



Di-electron production at ultra-relativistic energies

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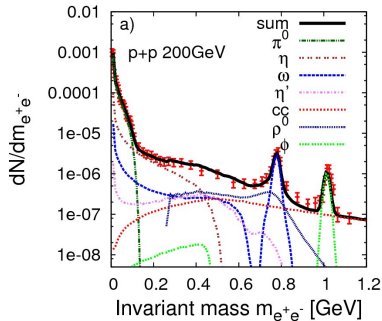
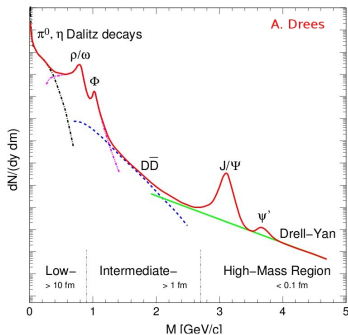
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June 29, 2012

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Introduction

Invariant mass spectrum of di-lepton pairs carry plenty of information



$p+p$ well understood in terms of CFO cocktail

Deviations from cocktail in $A+A$: dynamics, energy loss, quarkonia melting, in-medium modification, QGP

Electromagnetic signals survive the evolution and are "separable"
 \rightarrow offers windows to look into all stages of evolution (QGP!)

Different models for different stages of the evolution

Process	Model	M Region	Time (LHC)
◇ Initial state Drell-Yan [†]	pQCD ₁	IMR/HMR	< 0.03 fm
◇ Quark-gluon-plasma radiation	PHSD	IMR/HMR	few - 5 fm
◇ Quarkonia	data	HMR	few - 10 fm
◇ Quarkonia suppression	pQCD ₂	HMR	few - 5 fm
◇ Charm and beauty continuum	MC@ _s HQ	IMR/HMR	5 - 10 fm
◇ In-medium effects	PHSD	LMR	5 - 10 fm
◇ Freeze-out decay cocktail	SHM/PHSD	LMR	≈10 fm

[†] not important at LHC

pQCD₁=next to leading order collinear factorisation approach

pQCD₂=NLO $c + \bar{c} + p \rightarrow J/\psi + p$ with non-equilibrium c, \bar{c}

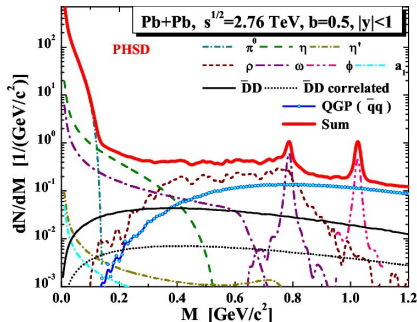
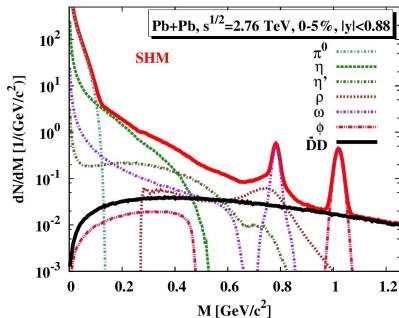
MC@_sHQ=pQCD + hydro based model for heavy-quark propagation

PHSD=off-shell parton-Hadron transport with dynamical quasi-particles

SHM=statistical hadronization model

Low invariant mass region in Pb+Pb at 2.76 TeV

Low invariant mass region is dominated by the freeze-out decay cocktail
 → SHM and PHSD in fair agreement in Pb+Pb, very good in p+p
 Contribution from QGP is fairly large (might be difficult to separate)



SHM: $T=170$ MeV ; $\gamma_S = 0.95$; $V_0=70$ fm³ (measured p_T spectrum) +
 $\sigma_{clust}^y(\sqrt{s}) = \ln(\sqrt{s}/2m_p)$ | $\langle p_T \rangle = \sqrt{2/3} M_{clust}$ with $\sigma_{p_T} = M_{clust}/2$
 PHSD: No tuning, internal switches as at RHIC

In medium modification of ρ^0

dropping mass

$$m^* = m_0(1 - \alpha \rho/\rho_0)$$

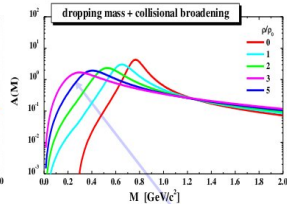
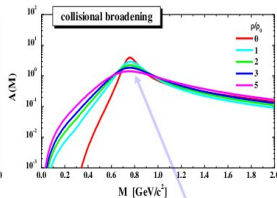
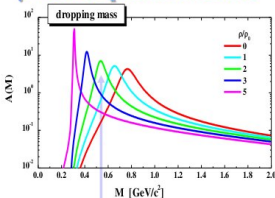
collisional broadening

$$\Gamma(M, \rho) = \Gamma_{\text{vac}}(M) + \Gamma_{\text{CB}}(M, \rho)$$

dropping mass + coll. broad.

