

# Theory and Phenomenology of Composite 2-Higgs Doublet Models



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Based on: SDC, S. Moretti, K. Yagyu and E. Yildirim, Phys.Rev.D94 (2016);  
arXiv:1610.02687[hep-ph]; in preparation.

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# Motivations and Outline

- ☑ The search for additional Higgses is one of the most important tasks of the LHC. Moreover, extra spineless states can induce sizeable effects in the couplings of the discovered one
- ☑ From a theoretical point of view, extra Higgses do not give an explanation for naturalness. Their pNGB nature can link them to natural theories at the weak scale
- ☑ Focus on Composite Two Higgs Doublet Models (C2HDMs) emerging from specific symmetry breaking patterns. Results for  $SO(6) \rightarrow SO(4) \times SO(2)$
- ☑ Perturbative unitarity and vacuum stability properties of the C2HDM
- ☑ Phenomenology at the LHC of the different Yukawa Type C2HDMs and comparison with the Elementary 2HDM predictions
- ☑ Phenomenology at future  $e^+e^-$  colliders (preliminary)

# Generalities on Extended Composite Higgs Models

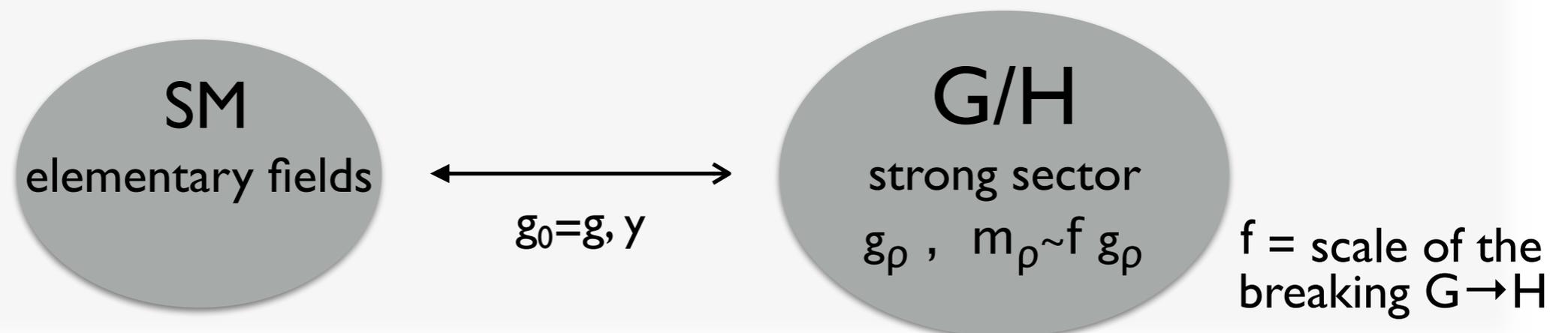
Models with a larger Higgs structure with respect to the SM have been proposed  
—> 2HDMs offer a rich phenomenology in EW and flavour physics

☑ In 2HDMs, as in the SM, the Higgs sector is very sensitive to UV physics —> Hierarchy problem

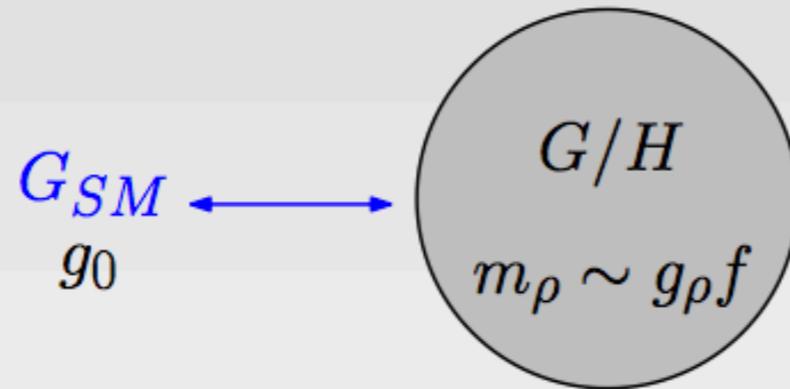
**Is it Naturalness a good guideline?**

The most popular solution, Supersymmetry, requires two Higgs doublets with specific Yukawa and potential terms

A **natural alternative** is to consider the Higgs bosons as composite states from a strong sector. They can be lighter than the strong scale if they are pNGBs of G/H



# Higgs as a Composite Pseudo Goldstone Boson



Kaplan, Georgi '80s

The basic idea

- ▶ Higgs as **Goldstone Boson** of  $G/H$  in a **strong** sector
- ▶ An idea already realized for pions in QCD

How to get an Higgs mass?

- ▶  $G$  is only an approximate global symmetry  $g_0 \rightarrow V(h)$
- ▶ EWSB as in the SM
- ▶ And the hierarchy problem?  
no Higgs mass term at tree level

$$\rightarrow \delta m_h^2 \sim \frac{g_0^2}{16\pi^2} \Lambda_{com}^2$$



# Characteristics of a Composite Higgs

It is not a true (SM-like) Higgs...

$$\mathcal{L} = \frac{1}{2}(\partial_\mu h)^2 + V(h) + \frac{v^2}{4} \text{Tr}[(D_\mu \Sigma)^\dagger (D^\mu \Sigma)] \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} + \dots \right) - \frac{v}{\sqrt{2}} \sum_{i,j} (\bar{u}_L^i \bar{d}_L^i) \Sigma \begin{pmatrix} \lambda_{ij}^u u_R^j \\ \lambda_{ij}^d d_R^j \end{pmatrix} \left( 1 + c \frac{h}{v} + \dots \right) + \mathcal{L}_{SM,h}$$

$$\Sigma = e^{i \frac{\sigma^a \chi^a}{v}}$$

- ▶ SM Higgs for a  $a = b = c = 1$
- ▶ GB Higgs  $a = \sqrt{1 - v^2/f^2}$ ,  $b = 1 - 2 v^2/f^2$  SM limit  $f \rightarrow \infty$
- ▶ Composite Higgs only partly unitarizes WW scattering  $A(s, t, u) \sim \frac{s+t}{f^2}$
- ▶ Up to effects  $v^2/f^2$ , the scalar h behaves as the SM Higgs
- ▶ Technicolor limit  $f = v$

# Extended Composite Higgs Models

J.Mrazek et al.1105.5403; DC,Moretti,Yagyu,Yildirim 1602.06437

- ☑ We characterise models where EWSB is driven by 2 Higgs doublets as pNGBs of new dynamics above the weak scale
- ☑ We focus on models based on  $SO(6)/SO(4) \times SO(2)$ . The unbroken group contains the custodial  $SO(4)$ . The spectrum of the GBs is completely fixed by the coset and it is given by 2 Higgs 4-plets
- ☑ The low-energy effective Lagrangian stands on few specific assumptions about the strong sector: the global symmetries, the SSB pattern, the sources of explicit breaking. At the leading 2-derivative order, the non-linear  $\sigma$ -model interactions are fixed in terms of a unique parameter  $f$  (compositeness scale)
- ☑ Elementary fields are linearly coupled to the strong sector (partial compositeness)  
$$\mathcal{L}_{\text{mix}} = g_0 (\psi_{\text{SM}} \mathcal{O}) \quad \psi_{\text{SM}} = (A_\mu, f) \quad g_0 = g, y$$
- ☑ The SM fields have a degree of mixing  $\sim g_0/g_\rho$ . Realistic models  $g_0 < g_\rho < 4\pi$
- ☑  $\mathcal{L}_{\text{mix}}$  breaks the global symm. of the strong sector, the Higgses become pNGBs and acquire a potential

# Extended Composite Higgs Models

- ✓ Crucial property is the presence of **discrete symmetries** in addition to the custodial  $SO(4)$ , to **control the T-parameter** (this because in non-minimal models, even though the non-linear interactions satisfy  $SO(4)$ , a contribution to T can arise for a generic vacuum structure [J.Mrazek et al.1105.5403](#))
- ✓ Discrete symmetries also **protect** from **Higgs-mediated Flavour Changing Neutral Currents**
- ✓ Besides CP, **impose a  $C_2$  discrete symmetry** ([J.Mrazek et al.1105.5403](#)) distinguishes the 2 Higgs doublets and restricts the form of the Higgs potential and the Yukawa couplings (analogous of  $Z_2$  in E2HDM)
- ✓ Two classes of models: 1) **exact discrete  $C_2$  symmetry (inert case)** — the second Higgs does not couple to the SM fields 2) **softly-broken  $C_2$  symmetry (active case)** which controls the T parameter and FCNC

# The model - 2 Higgs Doublets as pNGBs

J.Mrazek et al.1105.5403; DC,Moretti,Yagyu,Yildirim 1602.06437

Analogue of the construction in non-linear sigma models developed by Callan-Coleman-Wess-Zumino (CCWZ)

