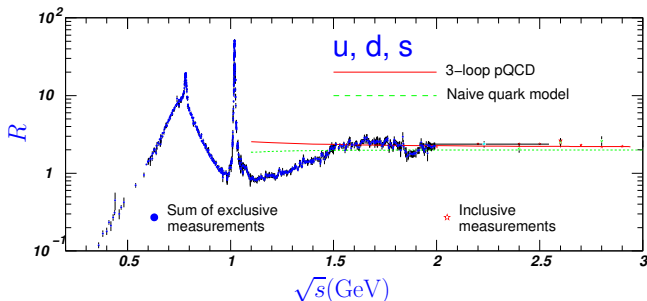


Fig. by A. Drees (from [RW00])

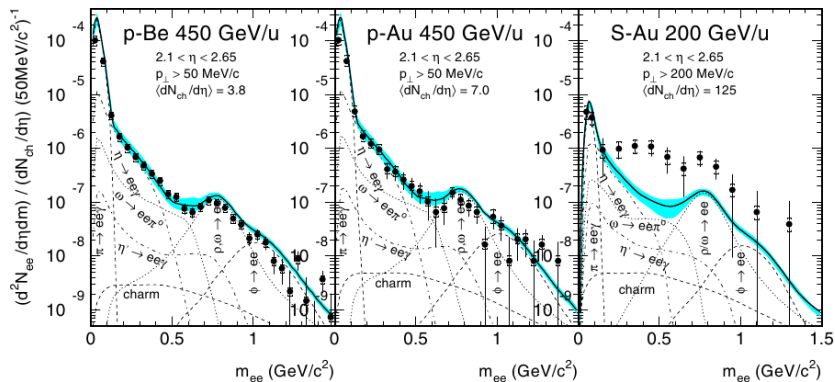
Vacuum Baseline: $e^+e^- \rightarrow \text{hadrons}$



$$R := \frac{\sigma_{e^+e^- \rightarrow \text{hadrons}}}{\sigma_{e^+e^- \rightarrow \mu^+\mu^-}}$$

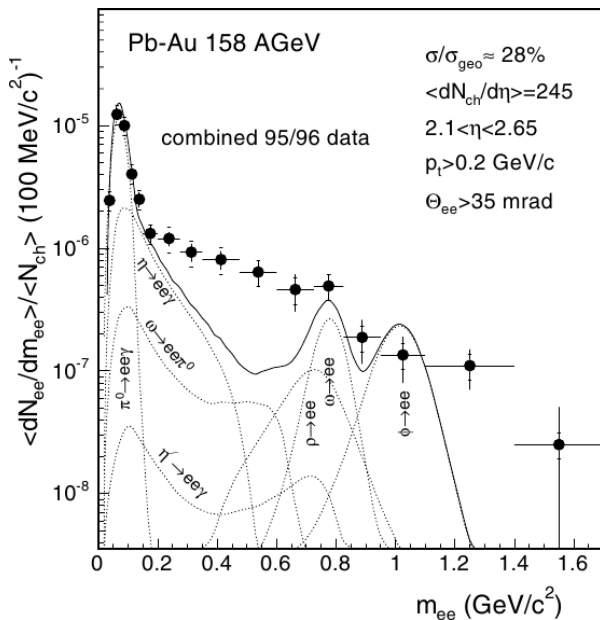
- probes all hadrons with quantum numbers of γ^*
- $R_{\text{QM}} = N_c \sum_{f=u,d,s} Q_f^2 = 3 \times [(2/3)^2 + (-1/3)^2 + (-1/3)^2] = 2$
- Our aim $pp \rightarrow \ell^+\ell^-$, $pA \rightarrow \ell^+\ell^-$, $AA \rightarrow \ell^+\ell^-$ ($\ell = e, \mu$)