$$m^* \text{ \& } \Gamma_{\text{CB}}(M, \rho)$$

$$\text{Collisional width } \Gamma_{\text{CB}}(M, \rho) = \gamma \rho \langle \sigma v_N^{\text{tot}} \rangle$$

 ρ -meson spectral function:Consequences when increasing the baryon density ρ :

➤ pole position m_0 : shift to low M

➤ pole position m_0 : unchanged

➤ pole position m_0 : shift to low M

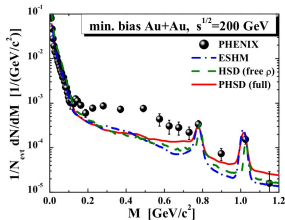
➤ spectral function : narrowing

➤ spectral function : broadening

➤ spectral function : broadening

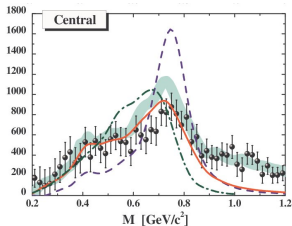
In medium effects: broadening of spectral functions

Dynamical broadening of vector mesons important in In+In at 158A GeV \Rightarrow
 (short QGP, long HRG) **excess only** \Rightarrow

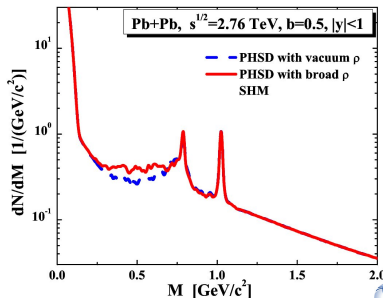


$\leq 20\%$ effect at LHC \Rightarrow
 (long QGP, short HRG)

Baryons modify ρ^0 the most
 \Rightarrow effects stronger at SPS

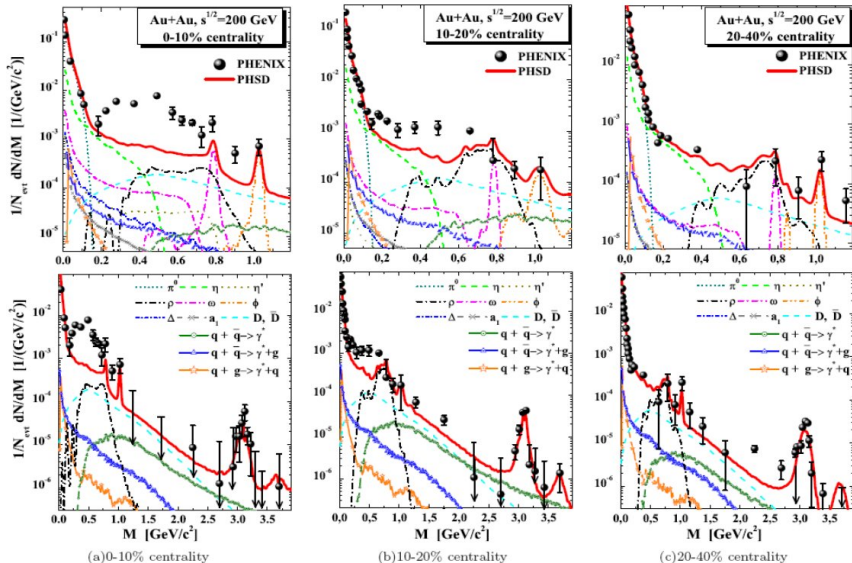


\Leftarrow Lesser impact in A+A at RHIC
 (longer QGP, short HRG)

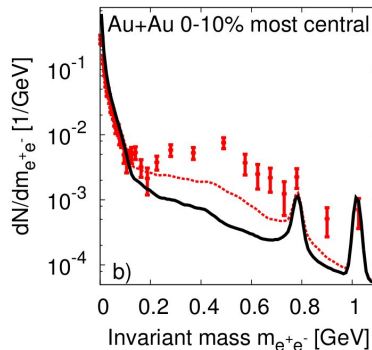
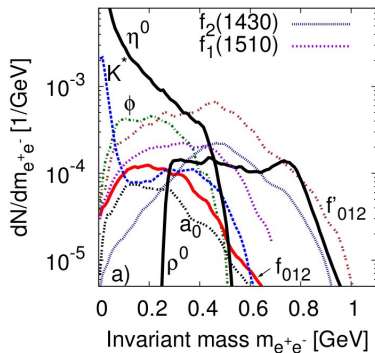


The PHENIX excess

PRC85,024910



Excited mesons and other exotic contributions



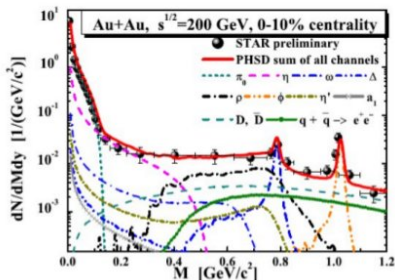
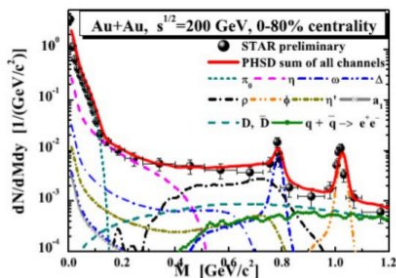
Exotic states may contribute to the PHENIX excess:



Upper limit estimate still below the PHENIX data

PHSD agree with the STAR data

PRC85,024910



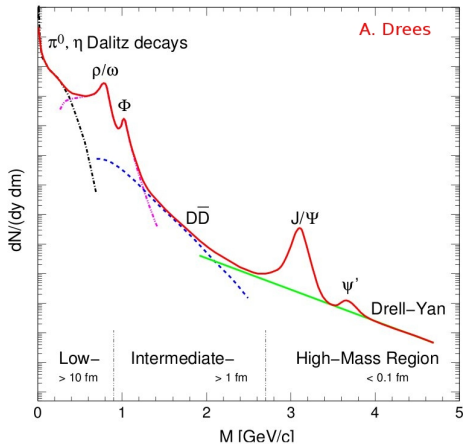
J. Harris, TURIC2012: STAR excess ≈ 2 (preliminary data)...

...with standard cocktail calculation

Broadening of ρ^0 lifts the excess region in PHSD with factor of ≈ 2

\Rightarrow Indication of in-medium effects in action at RHIC

Correlated open heavy flavour feed IMR



Extended SHM for open heavy flavour production

Open heavy flavor is assumed to be in relative chemical equilibrium

Relative yields of 6 (18) lowest D (B) mesons evaluated within SHM

with $T=170\text{MeV}$; $\gamma_S^{\text{hard}}=0.3$; $\mu_{\{B,S,Q\}} = 0$

p+p: $\sigma_{\bar{c}c}^{\text{tot}}(2.76\text{TeV})=3.6\text{mb}$ (experimental data) (or $\gamma_c \approx 30$)

p+p: $\sigma_{\bar{b}b}^{\text{tot}}(2.76\text{TeV})=1/40 \sigma_{\bar{c}c}^{\text{tot}}$ (MC@_sHQ)

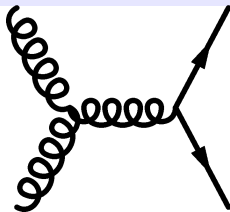
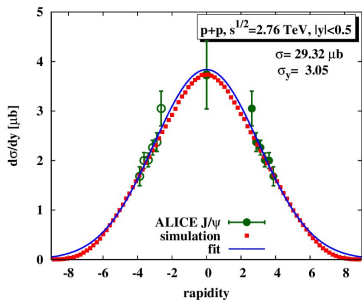
Pb+Pb: $\sigma_{\bar{c}c}^{\text{tot}}(2.76\text{TeV})=N_{\text{bin}}\sigma_{\bar{c}c}^{\text{tot}}(2.76\text{TeV})$ (also $\sigma_{\bar{b}b}^{\text{tot}}$)

	LHCb	ALICE	T=170 MeV	T=150 MeV
$\frac{D^0}{D^{*+}}$	2.20 ± 0.48	2.09	2.40	2.49
$\frac{D^0}{D^+}$	2.07 ± 0.37	2.08	2.37	2.25
$\frac{D^0}{D_s^+}$	7.67 ± 1.67		7.98	8.55
$\frac{D^{*+}}{D^+}$	0.94 ± 0.22	1.00	0.99	0.90
$\frac{D_s^+}{D^+}$	3.48 ± 0.93		3.32	3.44
$\frac{D_s^+}{D^+}$	3.70 ± 0.84		3.37	3.81

Heavy flavour rapidity distributions in $p + p$ collisions

- Modified BGK model **PRC82, 054906**

- $y_{cm} = \operatorname{atanh}\left(\frac{x_1 - x_2}{x_1 + x_2}\right)$
- Probability to find parton along the rapidity axis is defined by a triangle whose maximum is at y_{cm} and goes to zero at $y = \operatorname{asinh}(x_1\sqrt{s}/2m_N)$ and $y = -\operatorname{asinh}(x_2\sqrt{s}/2m_N)$.



All $c\bar{c}$ ($b\bar{b}$) due to $g + g \rightarrow g \rightarrow c\bar{c}$

Assume the same model describes all charmed rapidity distributions

Conversion $\sigma_{tot} \leftrightarrow \frac{d\sigma}{dy}_{y \approx 0}$

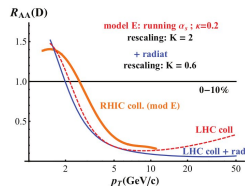
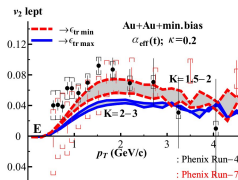
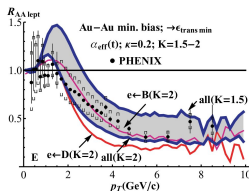
Heavy flavour p_T and energy loss