The kinetic Lagrangian invariant under the SO(6) is:

$$\mathcal{L}_{\text{kin}} = \frac{f^2}{4} (d_{\alpha}^{\hat{a}})_{\mu} (d_{\alpha}^{\hat{a}})^{\mu}; \quad (d_{\alpha}^{\hat{a}})_{\mu} = i \text{tr}(U^{\dagger} D_{\mu} U T_{\alpha}^{\hat{a}})$$

GB matrix  $U = \exp\left(i \frac{\Pi}{f}\right)$

$\alpha = 1, 2 \quad \hat{a} = 1, \dots, 4$   
are the 8 broken SO(6) generators

$$\Pi \equiv \sqrt{2} h_{\alpha}^{\hat{a}} T_{\alpha}^{\hat{a}} = -i \begin{pmatrix} 0_{4 \times 4} & h_1^{\hat{a}} & h_2^{\hat{a}} \\ -h_1^{\hat{a}} & 0 & 0 \\ -h_2^{\hat{a}} & 0 & 0 \end{pmatrix} \quad \Phi_{\alpha} \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} h_{\alpha}^2 + i h_{\alpha}^1 \\ h_{\alpha}^4 - i h_{\alpha}^3 \end{pmatrix}$$

$$h_{\alpha}^4 = \tilde{h}_{\alpha} = h_{\alpha} + v_{\alpha}$$

covariant derivative:  $D_{\mu} = \partial_{\mu} - ig T_L^a W_{\mu}^a - ig' Y B_{\mu}$

$$v^2 \equiv v_1^2 + v_2^2$$

the gauge boson masses are generated by the VEVs of the fourth components of the Higgs fields

$$m_W^2 = \frac{g^2}{4} f^2 \sin^2 \frac{v}{f} \rightarrow v_{\text{SM}}^2$$

# The model - 2 Higgs Doublets as pNGBs

Similarly to E2HDM, define the **Higgs basis**: only one doublet contains  $v$  and the NGs of W,Z

$$\begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix} = \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} \Phi \\ \Psi \end{pmatrix}$$

$$\tan \beta = v_2/v_1$$

$$\Phi = \begin{pmatrix} G^+ \\ \frac{v+h'_1+iG^0}{\sqrt{2}} \end{pmatrix}, \quad \Psi = \begin{pmatrix} H^+ \\ \frac{h'_2+iA}{\sqrt{2}} \end{pmatrix}$$

$A$  CP-odd  
 $h'_{1,2}$  CP-even

By expanding the kinetic term up to  $O(1/f^2)$  we get **non canonical** forms for  $G_0$ ,  $G^\pm$ ,  $h'_2$  we rescale according to:

$$G^+ \rightarrow \left(1 - \frac{\xi}{3}\right)^{-1/2} G^+, \quad G^0 \rightarrow \left(1 - \frac{\xi}{3}\right)^{-1/2} G^0, \quad h'_2 \rightarrow \left(1 - \frac{\xi}{3}\right)^{-1/2} h'_2$$

$$\xi = \frac{v_{\text{SM}}^2}{f^2}$$

The mass eigenstates of the CP-even scalars are defined by introducing the **mixing angle  $\Theta$**

$$\begin{pmatrix} h'_1 \\ h'_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ H \end{pmatrix}$$

identified with the Higgs discovered at the LHC

determined by the mass matrix from the Higgs potential

# Higgs potential in C2HDM

- ☑ The Higgs potential is generated at loop level
  - gauge boson loops give a positive squared-mass term
  - fermion loops can provide a negative squared-mass term and trigger EWSB
  
- ☑ Studied by [J.Mrazek et al. 1105.5403](#) in the SO(6)/SO(4)×SO(2) model for **several reps. of fermion fields** **assuming** that all the **explicit breaking** is associated with the couplings of the strong sector to the SM fields **due to Yukawa (y) and gauge (g) couplings** (by relaxing this hypothesis the parameter space could be enlarged)
  
- ☑ They obtain **the general E2HDM potential** with parameters expressed in terms of those in the **strong sector** and **the explicit breaking ones** (at each order in y and g, it is parameterized by a limited number of coefficients which depend on the fermion representation)

$$\begin{aligned}
 V(\Phi_1, \Phi_2) = & \frac{1}{2}m_{11}^2 \text{Tr}[\Phi_1^\dagger \Phi_1] + \frac{1}{2}m_{22}^2 \text{Tr}[\Phi_2^\dagger \Phi_2] + \frac{1}{2} \text{Tr}[\Phi_1^\dagger \Phi_2 (m_{12}^2 + i\tilde{m}_{12}^2 \sigma_3)] \\
 & + \frac{1}{4}\lambda_1 \text{Tr}^2[\Phi_1^\dagger \Phi_1] + \frac{1}{4}\lambda_2 \text{Tr}^2[\Phi_2^\dagger \Phi_2] + \frac{1}{4}\lambda_3 \text{Tr}[\Phi_1^\dagger \Phi_1] \text{Tr}[\Phi_2^\dagger \Phi_2] \\
 & + \frac{1}{4}\lambda_4 \text{Tr}^2[\Phi_1^\dagger \Phi_2] + \frac{1}{4}\tilde{\lambda}_4 \text{Tr}^2[\Phi_1^\dagger \Phi_2 \sigma_3] + i\frac{1}{4}\lambda_5 \text{Tr}[\Phi_1^\dagger \Phi_2] \text{Tr}[\Phi_1^\dagger \Phi_2 \sigma_3] \\
 & + \frac{1}{4} \text{Tr}[\Phi_1^\dagger \Phi_1] \text{Tr}[\Phi_1^\dagger \Phi_2 (\lambda_6 + i\tilde{\lambda}_6 \sigma_3)] + \frac{1}{4} \text{Tr}[\Phi_2^\dagger \Phi_2] \text{Tr}[\Phi_1^\dagger \Phi_2 (\lambda_7 + i\tilde{\lambda}_7 \sigma_3)]
 \end{aligned}$$

$$V = \frac{m_\rho^4}{16\pi^2} \sum_{n_R, n_L} \frac{1}{(g_\rho^2)^{n_R+n_L}} \sum_{\delta} c_\delta^{(n_R, n_L)} \mathcal{I}_{(n_R, n_L)}^\delta$$

small coupling expansion

SO(6) invariant operators constructed with the NGBs

Contribution to the parameters of the general C2HDM potential from fermions in the 6

operator	$\mathcal{I}_{(0,1)}^1$	$\mathcal{I}_{(1,0)}^1$	$\mathcal{I}_{(2,0)}^1$	$\mathcal{I}_{(2,0)}^4$	$\mathcal{I}_{(2,0)}^5$	$\mathcal{I}_{(1,1)}^1$	$\mathcal{I}_{(1,1)}^5$	$\mathcal{I}_{(1,1)}^6$	$\mathcal{I}_{(0,2)}^1$	$\mathcal{I}_{(0,2)}^4$
$\frac{1}{16\pi^2} \times$	$-\frac{y_L^2 g_\rho^2}{2}$	$y_R^2 g_\rho^2$	$\frac{y_R^4}{4}$	$\frac{y_R^4}{4} \left(\frac{g_\rho}{4\pi}\right)^2$	$\frac{y_R^4}{4} \left(\frac{g_\rho}{4\pi}\right)^2$	$\frac{y_R^2 y_L^2}{4}$	$y_R y_L^2 \left(\frac{g_\rho}{4\pi}\right)^2$	$-y_R^2 y_L^2 \left(\frac{g_\rho}{4\pi}\right)^2$	$-\frac{y_L^4}{2}$	$-y_L^4 \left(\frac{g_\rho}{4\pi}\right)^2$
$m_{11}^2/f^2$	1	$\cos^2 \theta$	0	0	0	$\cos^2 \theta$	$\cos^2 \theta$	0	1	1
$m_{22}^2/f^2$	1	$\sin^2 \theta$	0	0	0	$\sin^2 \theta$	$\sin^2 \theta$	0	1	1
$m_{12}^2/f^2$	0	0	0	0	$\sin 4\theta$	0	0	0	0	0
$\tilde{m}_{12}^2/f^2$	0	0	0	0	0	$-\sin 2\theta$	0	$\frac{1}{2} \sin 2\theta$	0	0
$\lambda_1$	$-\frac{1}{3}$	$-\frac{1}{3} \cos^2 \theta$	$2 \cos^4 \theta$	$2 \cos^4 \theta$	0	$-\frac{4}{3} \cos^2 \theta$	$-\frac{7}{12} \cos^2 \theta$	0	$-\frac{7}{12}$	$-\frac{11}{24}$
$\lambda_2$	$-\frac{1}{3}$	$-\frac{1}{3} \sin^2 \theta$	$2 \sin^4 \theta$	$2 \sin^4 \theta$	0	$-\frac{4}{3} \sin^2 \theta$	$-\frac{7}{12} \sin^2 \theta$	0	$-\frac{7}{12}$	$-\frac{11}{24}$
$\lambda_3$	0	0	$\sin^2 \theta$	$-\sin^2 \theta$	0	0	$-\frac{1}{4}$	0	0	$-\frac{1}{4}$
$\lambda_4$	$-\frac{2}{3}$	$-\frac{1}{3}$	0	$2 \sin^2 2\theta$	0	$-\frac{4}{3}$	$-\frac{1}{3}$	0	$-\frac{7}{6}$	$-\frac{2}{3}$
$\tilde{\lambda}_4$	0	0	0	0	0	0	0	0	$\frac{1}{2}$	0
$\lambda_5$	0	0	0	0	0	0	0	0	0	0
$\lambda_6$	0	0	0	0	$-\frac{1}{3} \sin 4\theta$	0	0	0	0	0
$\tilde{\lambda}_6$	0	0	0	0	0	$\frac{2}{3} \sin 2\theta$	0	$-\frac{1}{12} \sin 2\theta$	0	0
$\lambda_7$	0	0	0	0	$-\frac{1}{3} \sin 4\theta$	0	0	0	0	0
$\tilde{\lambda}_7$	0	0	0	0	0	$\frac{2}{3} \sin 2\theta$	0	$-\frac{1}{12} \sin 2\theta$	0	0