The CERES findings: Dilepton enhancement



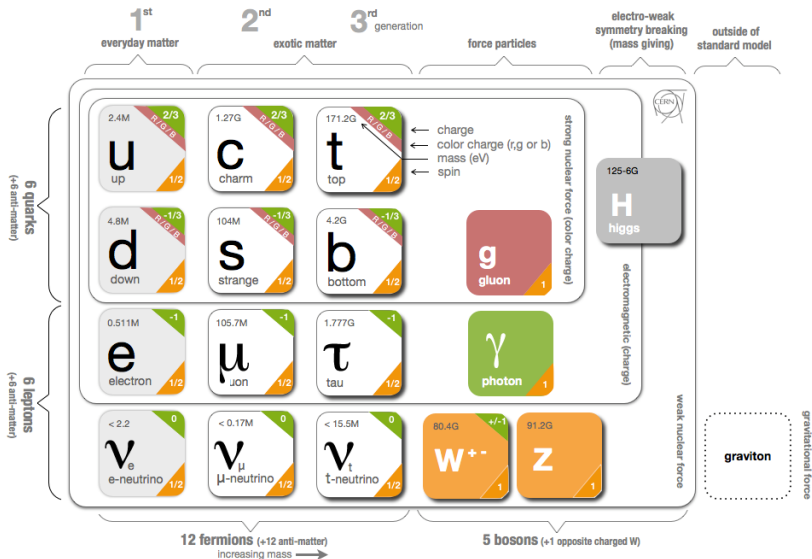
- pp (pBe): “elementary reactions”; baseline (mandatory to understand first!)
- pA: “cold nuclear matter effects”; next step (important as baseline for other observables like “ J/ψ suppression”)
- AA: “medium effects”; hope to learn something about **in-medium properties of vector mesons, fundamental QCD properties**

The CERES findings: Dilepton enhancement



QCD and chiral symmetry

The standard model in a nutshell: particles and forces



[graphics from <http://www.isgtw.org/spotlight/go-particle-quest-first-cern-hackfest>]

Quantum Electrodynamics (QED)

Literature: [Nac90, DGH92, B⁺12], conventions as in [Nac90]

- **electrons+positrons**: massive spin-1/2 Dirac field $\psi \in \mathbb{C}^4$
- describes electron (charge $q_e = -1$) and antielectron (=positron)
- **photon**: massless vector field A_μ
- antisymmetric field-strength tensor $\rightarrow (\vec{E}, \vec{B})$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu = \begin{pmatrix} 0 & E^1 & E^2 & E^3 \\ -E_1 & 0 & -B_3 & B_2 \\ -E_2 & B_3 & 0 & -B_1 \\ -E_3 & -B_2 & B_1 & 0 \end{pmatrix}$$

- Lagrangian ($e > 0$): em. coupling constant $e^2/(4\pi) = \alpha_{\text{em}} \simeq 1/137$

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} [i(\not{\partial} + iq_e e \not{A}) - m] \psi, \quad q_e = -1$$

- Dirac matrices: $\gamma^\mu \in \mathbb{C}^{4 \times 4}$, $\mu \in \{0, 1, 2, 3\}$,
 $\{\gamma^\mu, \gamma^\nu\} = 2\eta^{\mu\nu} = \text{diag}(1, -1, -1, -1)$, $\bar{\psi} = \psi^\dagger \gamma^0$
- “Feynman slash” $\not{A} = A_\mu \gamma^\mu$, $\not{\partial} = \gamma^\mu \partial_\mu = \gamma^\mu \frac{\partial}{\partial x^\mu}$

Symmetries of QED

- as a classical field theory: **Least-action principle** \Rightarrow equations of motion
- action (**Lorentz invariant!**)

$$S[A, \psi] = \int d^4x \mathcal{L}$$

- symmetries lead to conservation laws (**Noether's Theorem**)
- space-time symmetries
 - time translations: **energy conservation**
 - space translations: **momentum conservation**
 - rotations: **angular-momentum conservation**
- intrinsic symmetry: invariant under change of phase factor $\psi \rightarrow \exp(-iq_e e a)\psi$, $a \in \mathbb{R} \Rightarrow$ electric-charge conservation

$$j_{\text{em}}^{(e)\mu} = q_e e \bar{\psi} \gamma^\mu \psi, \quad \partial_\mu j_{\text{em}}^{(e)\mu} = 0$$

- here even **local gauge symmetry**:

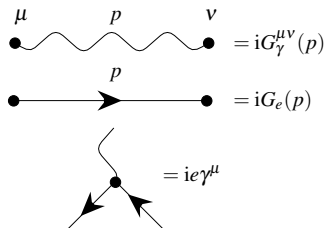
$$\psi \rightarrow \exp[-iq_e e \chi(x)]\psi, \quad A_\mu \rightarrow A_\mu + q_e \partial_\mu \chi$$