PRC78,014904

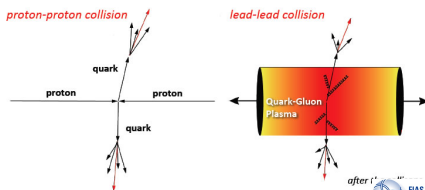
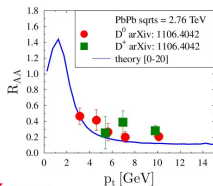
pQCD: c and b quark cross sections & initial momentum

MC@HQ evolution: running coupling & improved infrared regulator
 HQ propagate in Heinz & Kolb hydro background

→ simultaneous R_{AA} and v_2 @ RHIC ($K_{coll} = 2$; $K_{coll+rad} = 0.6$)



The model is in agreement with preliminary R_{AA} of D mesons at LHC

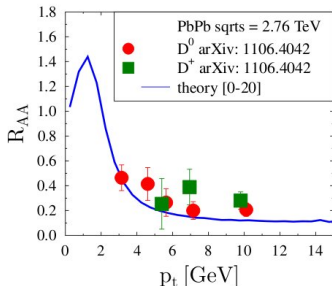
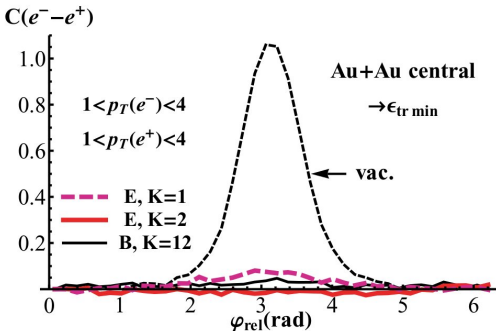


Angular correlations of open heavy flavour mesons at LHC (in)

p+p: π correlations among heavy flavour mesons == hardest (up limit)

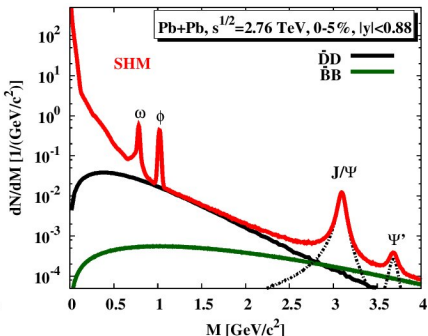
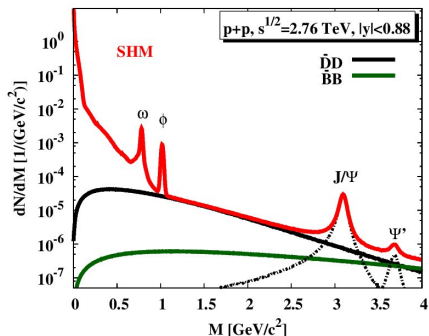
central Pb+Pb: correlations are washed out == softest (low limit)

$$P_{corr} \sim R_{AA}^2 < 10\%$$



Angular correlations of open heavy flavor mesons (out)

p+p: exact back-to-back correlations among heavy flavour mesons
 central Pb+Pb: correlations are washed out ($P_{corr} \sim R_{AA}^2 < 10\%$)



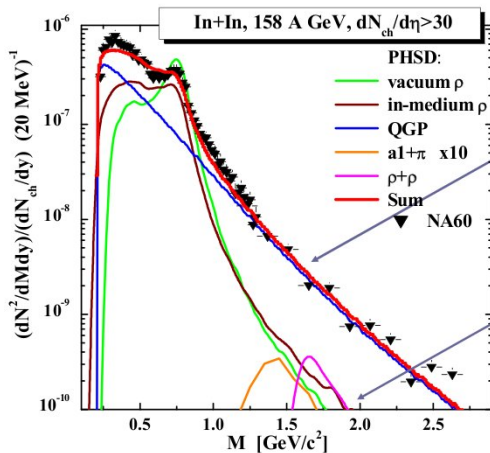
Central Pb+Pb: $J/\psi = 0.3 N_{bin} J/\psi^{pp}$; $\psi' = 0.4 N_{bin} \psi'^{pp}$ PRC85,054905

Vanishing correlations in Pb+Pb \rightarrow softer M spectrum (both D & B)

$m_b > m_c \rightarrow$ due to, energy loss, D mesons M spectrum softens

more than B mesons M spectrum in Pb+Pb (model dependent \times ing)

Acceptance corrected NA60 data



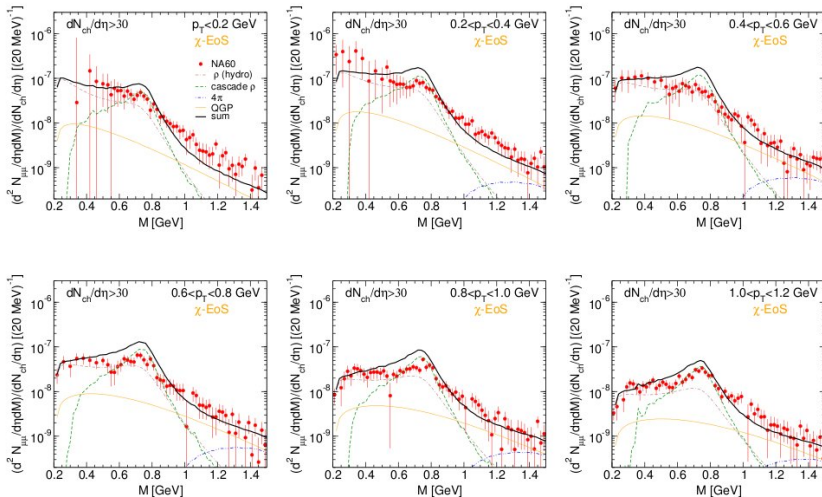
Mass region above
1 GeV is dominated by
partonic radiation