power counting estimate of the pre-factors up to the fourth-order

The result depends on:

- ▶ the fermionic repr.
- ▶ the explicit breaking assumption
- ▶ the order of the expansion in the degree of mixing

$\xi_0/\xi_\rho$  with  $\xi_0 = \xi, \xi', y_L, y_R$

# Higgs potential in C2HDM DC, Moretti, Yagyu, Yildirim 1602.06437

- ✓ Here we assume the most general CP-conserving E2HDM form for the potential. The masses and couplings of the Higgses are free parameters
- ✓ We will however highlight **parameter space regions where differences can be found between E2HDM and C2HDM** (the compositeness implemented in the kinetic terms and interactions with SM fields)
- ✓ To avoid FCNC's at tree level we impose a discrete  $C_2$  symmetry  $(\Phi_1, \Phi_2) \rightarrow (+\Phi_1, -\Phi_2)$  which could be **exact (inert case)** or **softly broken (active case)**

$$V(\Phi_1, \Phi_2) = m_1^2 \Phi_1^\dagger \Phi_1 + m_2^2 \Phi_2^\dagger \Phi_2 - m_3^2 (\Phi_1^\dagger \Phi_2 + \text{h.c.}) + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{1}{2} \lambda_5 [(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}],$$

$m_3^2$  and  $\lambda_5$  are real,  $M$  defined by  $M^2 = \frac{m_3^2}{s_\beta c_\beta}$  is the soft-breaking  $C_2$  parameter

(The  $C_2$  symm. also avoids anomalous contributions to the T parameter from dim-6 operators  
E. Bertuzzo et al. 1206.2623)

# Mass spectrum for the Active C2HDM

The mass matrices for charged states and the CP-odd scalars are diagonalised by a  $\beta$ -angle rotation

$$\tan\beta = v_2/v_1$$

$$m_{H^\pm}^2 = M^2 - \frac{v^2}{2}(\lambda_4 + \lambda_5), \quad m_A^2 = M^2 - v^2\lambda_5$$

The mass matrix for the CP-even scalars is diagonalised by a  $\Theta$ -angle rotation

$$(M_{\text{even}})_{11}^2 = v^2(\lambda_1 c_\beta^4 + \lambda_2 s_\beta^4 + 2\lambda_{345} c_\beta^2 s_\beta^2),$$

$$(M_{\text{even}})_{22}^2 = \left(1 + \frac{\xi}{3}\right) [M^2 + v^2(\lambda_1 + \lambda_2 - 2\lambda_{345}) s_\beta^2 c_\beta^2],$$

$$(M_{\text{even}})_{12}^2 = v^2 \left(1 + \frac{\xi}{6}\right) [-\lambda_1 c_\beta^2 + \lambda_2 s_\beta^2 + c_{2\beta} \lambda_{345}] s_\beta c_\beta$$

$$\lambda_{345} = \lambda_3 + \lambda_4 + \lambda_5.$$

$$\tan 2\theta = \frac{2(M_{\text{even}})_{12}^2}{(M_{\text{even}})_{11}^2 - (M_{\text{even}})_{22}^2}$$

$$m_h^2 = c_\theta^2 (M_{\text{even}})_{11}^2 + s_\theta^2 (M_{\text{even}})_{22}^2 + 2s_\theta c_\theta (M_{\text{even}})_{12}^2,$$

$$m_H^2 = s_\theta^2 (M_{\text{even}})_{11}^2 + c_\theta^2 (M_{\text{even}})_{22}^2 - 2s_\theta c_\theta (M_{\text{even}})_{12}^2$$

Decoupling limit for large M: the extra Higgses get degenerate with M and  $\Theta \rightarrow 0$   
(the usual 2HDM notation is recovered with  $\Theta = \alpha - \beta - \pi/2$ )

$\lambda_i$  parameters in terms of the masses of the physical Higgs bosons

$$\lambda_1 = \frac{1}{v^2 c_\beta^2} \left[ m_h^2 c_{\beta+\theta}^2 + m_H^2 s_{\beta+\theta}^2 - M^2 s_\beta^2 + \frac{\xi}{3} s_\beta (m_h^2 c_{\beta+\theta} s_\theta - m_H^2 s_{\beta+\theta} c_\theta) \right],$$

$$\lambda_2 = \frac{1}{v^2 s_\beta^2} \left[ m_h^2 s_{\beta+\theta}^2 + m_H^2 c_{\beta+\theta}^2 - M^2 c_\beta^2 - \frac{\xi}{3} c_\beta (m_h^2 s_{\beta+\theta} s_\theta + m_H^2 c_{\beta+\theta} c_\theta) \right],$$

$$\lambda_3 = \frac{1}{v^2} \left[ \frac{2s_{\beta+\theta} c_{\beta+\theta}}{s_{2\beta}} (m_h^2 - m_H^2) + 2m_{H^\pm}^2 - M^2 - \frac{\xi}{3s_{2\beta}} (m_h^2 s_\theta c_{2\beta+\theta} - m_H^2 c_\theta s_{2\beta+\theta}) \right]$$

$$\lambda_4 = \frac{1}{v^2} (M^2 + m_A^2 - 2m_{H^\pm}^2),$$

$$\lambda_5 = \frac{1}{v^2} (M^2 - m_A^2).$$

$$m_h = 125 \text{ GeV}, \quad v = 245 \text{ GeV}$$

Total of 7 free parameters:

$m_H, m_A, m_{H^\pm}, \sin\Theta, \tan\beta, M, \xi$  (or  $f$ )

## Mass spectrum for the Inert C2HDM

$$m_{H^\pm}^2 = m_2^2 + \frac{v^2}{2} \lambda_3, \quad m_H^2 = \left(1 + \frac{\xi}{3}\right) \left(m_2^2 + \frac{v^2}{2} \lambda_{345}\right)$$

$$m_A^2 = m_2^2 + \frac{v^2}{2} (\lambda_3 + \lambda_4 - \lambda_5), \quad m_h^2 = \lambda_1 v^2.$$

$m_3 = M = 0$  ( $C_2$  symm) and  $\langle \Phi_2 \rangle = 0$ ,  $m_2$  sets the scale for the mass of the inert Higgs