- local symmetry \Leftrightarrow **gauge boson**

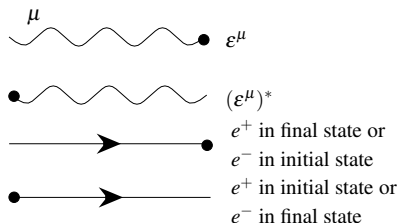
Quantization

- fields \Rightarrow operators
- physical quantities S-matrix elements: $|T_{fi}|^2$ transition probabilities for scattering from asymptotic free initial to asymptotic free final state
- local, microcausal quantum field theory with stable ground state
 - **spin-statistics relation:**
half-integer spin \Leftrightarrow fermions, integer spin \Leftrightarrow bosons
- can only evaluate in perturbation theory \Rightarrow Feynman rules

Internal lines: Propagators



External lines: Initial and final states



- $G_{\gamma}^{\mu\nu} = -\eta_{\mu\nu}/(p^2 + i0^+)$, $G_e = (\not{p} - m)/(p^2 - m^2 + i0^+)$

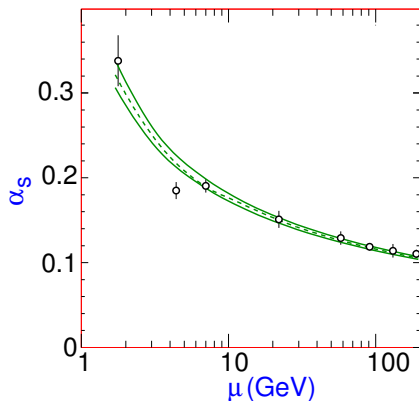
- Theory for strong interactions: QCD

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} F_a^{\mu\nu} F_{\mu\nu}^a + \bar{\psi}(i\not{D} - \hat{M})\psi$$

- non-Abelian gauge group $\text{SU}(3)_{\text{color}}$
 - each quark: color triplet
 - covariant derivative: $D_\mu = \partial_\mu + ig \hat{T}^a A_\mu^a$ ($a \in \{1, \dots, 8\}$)
 - field-strength tensor $F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g f^{abc} A_\mu^b A_\nu^c$
 - group structure constants: $[\hat{T}^a, \hat{T}^b] = if^{abc} \hat{T}^c$, $\hat{T}^a = (\hat{T}^a)^\dagger \in \mathbb{C}^{3 \times 3}$
- Particle content:
 - ψ : Quarks with flavor ($u, d; c, s; t, b$) (mass eigenstates!)
 - $\hat{M} = \text{diag}(m_u, m_d, m_s, \dots) =$ current quark masses
 - A_μ^a : gluons, gauge bosons of $\text{SU}(3)_{\text{color}}$
- Symmetries
 - fundamental building block: local $\text{SU}(3)_{\text{color}}$ symmetry
 - in light-quark sector: approximate chiral symmetry ($\hat{M} \rightarrow 0$)
 - dilation symmetry (scale invariance for $\hat{M} \rightarrow 0$)

Features of QCD

- asymptotically free: at **large** momentum transfers $\alpha_s = 4\pi g_s^2 \rightarrow 0$
- running from renormalization group (due to self-interactions of gluons!):
Nobel prize 2004 for Gross, Wilczek, Politzer



- quarks and gluons **confined in hadrons**
- theoretically not fully understood (nonperturbative phenomenon!)
- need of **effective hadronic models** at low energies: (Chiral) symmetry!

Chiral Symmetry of (massless) QCD

- Consider only **light** u, d quarks
- **iso-spin 1/2 doublet**: $\psi = \begin{pmatrix} u \\ d \end{pmatrix} = \begin{pmatrix} \psi_1 \\ \psi_2 \end{pmatrix}$
- NB: ψ has three “indices”: Dirac spinor, color, flavor iso-spin!
- γ matrices: $\{\gamma_\mu, \gamma_\nu\} = 2\eta_{\mu\nu}\mathbb{1}$, $\gamma_5 := i\gamma_0\gamma_1\gamma_2\gamma_3$, $\gamma_5\gamma_\mu = -\gamma_\mu\gamma_5$, $\gamma_5^\dagger = \gamma_5$, $\gamma_5^2 = \mathbb{1}$
- Diracology of **left and right-handed components**

$$\psi_L = \frac{\mathbb{1} - \gamma_5}{2}\psi = P_L\psi, \quad \psi_R = \frac{\mathbb{1} + \gamma_5}{2}\psi = P_R\psi,$$