4 π contribution
subdominant

Preliminary

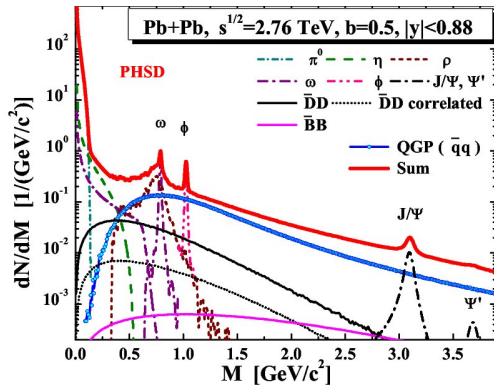
QGP radiation at SPS with hydro partons

PRC84,014901



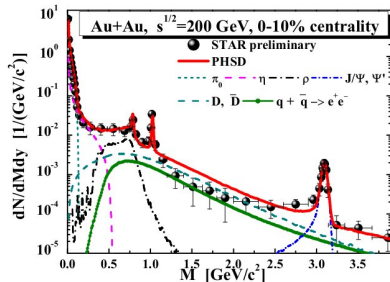
Hybrid mode of **UrQMD** (transport-hydro-cascade) also highlights the role of QGP at SPS

Di-electron radiation from QGP in Pb+Pb 2.76 TeV

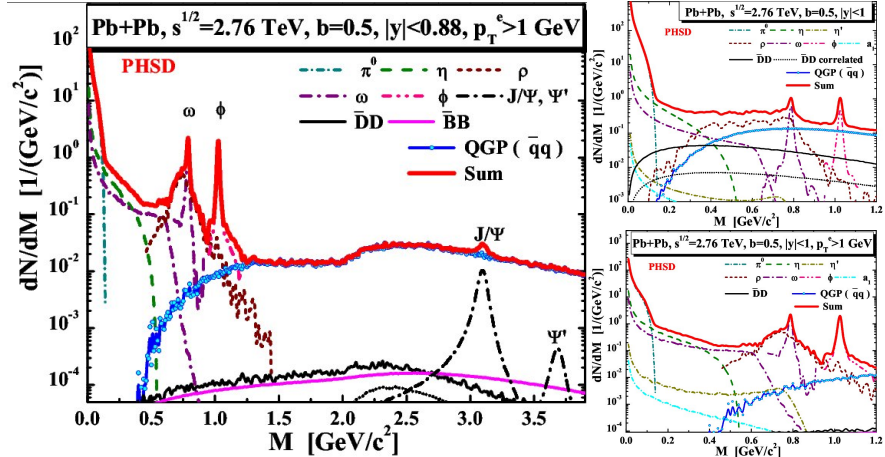


QGP dominates the $M \in [M_\phi : M_{J/\psi}]$
over heavy flavor radiation at LHC

Di-electrons provide a unique window to
detect and study properties of QGP at LHC



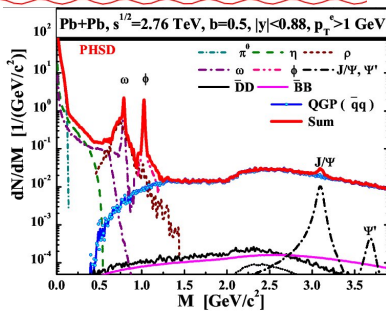
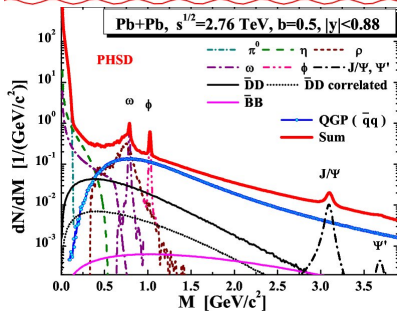
RHIC open charm \approx QGP
large un-certainty in $\sigma_{\bar{c}c}$
 \Rightarrow no strong conclusions

QGP contribution can be enhanced with p_T cuts

Choose $p_T^e > 1\text{GeV} \Rightarrow$ QGP dominates intermediate/high mass regions
 LHC open heavy \ll QGP within $\sigma_{\bar{c}c}$ un-certainties

Summary

- ◇ STAR excess can be understood with collisional broadening
- ◇ Realistic predictions for all relevant di-electron sources at LHC
- ◇ QGP dominate di-electron radiation in intermediate mass region
- ◇ QGP contribution can be enhanced by suitable p_T cuts