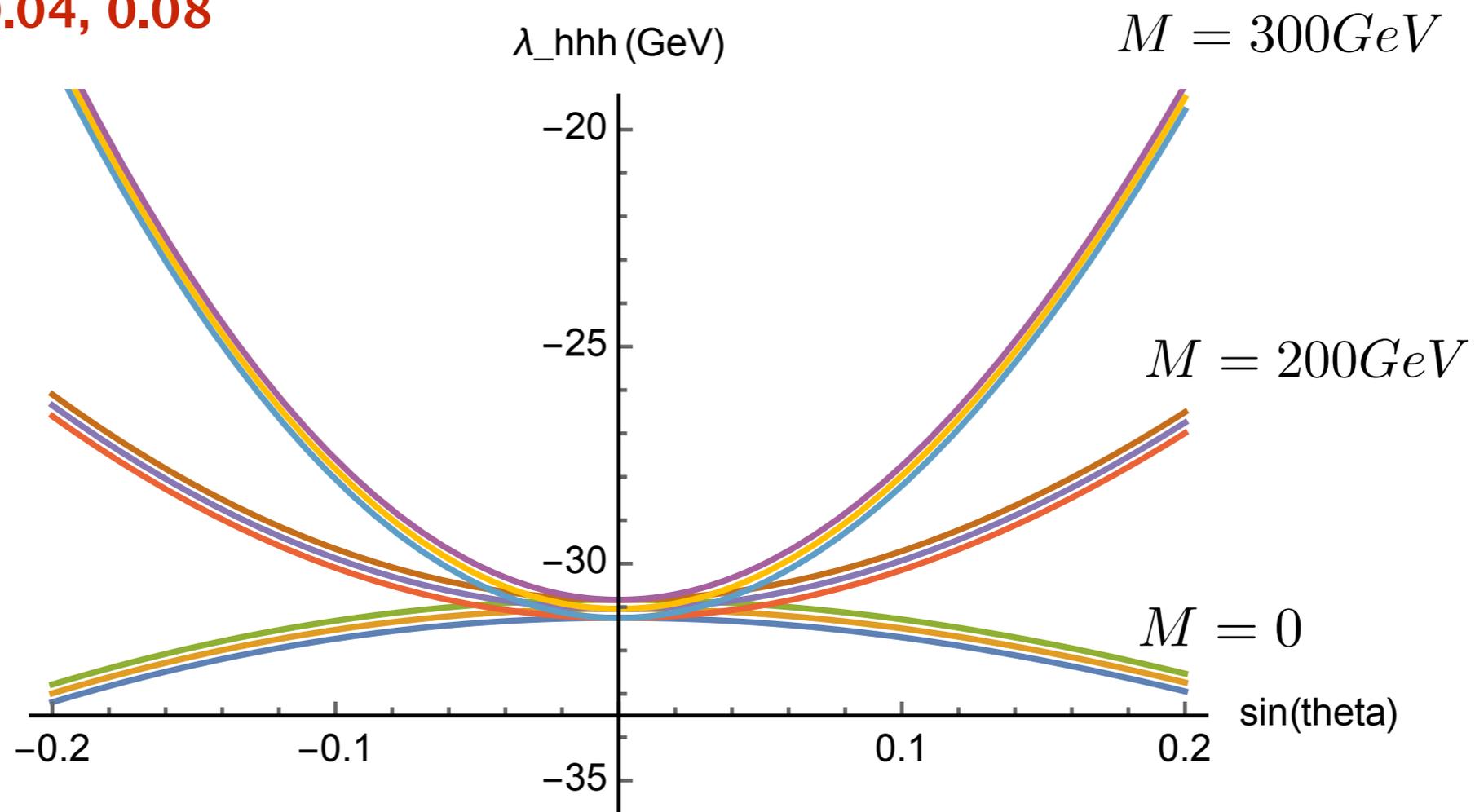
$\Phi_2 \equiv H$  possible candidate for composite neutral dark matter

# Trilinear Higgs self-coupling - role of M

$$\lambda_{hhh} = \frac{1}{4v_{\text{SM}}s_{2\beta}} \left[ (s_{2\beta+3\theta} - 3s_{2\beta+\theta})m_h^2 + 4s_\theta^2s_{2\beta+\theta}M^2 \right] + \frac{\xi}{12v_{\text{SM}}} \left[ c_\theta m_h^2 + 2s_\theta^2M^2(c_\theta + 2s_\theta \cot 2\beta) \right] + \mathcal{O}(\xi^2)$$

$\tan\beta=1$  (nearly independent of  $\tan\beta$  for small  $\Theta$ )

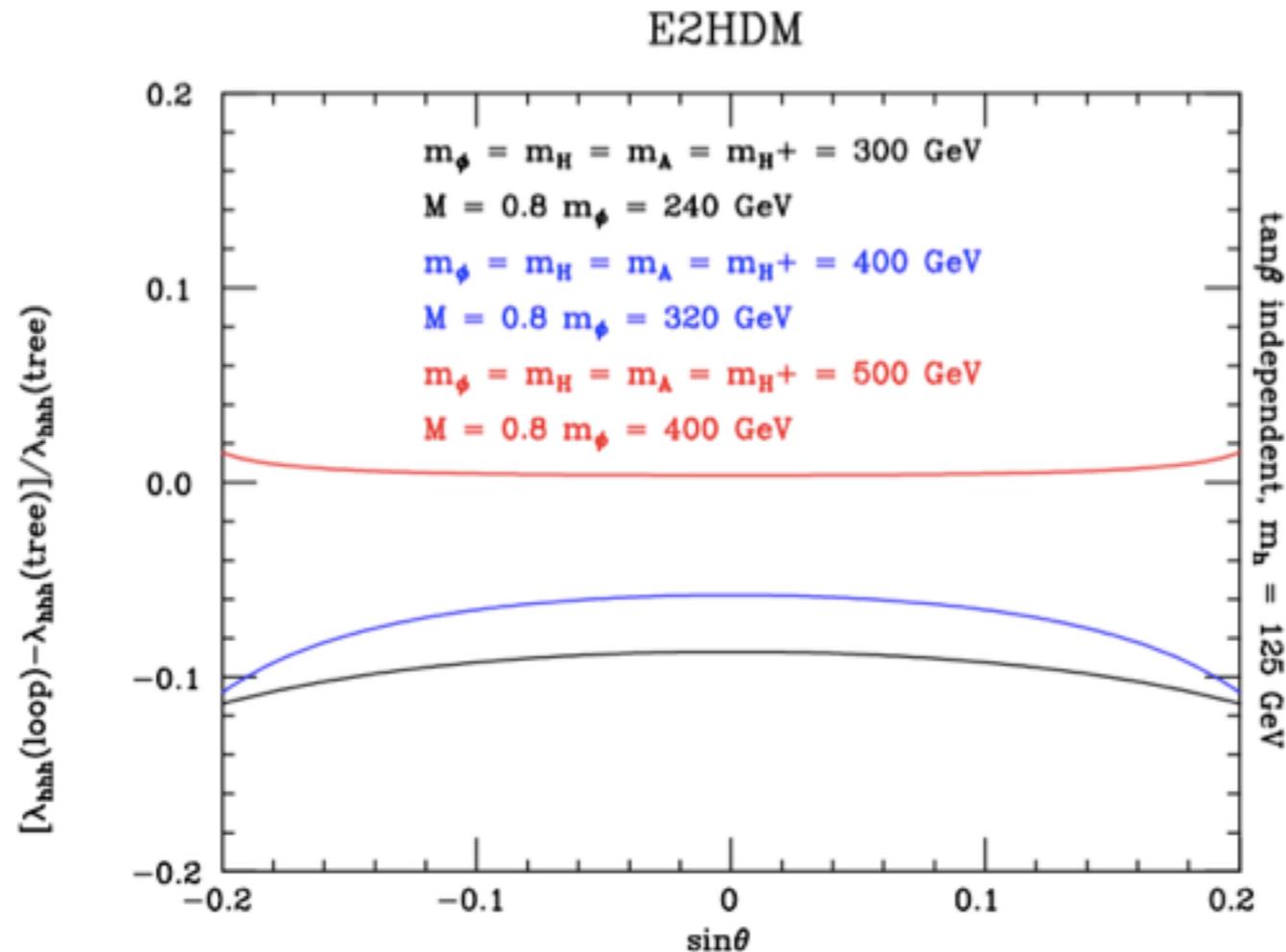
$\xi=0, 0.04, 0.08$



# $\lambda_{hhh}$ one-loop

S.Kanemura et al. 0408364

- ✓ The quantum effect of **additional particles** in loop diagrams for  $\lambda_{hhh}$  can be enhanced when they show the **non-decoupling property** and can become as large as **plus 100%** for  $M \ll m_\phi$
- ✓ Under control in the decoupling limit  $M \approx m_\phi = m_H = m_{H^+} = m_A$



Deviations  $\sim 10\%$  for  $M=0.8 m_\phi$  and  $m_\phi=300\text{GeV}$ . Lower for larger masses