$$P_{L/R}^2 = P_{L/R}, \quad P_R P_L = P_L P_R = 0, \quad P_{L/R}\gamma_5 = \gamma_5 P_{L/R} = \mp P_{L/R}$$

$$P_{L/R}\gamma_\mu = \gamma_\mu P_{R/L}, \quad \overline{P_L\psi} = \overline{\psi}P_R, \quad \overline{P_R\psi} = \overline{\psi}P_L$$

$$\overline{\psi}\gamma_\mu\psi = \overline{\psi}_L\gamma_\mu\psi_L + \overline{\psi}_R\gamma_\mu\psi_R, \quad \overline{\psi}\psi = \overline{\psi}_L\psi_R + \overline{\psi}_R\psi_L$$

- $\overline{\psi} := \psi^\dagger\gamma_0$, $\overline{\gamma_5\psi} = \psi^\dagger\gamma_5^\dagger\gamma_0 = -\overline{\psi}\gamma_5$
- in the massless limit ($m_u = m_d = 0$)

$$\mathcal{L}_{u,d} = \overline{\psi}i\not{D}\psi = \overline{\psi}_L i\not{D}\psi_L + \overline{\psi}_R i\not{D}\psi_R$$

Chiral Symmetry of (massless) QCD

- in the massless limit ($m_u = m_d = 0$)
- a lot of global **chiral symmetries**:
 - change of **independent** phases for **left** and **right** components:

$$\psi_L(x) \rightarrow \exp(-i\phi_L)\psi_L(x), \quad \psi_R(x) \rightarrow \exp(-i\phi_R)\psi_R(x)$$

- symmetry group $U(1)_L \times U(1)_R$
- independent “iso-spin rotations”

$$\psi_L(x) \rightarrow \exp(-i\vec{\alpha}_L \cdot \vec{T})\psi_L(x), \quad \psi_R(x) \rightarrow \exp(-i\vec{\alpha}_R \cdot \vec{T})\psi_R(x)$$

- $\vec{T} = \vec{\tau}/2$, $\vec{\tau}$: **Pauli matrices**; symmetry group $SU(2)_L \times SU(2)_R$
- alternative notation scalar-pseudoscalar phases/iso-spin rotations

$$\psi \rightarrow \exp(-i\phi_s)\psi, \quad \psi \rightarrow \exp(-i\gamma_5\phi_a)\psi$$

$$\psi \rightarrow \exp(-i\vec{\alpha}_V \cdot \vec{T})\psi, \quad \psi \rightarrow \exp(-i\gamma_5\vec{\alpha}_A \cdot \vec{T})\psi$$

- $U(1)_s$ and $SU(2)_V$ **are subgroups** that are **symmetries** even if $m_u = m_d \neq 0 \Rightarrow$ Heisenberg’s iso-spin symmetry!

Currents: relation to mesons

- based on [Koc97, Sch03, Din11]
- Noether: each global symmetry leads to a **conserved quantity**
- from **chiral symmetries**

$$j_s^\mu = \bar{\psi}\gamma^\mu\psi, \quad j_a^\mu = \bar{\psi}\gamma^\mu\gamma_5\psi$$
$$\vec{j}_V^\mu = \bar{\psi}\gamma^\mu\vec{T}\psi, \quad \vec{j}_A^\mu = \bar{\psi}\gamma^\mu\gamma_5\vec{T}\psi$$

- Link to mesons: Build Lorentz-invariant objects with corresponding quantum numbers
 - σ : $\bar{\psi}\psi$ (scalar and iso-scalar)
 - π 's: $i\bar{\psi}\vec{T}\gamma_5\psi$ (pseudoscalar and iso-vector)
 - ρ 's: $\bar{\psi}\gamma_\mu\vec{T}\psi$ (vector and iso-vector)
 - a_1 's: $\bar{\psi}\gamma_\mu\gamma_5\vec{T}\psi$ (axialvector and iso-axialvector)
- in nature: σ and π 's; ρ 's and a_1 's **do not have same mass!**
- reason: QCD ground state **not symmetric** under pseudoscalar and pseudovector trafos since $\langle \text{vac} | \bar{\psi}\psi | \text{vac} \rangle \neq 0$