Back-up slides

Relevant channels at RHIC and LHC

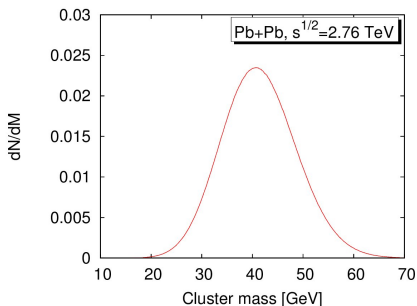
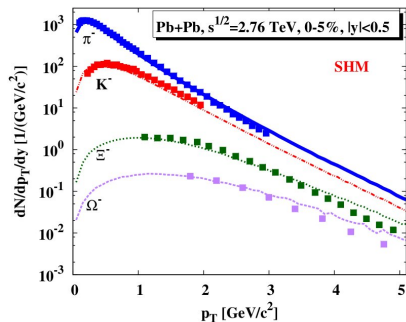
Hadron	direct	Dalitz	other
π^0	-	$\pi^0 \rightarrow \gamma e^+ e^-$	-
η^0	-	$\eta^0 \rightarrow \gamma e^+ e^-$	$\eta^0 \rightarrow \pi^+ \pi^- e^+ e^-$
η'	-	$\eta' \rightarrow \gamma e^+ e^-$	$\eta' \rightarrow \pi^+ \pi^- e^+ e^-$
ρ^0	$\rho^0 \rightarrow e^+ e^-$	-	-
ω^0	$\omega^0 \rightarrow e^+ e^-$	-	$\omega^0 \rightarrow \pi^0 e^+ e^-$
ϕ^0	$\phi^0 \rightarrow e^+ e^-$	-	$\phi^0 \rightarrow \eta e^+ e^-$
J/ψ	$J/\psi \rightarrow e^+ e^-$	$J/\psi \rightarrow \gamma e^+ e^-$	
ψ'	$\psi' \rightarrow e^+ e^-$	$\psi' \rightarrow \gamma e^+ e^-$	-
D mesons	-	-	$D^\pm \rightarrow e^\pm \nu_e + X$
B mesons	-	-	$B \rightarrow e^\pm \nu_e + X$

Convention: Only channels with definite BR:s are taken into account

Beyond standard cocktail contributions

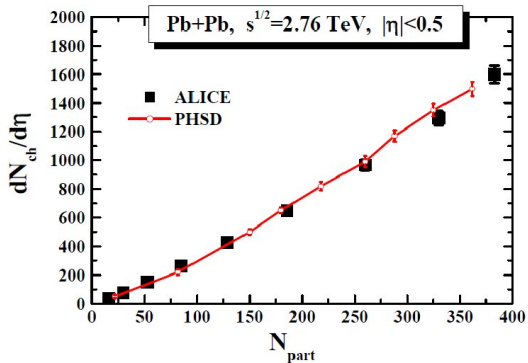
Hadron			
$f_0(980)$	K^+K^-	$K^0\bar{K}^0$	-
$f_1(1285)$	-	-	$K\bar{K}\pi$
$f_2(1270)$	K^+K^-	$K^0\bar{K}^0$	-
$f'_0(1350)$	K^+K^-	$K^0\bar{K}^0$	-
$f'_1(1420)$	$K^{*+}K^- + \text{c.c}$	$K^{*0}K^0 + \text{c.c}$	-
$f'_2(1525)$	K^+K^-	$K^0\bar{K}^0$	-
$f_0(1500)$	K^+K^-	$K^0\bar{K}^0$	-
$f_1(1510)$	$K^{*+}K^- + \text{c.c}$	$K^{*0}K^0 + \text{c.c}$	-
$f_2(1430)$	K^+K^-	$K^0\bar{K}^0$	-
ϕ	K^+K^-	$K^0\bar{K}^0$	-
$a_0^0(980)$	K^+K^-	$K^0\bar{K}^0$	-
$K(892)^\pm$	$K^\pm\pi^0$	-	-
$K(892)^0$	$K^0\pi^0$	-	-

SHM transverse momentum spectra in Pb+Pb at 2.76 TeV



In thermal equilibrium, energy is shared equally among available forms
 \Rightarrow In each event in the rest frame of the cluster $M_{clust} = \sum_i E_i$
 Transverse momentum of the cluster in LAB frame is normally distributed with $\langle |\vec{p}_{clust}| \rangle = M_{clust}$ and $\sigma_{p_T} = M_{clust}/2$

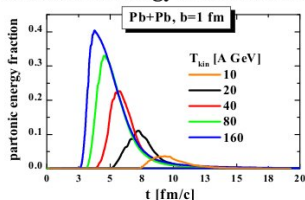
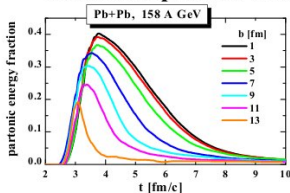
PHSD charged hadron rapidity densities in Pb+Pb 2.76 TeV