We will set  $M=0.8 m_\phi$  in our analysis

# C2HDM coupling deviations

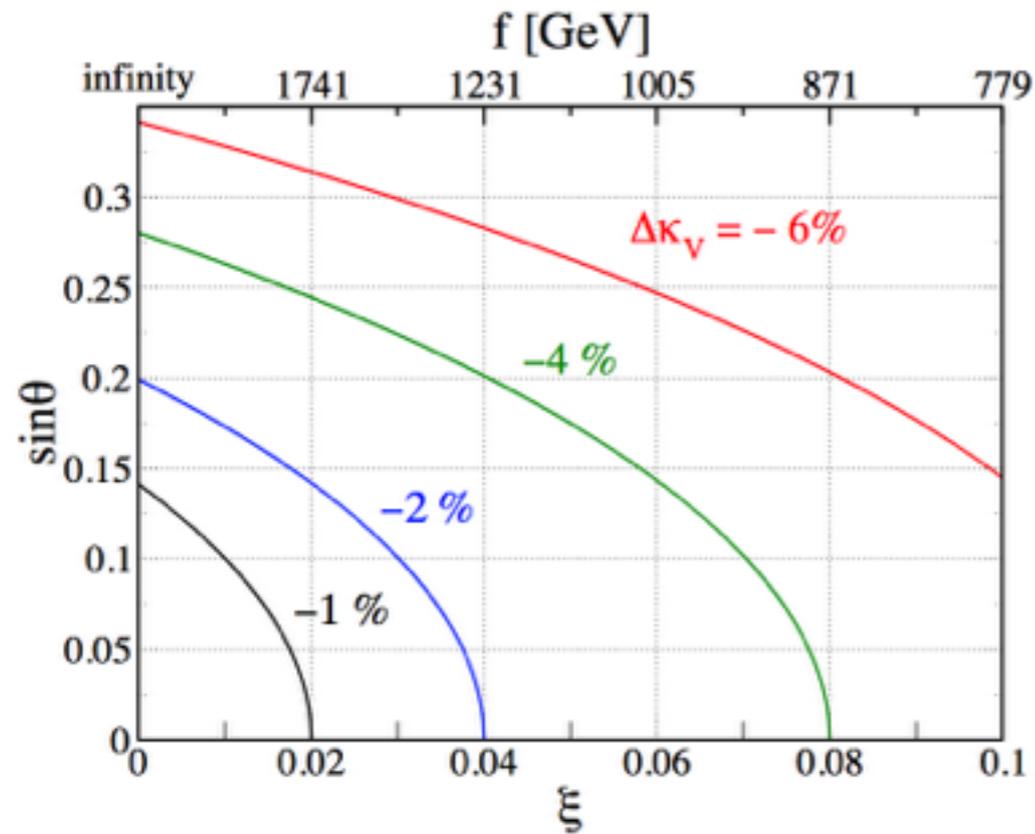
Even without introducing fermions, the pattern of deviations from the SM-like properties can be different between C2HDMs and E2HDMs

Introduce a scaling factor  $\kappa_X$  for the  $hXX$  couplings as  $\kappa_X = g_{hXX}^{\text{NP}} / g_{hXX}^{\text{SM}}$

- ☑ In the C2HDM, at the first order in  $\xi$  we get  $\kappa_V = (1 - \xi/2)c_\theta$  ( $V=W,Z$ )
- ☑ E2HDM is obtained with  $\xi=v^2/f^2 \rightarrow 0$  or  $f \rightarrow \infty$ , while SM has  $\kappa_X = 1$
- ☑ Two sources giving  $\kappa_X \neq 1$  in C2HDM: non zero value of  $\xi$  and/or  $\theta$
- ☑ Conversely, only  $\theta \neq 0$  gives  $\kappa_X \neq 1$  in E2HDM

Therefore, for a given value of  $\kappa_X$ , the value of  $\theta$  is determined in E2HDM while only the combination  $(\theta, \xi)$  is determined in C2HDM

# C2HDM coupling deviations



Contours for the deviations in the

$hVV$  coupling  $\Delta\kappa_V = \kappa_V - 1$

$$\kappa_V = g_{hVV} / g_{hVV}^{\text{SM}} = (1 - \xi/2) c_\theta$$

Ex.  $\Delta\kappa_V = -2\%$  corresponds to  $\sin\theta=0.2$  in the E2HDM but can be reproduced by  $(\sin\theta, \xi)=(0.2, 0.04)$  in the C2HDM

Even in the case of no-mixing between  $h$  and  $H$ , a non-zero deviation in  $hVV$  coupling is present in the C2HDM

Vertex	Coefficient
$H^\pm \overleftrightarrow{\partial}_\mu A W^\mp \mu$	$\frac{g}{2}$
$H^\pm \partial_\mu h W^\mp \mu$	$\mp i \frac{g}{2} (1 - \frac{5}{6} \xi) \sin \theta$
$h \partial_\mu H^\pm W^\mp \mu$	$\pm i \frac{g}{2} (1 - \frac{1}{6} \xi) \sin \theta$
$H^\pm \partial_\mu H W^\mp \mu$	$\mp i \frac{g}{2} (1 - \frac{5}{6} \xi) \cos \theta$
$H \partial_\mu H^\pm W^\mp \mu$	$\pm i \frac{g}{2} (1 - \frac{1}{6} \xi) \cos \theta$
$A \partial_\mu h Z^\mu$	$-\frac{g_Z}{2} (1 - \frac{5}{6} \xi) \sin \theta$
$h \partial_\mu A Z^\mu$	$\frac{g_Z}{2} (1 - \frac{1}{6} \xi) \sin \theta$
$A \partial_\mu H Z^\mu$	$-\frac{g_Z}{2} (1 - \frac{5}{6} \xi) \cos \theta$
$H \partial_\mu A Z^\mu$	$\frac{g_Z}{2} (1 - \frac{1}{6} \xi) \cos \theta$
$H^+ \overleftrightarrow{\partial}_\mu H^- Z^\mu$	$-i \frac{g_Z}{2} c_{2W}$
$H^+ \overleftrightarrow{\partial}_\mu H^- A^\mu$	$-ie$

Coefficients of the scalar-scalar-gauge type vertices

# Perturbative Unitarity in C2HDM

DC, Moretti, Yagyu, Yildirim 1602.06437

- ☑ The s-wave amplitudes  $A(V_L V_L \rightarrow V_L V_L)$  grow with energy due to the modified hVV coupling and lead to perturbative unitarity violation

$$a_0(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) = \frac{s}{32\pi v_{\text{SM}}^2} \xi - \frac{1}{8\pi v_{\text{SM}}^2} (m_h^2 c_\theta^2 + m_H^2 s_\theta^2) (1 - \xi) + \mathcal{O}(g^2, s^{-1}).$$

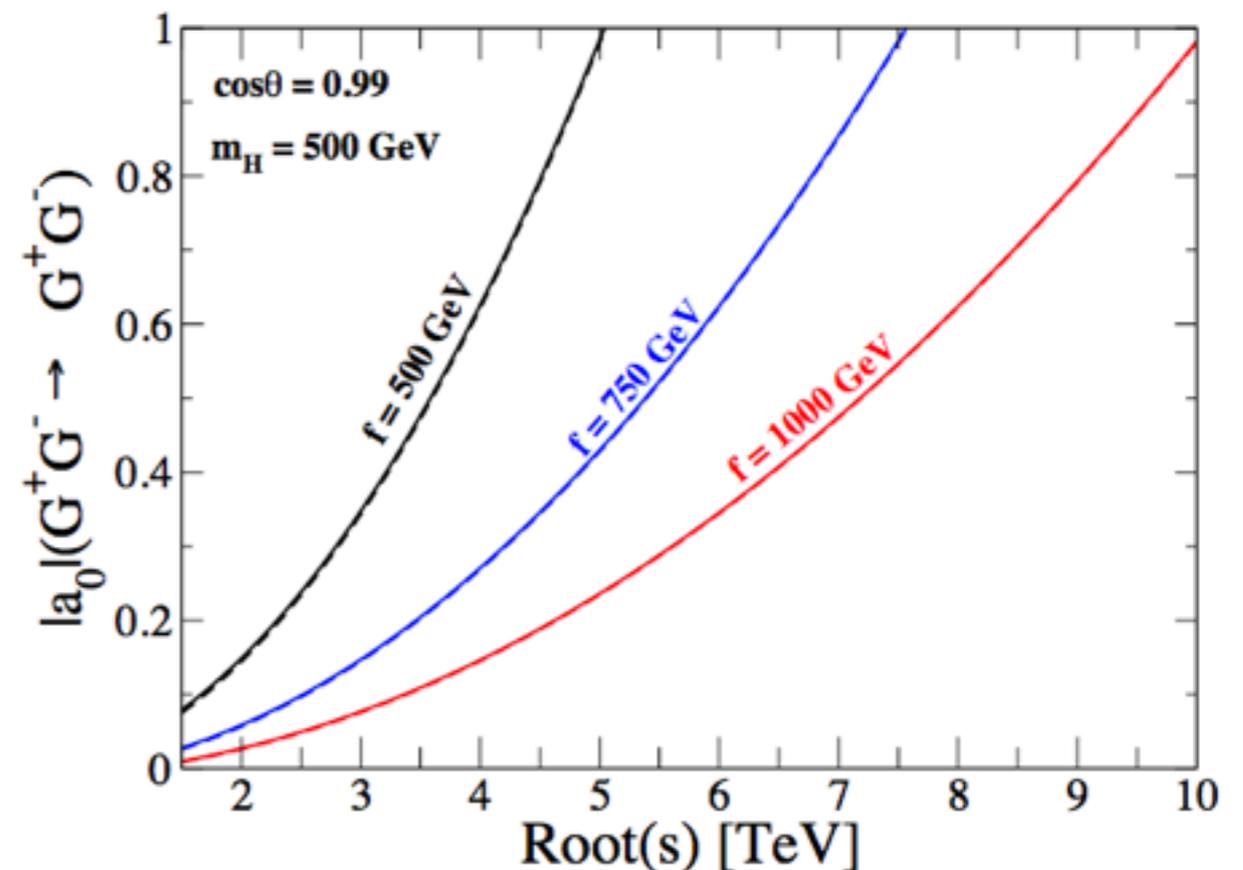
- ☑ The study of unitarity bounds gives an indication of the scale at which effects of the strong sector become relevant