Spontaneous symmetry breaking

- **spontaneously broken symmetry**: ground state not symmetric
- vacuum necessarily **degenerate**
- vacuum invariant under scalar and vector transformations: $U(1)_L \times U(1)_R$ broken to $U(1)_S$; $SU(2)_L \times SU(2)_R$ broken to $SU(2)_V$
- for each broken symmetry **massless scalar Goldstone boson**
- there are three pions which are very light compared to other hadrons (finite masses due to **explicit** breaking through m_u, m_d !)
- **but no pseudoscalar isoscalar light particle!** ($m_\eta \simeq 548$ MeV)
- **reason: $U(1)_a$ anomaly**
 - axialscalar symmetry does not survive quantization!
 - good for explanation of correct decay rate for $\pi_0 \rightarrow \gamma\gamma$
 - axialscalar current not conserved $\partial_\mu j_a^\mu = 3/8\alpha_s \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a$
- explicit breaking due to quark masses
 - can be treated perturbatively \Rightarrow **chiral perturbation theory**
 - axial-vector current only approximately conserved \Rightarrow **PCAC**
 - a lot of low-energy properties of hadrons derivable

Chiral transformations

- σ meson and pions (chiral partners)
- meson = $\bar{q}-q$ bound state
- infinitesimal chiral transformations for quarks ($\vec{T} = \vec{\tau}/2$) in $SU(2)_L \times SU(2)_R$ model

$$\psi \rightarrow (1 - i\delta\vec{\alpha}_V \cdot \vec{\tau}/2)\psi \quad (\text{iso-vector transformation})$$

$$\psi \rightarrow (1 - i\gamma_5\delta\vec{\alpha}_A \cdot \vec{\tau}/2)\psi \quad (\text{axial-vector transformation})$$

- transformation properties under χ transformations as $\sigma \sim \bar{\psi}\psi$, $\vec{\pi} \sim i\bar{\psi}\vec{\tau}\gamma_5\psi$

$$\sigma \rightarrow \sigma - \delta\vec{\alpha}_A \cdot \vec{\pi}, \quad \vec{\pi} \rightarrow \vec{\pi} + \delta\vec{\alpha}_V \times \vec{\pi} + \delta\vec{\alpha}_A\sigma$$

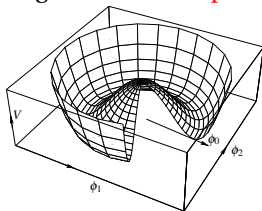
- $\sigma^2 + \vec{\pi}^2$ invariant $\Rightarrow \chi$ symmetry realized as $SO(4)$ rotations

The minimal linear σ model

- chiral symmetry realized by $SO(4)$: meson fields $\phi \in \mathbb{R}^4$
- describes σ and pions (π^\pm, π^0)

$$\mathcal{L}_{\chi\text{limit}} = \frac{1}{2}(\partial_\mu \phi)(\partial^\mu \phi) - V(\phi) = \frac{1}{2}(\partial_\mu \phi)(\partial^\mu \phi) - \frac{\lambda}{4}(\phi^2 - f_\pi^2)^2$$

- spontaneous symmetry breaking: **mexican-hat potential**



- doesn't cost energy to excite field in direction of the rim
⇒ **massless Nambu-Goldstone bosons (pions)**
- vacuum expectation value $\langle \phi^0 \rangle = f_\pi \neq 0$
- symmetry **spontaneously broken** from $SO(4)$ to $SO(3)_V$
- particle spectrum: **4 field-degrees** of freedom ⇒ vacuum inv. **3-dim** $SO(3)$
⇒ **3 massless pions** ⇒ **4 - 3 = 1 massive σ**

Pion decay and PCAC

- weak decay $\pi^+ \rightarrow \mu^+ + \nu_\mu$
- weak interaction $\propto J_V^\mu - J_A^\mu$
- pion **pseudoscalar** \Rightarrow decay must be due to axial current \Rightarrow

$$\langle 0 | J_A^{a\mu}(x) | \pi_b(p) \rangle = i p^\mu \delta_{ab} f_\pi \exp(-i p \cdot x)$$

- decay rate from Fermi model $\Rightarrow f_\pi \simeq 93 \text{ MeV}$

$$\langle 0 | \partial_\mu J_A^{a\mu}(x) | \pi_b(p) \rangle = -f_\pi p^2 \delta^{ab} \exp(-i p \cdot x) = -f_\pi m_\pi^2 \delta^{ab} \exp(-i p \cdot x)$$