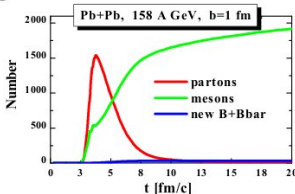
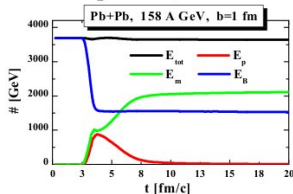
Energy fraction in partonic phase



Increase of partonic energy fraction with energy and centrality

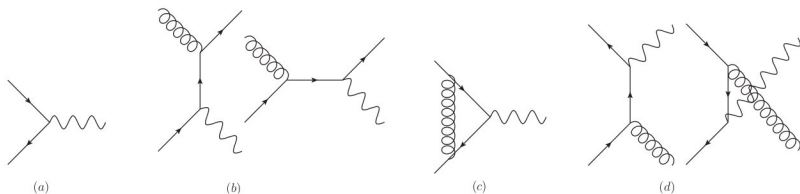


In central Pb + Pb at 158 A GeV about 40% of the converted energy goes to partons; the rest is in the ,large' hadronic corona!



Cassing & Bratkovskaya, NPA 831, 215 (2009)

Di-lepton radiation from quark-gluon-plasma



(a) QGP Drell-Yan

dominates

(b) gluon-Compton scattering

un-important

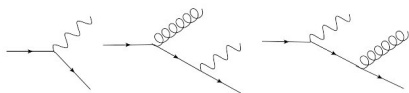
(c) vertex correction

un-important

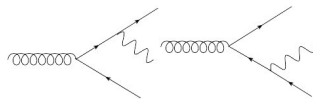
(d) gluon bremsstrahlung

2nd most important

+ radiation from virtual partons

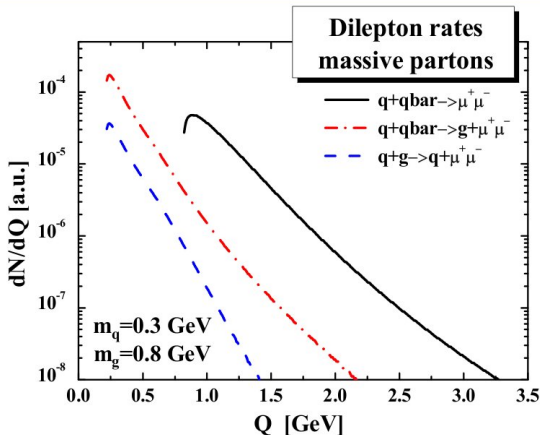
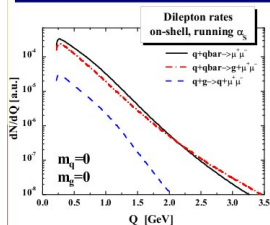


virtual quark decay



virtual gluon decay

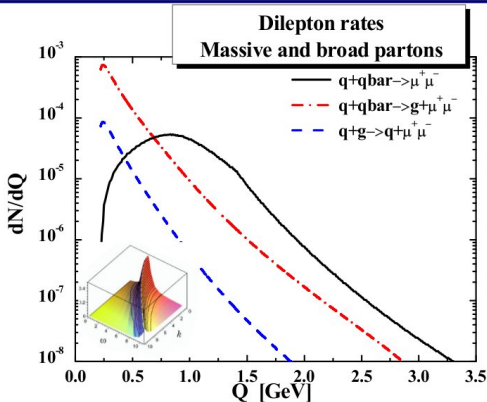
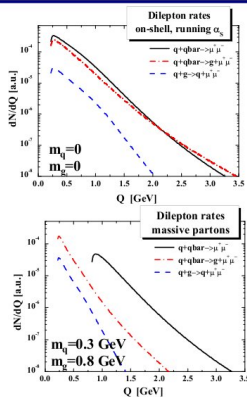
Dilepton rates from **massive** quarks/gluons



Note: Threshold in the Born contribution due to finite masses of incoming particles.

O. L., arXiv:1004.2591

Massive and broad quarks and gluons



Due to broad spectral functions of partons, the threshold of the Born term is smeared, the contributions of the 2→2 processes increased.

O. L., arXiv:1004.2591

The Dynamical QuasiParticle Model (DQPM)

Basic idea: Interacting quasiparticles

- massive quarks and gluons (g, q, q_{bar}) with spectral functions :

$$\rho(\omega) = \frac{\gamma}{E} \left(\frac{1}{(\omega - E)^2 + \gamma^2} - \frac{1}{(\omega + E)^2 + \gamma^2} \right)$$

$$E^2 = p^2 + M^2 - \gamma^2$$

■ quarks

mass: $m^2(T) = \frac{N_c^2 - 1}{8N_c} g^2 \left(T^2 + \frac{\mu_q^2}{\pi^2} \right)$

width: $\gamma_q(T) = \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{4\pi} \ln \frac{c}{g^2}$

running coupling: $\alpha_S(T) = g^2(T)/(4\pi)$

$$g^2(T/T_c) = \frac{48\pi^2}{(11N_c - 2N_f) \ln(\lambda^2(T/T_c - T_s/T_c)^2)}$$

➤ fit to lattice (IQCD) results (e.g. entropy density)