- ☑ Use of the Equivalence Theorem

$|a_0| < 1/2$  gives a unitarity cut-off on energy

Ex:  $f = 1 \text{ TeV}$  ( $\xi = 0.06$ )

$\Lambda \sim 7 \text{ TeV}$



# Perturbative Unitarity in C2HDM

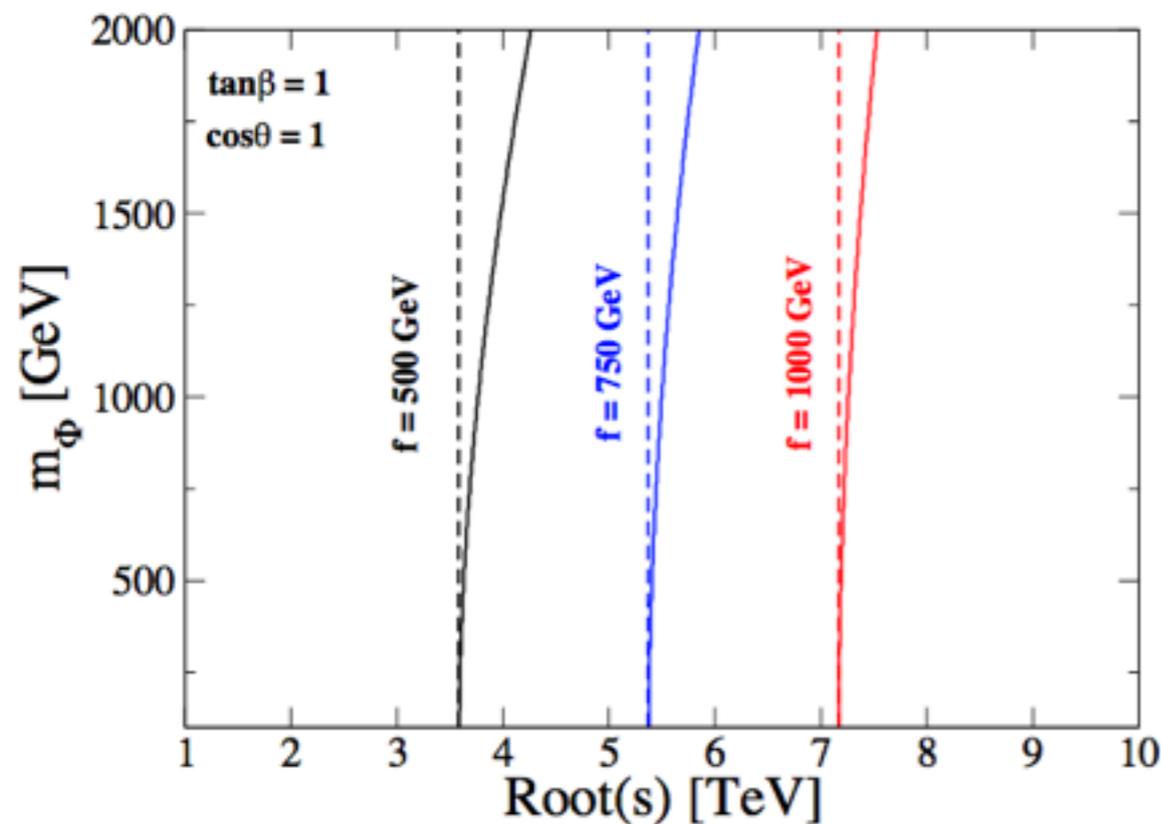
$\phi$  scattering angle

$$\mathcal{M}(H^+H^- \rightarrow H^+H^-) = \frac{s}{2v_{\text{SM}}^2} \xi(1 + c_\phi) - \frac{m_{H^\pm}^2}{v_{\text{SM}}^2} \xi \left( \frac{2}{3} + 4c_\phi \right) + \lambda_{H^+H^-H^+H^-} + \mathcal{O}(s^{-1})$$

from kinetic term  
due to NGB nature

from kinetic term and potential

from potential



Unitarity bound from the requirement

$$|a_0(H^+H^- \rightarrow H^+H^-)| < 1/2$$

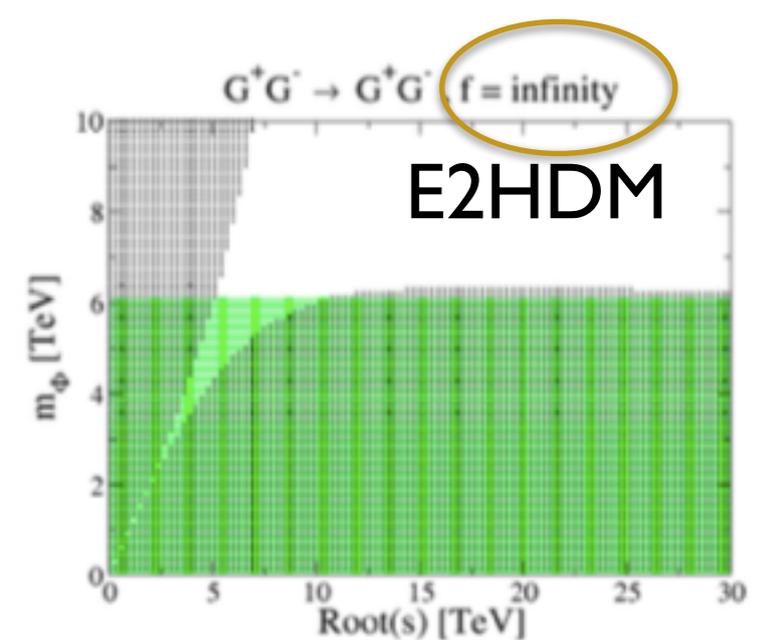
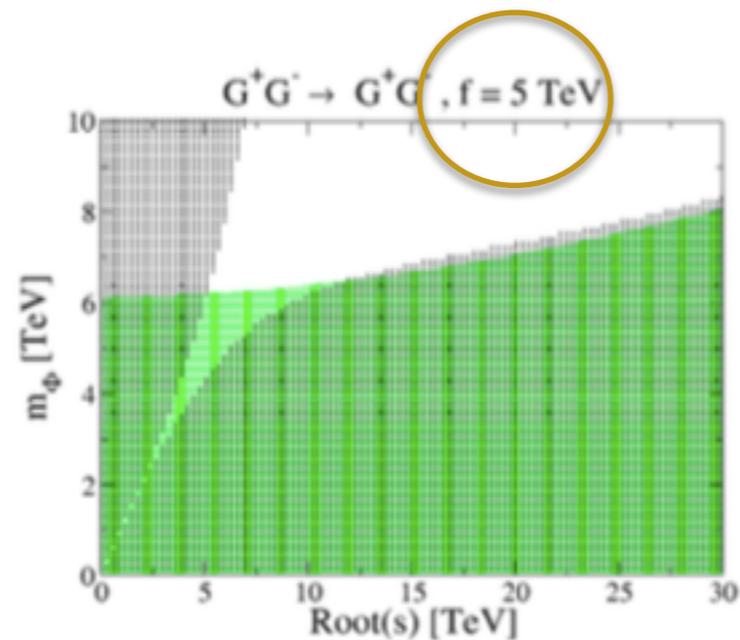
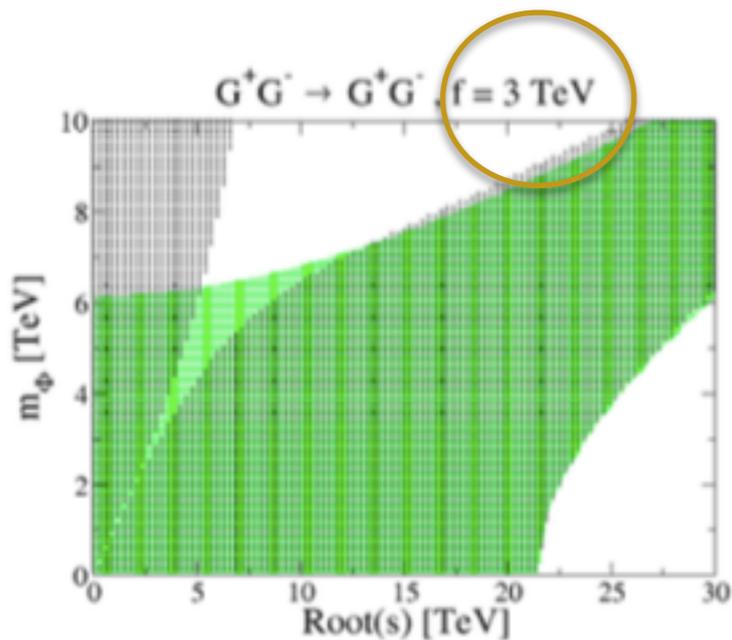
for  $M=m_A=m_H=m_{H^\pm}=m_\phi$