- exact chiral symmetry $\Rightarrow m_\pi = 0$ (Goldstone theorem!) $\Rightarrow \partial_\mu J_A^{a\mu} = 0$ Noether
- $m_\pi \neq 0$ but “small” \Rightarrow “partial conservation of axial current” (**PCAC**)
- in effective model

$$J_{A,\pi}^{a\mu} = f_\pi \partial_\mu \phi^a, \quad a \in \{1, 2, 3\}$$

Explicit symmetry breaking

- explicit breaking due to **finite quark masses**
- symmetry-breaking term in QCD: $\mathcal{L}_{\chi\text{SB}} = -m\bar{\psi}\psi$
- $m = (m_u + m_d)/2$; from $\bar{\psi}\psi \sim \sigma \Rightarrow$

$$\mathcal{L}_{\chi\text{SB}} = -\epsilon\sigma$$

- now write for σ -pion potential

$$V(\sigma, \vec{\pi}) = \frac{\lambda}{4} [(\sigma^2 + \vec{\pi}^2) - v_0^2]^2 - \epsilon\sigma$$

- tilted in σ -direction \Rightarrow “selects” direction of vacuum expectation value
- minimum at $f_\pi \Rightarrow$

$$v_0 = f_\pi - \frac{\epsilon}{2\lambda f_\pi^2}, \quad m_\sigma^2 = 2\lambda f_\pi^2 + \frac{\epsilon}{f_\pi}, \quad m_\pi^2 = \frac{\epsilon}{f_\pi}$$

- Noether with symmetry breaking + PCAC (**consistency!**):

$$\partial_\mu J_A^{a\mu} = -\epsilon\pi^a \stackrel{\text{PCAC}}{=} -f_\pi m_\pi^2 \pi^a \Rightarrow \epsilon = f_\pi m_\pi^2$$

- χSB in QCD as in effective model \Rightarrow **Gell-Mann-Oaks-Renner Relation**

$$\langle 0 | \epsilon \sigma | 0 \rangle = f_\pi \epsilon = m_\pi^2 f_\pi^2 = -m \langle 0 | \bar{\psi} \psi | 0 \rangle$$

Adding nucleons

- axial current of nucleon

$$\vec{J}_{A,\text{nucl}}^\mu = g_a \bar{\Psi} \gamma^\mu \gamma_5 \vec{\tau} \Psi$$

- from neutron- β decay $\Rightarrow g_a = 1.25$
- total axial current $\vec{J}_A^\mu = \vec{J}_{A,\pi}^\mu + \vec{J}_{A,\text{nucl}}^\mu$ should fulfill PCAC $\partial_\mu \vec{J}_A^\mu = -f_\pi m_\pi^2 \vec{\pi} \Rightarrow$

$$(\square + m_\pi^2) \pi^a = -g_a i \frac{M}{f_\pi} \bar{\Psi} \gamma_5 \vec{\tau} \Psi$$

- Goldberger-Treiman relation**

$$g_{\pi NN} = g_a \frac{M}{f_\pi} \simeq 12.6 \quad \text{vs.} \quad g_{\pi NN}^{\text{exp}} = 13.4$$

- extension of linear σ model

$$\mathcal{L}_{\text{nucl}} = \bar{\Psi} i \not{\partial} \Psi - g_{\pi NN} [i \bar{\Psi} \gamma_5 \vec{\tau} \Psi \cdot \vec{\pi} + \bar{\Psi} \Psi \sigma] + \mu \bar{\Psi} \Psi$$

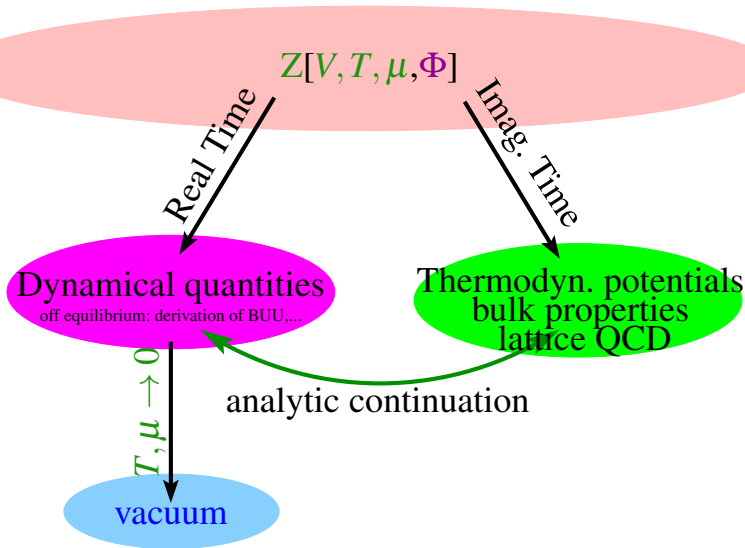
- GT relation: $\langle 0 | \sigma | 0 \rangle = f_\pi \Rightarrow M = g_A M - \mu$