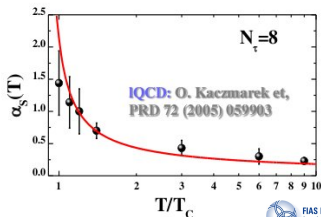
with 3 parameters: $T_s/T_c=0.46$; $c=28.8$; $\lambda=2.42$

■ gluons:

A. Peshier, PRD 70 (2004) 034016

$$M^2(T) = \frac{g^2}{6} \left((N_c + \frac{1}{2}N_f) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right) \quad N_c = 3, N_f = 3$$

$$\gamma_g(T) = N_c \frac{g^2 T}{4\pi} \ln \frac{c}{g^2}$$

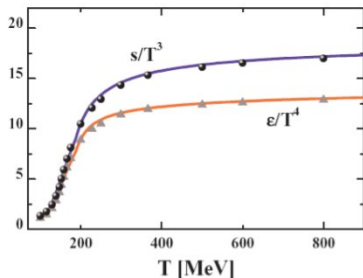


DQPM thermodynamics ($N_f=3$) and IQCD

entropy $s = \frac{\partial P}{\partial T} \rightarrow$ pressure P

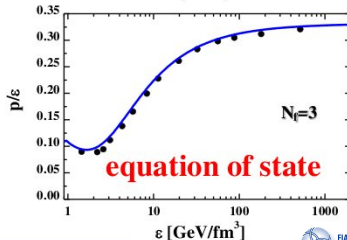
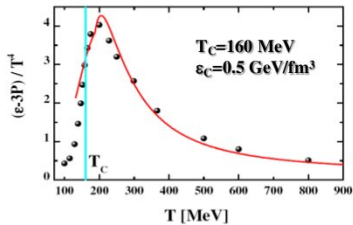
energy density: $\epsilon = Ts - P$

IQCD: Wuppertal-Budapest group
Y. Aoki et al., JHEP 0906 (2009) 088.



interaction measure:

$$W(T) := \epsilon(T) - 3P(T) = Ts - 4P$$



Meson decay formulae

$$\frac{d\Gamma^{X \rightarrow \gamma I^+ I^-}}{dM} = \frac{\Gamma^{X \rightarrow I^+ I^-}}{M} \frac{4\alpha}{3\pi} \sqrt{1 - \frac{4m_I^2}{M^2}} \times \left(1 + \frac{2m_I^2}{M^2}\right) \left(1 - \frac{M^2}{m_X^2}\right)^3 |F^{X \rightarrow \gamma\gamma}(M)|^2$$

$$F^{\eta \rightarrow \gamma\gamma}(M) = \left(1 - \frac{M^2}{(0.72\text{GeV})^2}\right)^{-1}$$

$$|F^{\eta' \rightarrow \gamma\gamma}(M)|^2 = \frac{(0.75\text{GeV})^4}{((0.75\text{GeV})^2 - M^2)^2 + (0.105\text{GeV}^2)^2}$$

$$F^{\pi^0 \rightarrow \gamma\gamma}(M) = 1 + \frac{5.5}{\text{GeV}^2} M^2$$

$$|F^{\omega \rightarrow \pi^0 I^+ I^-}(M)|^2 = \frac{(0.65\text{GeV})^4}{((0.65\text{GeV})^2 - M^2)^2 + (0.0488\text{GeV}^2)^2}$$

$$\begin{aligned} \frac{d\Gamma^{\omega \rightarrow \pi^0 I^+ I^-}}{dM} &= \frac{\Gamma^{\omega \rightarrow \pi^0 \gamma}}{M} \frac{2\alpha}{3\pi} \sqrt{1 - \frac{4m_I^2}{M^2}} \left(1 + \frac{2m_I^2}{M^2}\right) \\ &\times \left[\left(1 + \frac{M^2}{m_\omega^2 - m_\pi^2}\right)^2 - \frac{4m_\omega^2 M^2}{(m_\omega^2 - m_\pi^2)^2} \right]^{3/2} |F^{\omega \rightarrow \pi^0 I^+ I^-}(M)|^2 \end{aligned}$$

Direct decays

$$\Gamma^{V \rightarrow l^+ l^-}(M) = \frac{m_0^3}{M^3} \Gamma^{V \rightarrow l^+ l^-}(m_0)$$

$$\Gamma_{tot}^{\rho^0}(M) \simeq \Gamma^{\rho \rightarrow \pi\pi} = \Gamma(m_0) \left(\frac{m_0}{M}\right)^2 \frac{(M^2 - 4m_\pi^2)^{3/2}}{(m_0^2 - 4m_\pi^2)^{3/2}}$$

J/ψ Dalitz

$$\frac{d\Gamma^{X \rightarrow l^+ l^- \gamma}}{dM} = \frac{\alpha}{\pi} \frac{2M}{m_X^2 - M^2} \left(1 + \frac{M^4}{m_X^4}\right) \times \left(\ln \frac{1+r}{1-r} - r\right) \Gamma_0^{X \rightarrow l^+ l^-}$$