dashed lines neglecting  $\mathcal{O}(s^0\xi)$  terms

$\mathcal{O}(s^0\xi)$  contributions are not so important as long as we consider  $m_\phi \lesssim 1 \text{ TeV}$

Neglecting  $\mathcal{O}(s^0\xi)$  makes the calculation of all the  $2 \rightarrow 2$  body scattering amplitudes simpler and it is safe in the parameter region relevant for the phenomenology at the LHC

# Perturbative Unitarity in C2HDM from $G^+G^- \rightarrow G^+G^-$



grey regions: exact formulae

green regions: neglecting  $O(1/s)$  terms

$m_H = m_A = m_{H^\pm} = M = m_\Phi$   
 $\cos\Theta = 0.99$ ,  $\tan\beta = 1$

- The results are in good agreement for  $\sqrt{s} > m_\Phi$
- The region  $\sqrt{s} \approx m_\Phi$  is excluded due to the resonant effects

Compare C2HDM (left, center) with E2HDM (right):

- Energy cut-off  $\sim 20 \text{ TeV}$  for  $f = 3 \text{ TeV}$  in C2HDM
- Below the cut-off the bound on the mass is less stringent in the C2HDM due to a partial cancellation between the  $s$  term and the  $m_H^2$  one

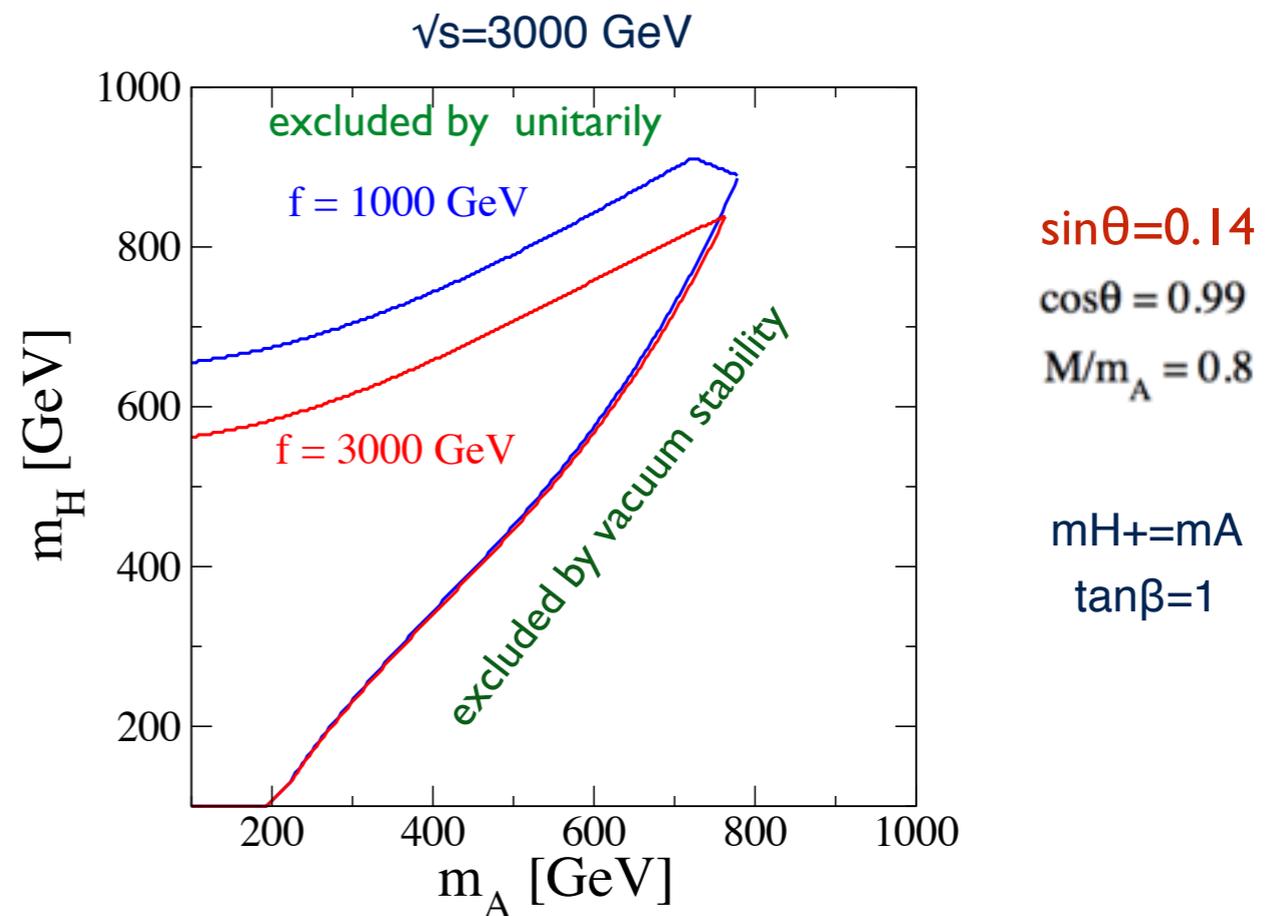
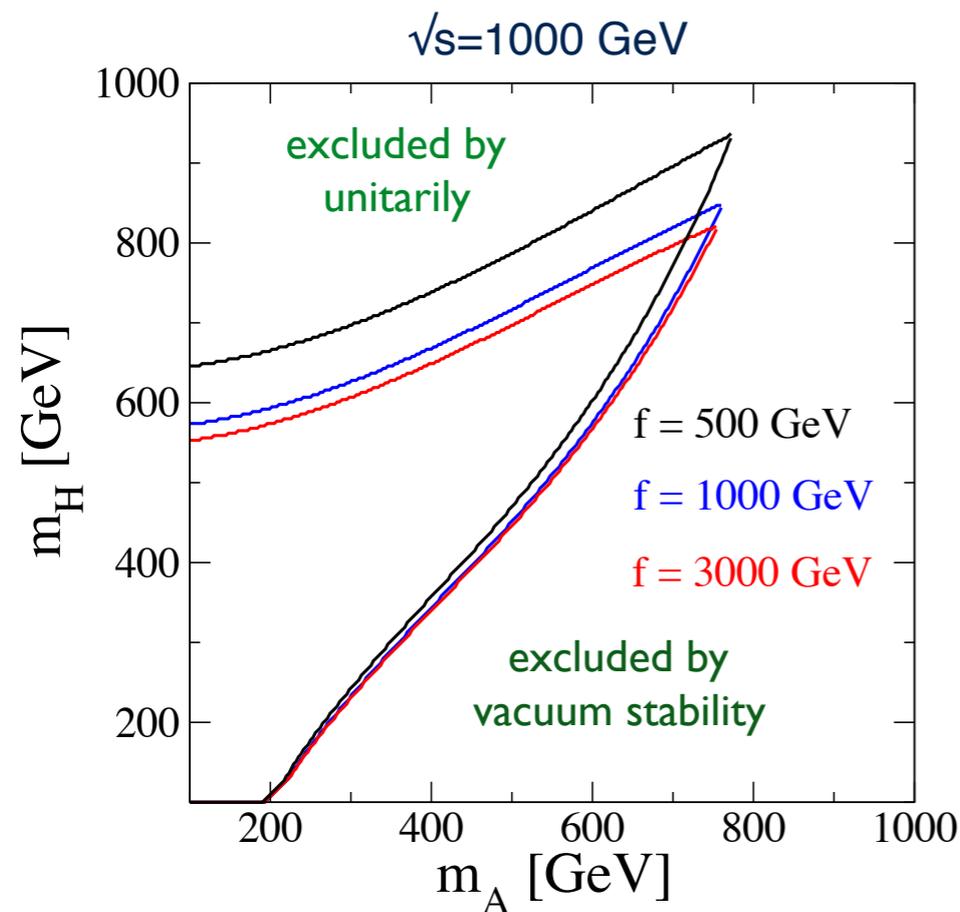
# Perturbative Unitarity in C2HDM