$$\mu = (g_A - 1) M \simeq \frac{M}{4}$$

QFT@finite T, μ

Finite Temperature/Density: Idealized theory picture

- partition sum: $Z(V, T, \mu_q, \Phi) = \text{Tr}\{\exp[-(\mathbf{H}[\Phi] - \mu_q \mathbf{N})/T]\}$



- Asymptotic freedom
 - **quark condensate melts** at high enough **temperatures/densities**
- all bulk properties from **partition sum**:

$$Z(V, T, \mu_q) = \text{Tr}\{\exp[-(\mathbf{H} - \mu_q \mathbf{N})/T]\}$$

- Free energy: $\Omega = -\frac{T}{V} \ln Z = -P$
- **Quark condensate**: $\langle \bar{\psi}_q \psi_q \rangle_{T, \mu_q} = \frac{V}{T} \frac{\partial P}{\partial m_q}$
- Lattice QCD (at $\mu_q = 0$)
 - **chiral symmetry** $\Leftrightarrow \langle \bar{\psi} \psi \rangle$
 - **deconfinement transition** \Leftrightarrow Polyakov Loop $\text{tr} \left\langle P \exp(i \int_0^\beta d\tau A^0) \right\rangle$
 - **Chiral symmetry restoration** and **deconfinement transition** at same T_c

What can we learn from em. probes in heavy-ion collisions?

- only **penetrating probe**
 - leptons and photons leave **hot and dense fireball** unaffected
 - they are produced during the **entire fireball evolution**
 - dileptons provide information on **in-medium spectral properties of hadrons**
- theoretical challenge
 - need an understanding of **QCD medium** at all stages of its evolution
⇒ **transport models, hydrodynamics**
 - need to identify **all sources of dileptons and photons**
 - **perturbative QCD** not applicable
⇒ **non-perturbative QCD, effective hadronic models**
 - evaluate **dilepton and photon rates** ⇒ **QFT at finite T and μ_B**

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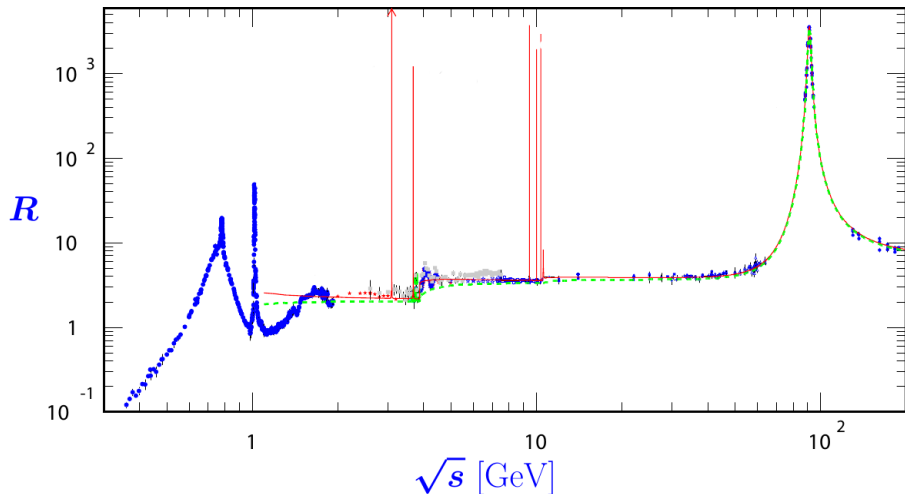
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Quiz

- 1 What are the peaks in the following figure of $R_{e^+e^- \rightarrow \text{hadrons}}$?
- 2 Can you explain the horizontal lines (values: 2, 3.333, 3.667)?



- 4 Why is chiral symmetry (intuitively) only true for massless quarks?
- 5 What's the main consequence of spontaneous symmetry breaking?
- 6 Why can one measure the vector and axial-vector current-current correlators from $\tau \rightarrow$ even/odd number of pions + ν ?