DC, Moretti, Yagyu, Yildirim 1602.06437

☑ We calculate all the  $2 \rightarrow 2$  body elastic (pseudo)scalar scattering amplitudes in the C2HDM  
There are 14 neutral, 8 singly charged and 3 double charged states

☑ We also impose the **vacuum stability condition** (scalar potential bounded from below in any direction)

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \sqrt{\lambda_1 \lambda_2} + \lambda_3 + \text{MIN}(0, \lambda_4 \pm \lambda_5) > 0$$



E2HDM corresponds to  $f \rightarrow \infty$   
(indistinguishable from  $f=3000 \text{ GeV}$ )

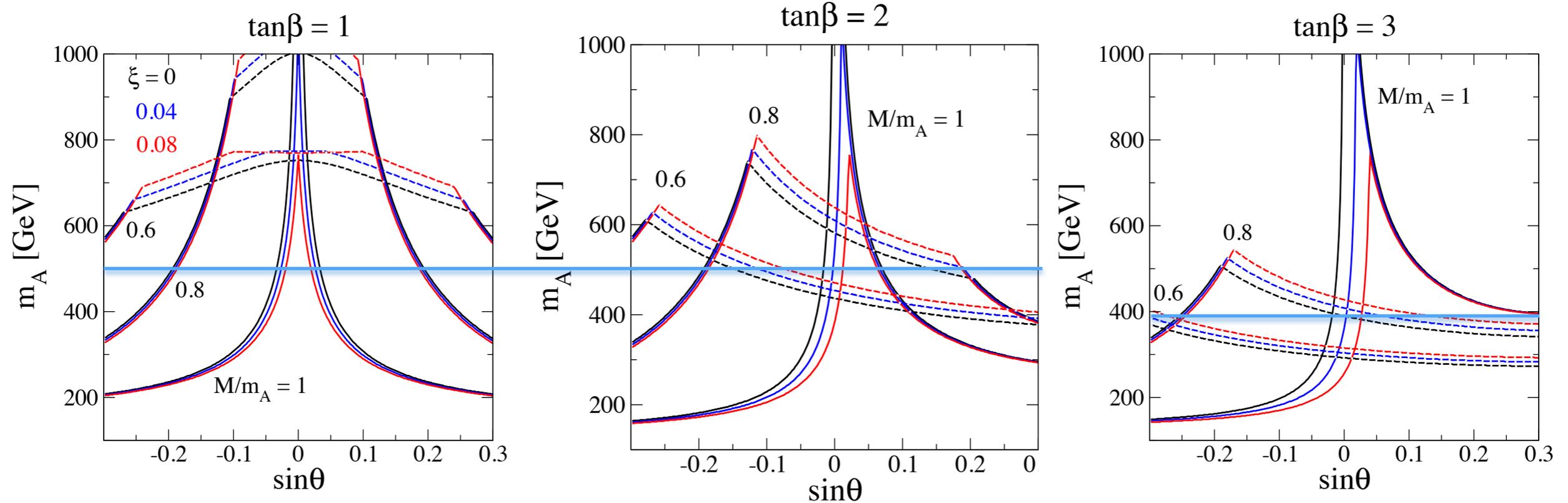
More parameter space becomes available  
to the C2HDM with respect to the  
E2HDM for smaller  $f$  values

# Perturbative Unitarity and Vacuum Stability in C2HDM

outside the alignment limit  $\sin\theta \rightarrow 0$

$$m_{H^\pm} = m_A = m_H$$

$$M/m_A = 1, 0.8, 0.6$$



below solid (dashed) lines : allowed by vacuum stability (unitarity )

C2HDM bounds are for  $\sqrt{s}=1000$  GeV and  $f = 1250(850)$  GeV corresponding to  $\xi=0.04(0.08)$   
 E2HDM corresponds to  $f \rightarrow \infty (\xi=0)$

for  $m_\phi=500$  GeV,  $M=0.8m_A$ ,  $\tan\beta=1,2$   
 $-0.2 < \sin\theta < 0.2$  is allowed

larger  $\tan\beta$   
 values require  
 lower  $m_\phi$

# Effective Yukawa Lagrangian for C2HDM

DC, Moretti, Yagyu, Yildirim 1610.02087

- ✓ The kinetic term of the pNGB is uniquely determined by the structure of the global symmetry breaking  $SO(6)/SO(4) \times SO(2)$
- ✓ For the Yukawa sector we need to assume the embedding for SM fermions into  $SO(6)$  multiplets. It is justified by the partial compositeness assumption where the SM fermions mix with the composite ones in a  $SU(2) \times U(1)$  invariant form. The low-energy Lagrangian is obtained after integrating out the composite fermions
- ✓ We use here the 6-plet reprs of  $SO(6)$  for SM quarks and leptons

$$(\Psi_{2/3})_L \equiv Q_L^u = (-id_L, -d_L, -iu_L, u_L, 0, 0)^T,$$

$$(\Psi_{-1/3})_L \equiv Q_L^d = (-iu_L, u_L, id_L, d_L, 0, 0)^T,$$

$$(\Psi_{2/3})_R \equiv U_R = (0, 0, 0, 0, 0, u_R)^T,$$

$$(\Psi_{-1/3})_R \equiv D_R = (0, 0, 0, 0, 0, d_R)^T,$$

$$(\Psi_{-1})_L \equiv L_L = (-i\nu_L, \nu_L, ie_L, e_L, 0, 0)^T,$$

$$(\Psi_{-1})_R \equiv E_R = (0, 0, 0, 0, 0, e_R)^T.$$

$$Q = T_3^L + T_3^R + X.$$

- ✓ In order to reproduce the correct electric charge we have added an additional  $U(1)_X$  symmetry.

# Effective Yukawa Lagrangian for C2HDM

- ✓ The Yukawa Lagrangian is given in terms of  $\Sigma$ , the 15-plet of pNGB, SO(6) adjoint, the 6-plet of fermions

$$\mathcal{L}_Y = f \left[ \bar{Q}_L^u (a_u \Sigma - b_u \Sigma^2) U_R + \bar{Q}_L^d (a_d \Sigma - b_d \Sigma^2) D_R + \bar{L}_L (a_e \Sigma - b_e \Sigma^2) E_R \right] + \text{h.c.}$$

$$\Sigma = U \Sigma_0 U^T \quad \Sigma_0 = \begin{pmatrix} 0_{4 \times 4} & 0_{4 \times 2} \\ 0_{2 \times 4} & i\sigma_2 \end{pmatrix}$$

U=pNGB matrix

transforms linearly under SO(6)  
 $\Sigma \rightarrow g \Sigma g^T$

$a_f$  and  $b_f$  are 3x3 complex matrices in the flavor space

- ✓ **Masses of fermions** (at the first order in  $\xi$ )  $\rightarrow m_f = v_{\text{SM}} \left[ a_f c_\beta + b_f s_\beta \left( 1 - \frac{\xi}{2} \right) \right]$

- ✓ In general FCNCs appear at tree level due to the existence of two independent Yukawa couplings  $a_f$  and  $b_f$  (both doublets couple to each fermion type).

To avoid it, impose a  $C_2$  discrete symmetry (J.Mrazek et al. 1105.5403)

$$U(\pi_1^{\hat{a}}, \pi_2^{\hat{a}}) \rightarrow C_2 U(\pi_1^{\hat{a}}, \pi_2^{\hat{a}}) C_2 = U(\pi_1^{\hat{a}}, -\pi_2^{\hat{a}})$$

$$C_2 = \text{diag}(1, 1, 1, 1, 1, -1)$$

$$\begin{matrix} \pi_1^{\hat{a}} & C_2\text{-even} \\ \pi_2^{\hat{a}} & C_2\text{-odd} \end{matrix} \quad (\pi_1^{\hat{a}}, \pi_2^{\hat{a}}) \rightarrow (\pi_1^{\hat{a}}, -\pi_2^{\hat{a}})$$

- ✓ Depending on the  $C_2$  charge of the right-handed fermions, we define 4-independent Types of Yukawa interactions, like the  $Z_2$  symm. in E2HDM

# Effective Yukawa Lagrangian for C2HDM

$$\mathcal{L}_Y = \sum_{f=u,d,e} \frac{m_f}{v_{\text{SM}}} \bar{f} \left( \bar{X}_f^h h + \bar{X}_f^H H - 2iI_f \bar{X}_f^A \gamma_5 A \right) f \quad \bar{X}_f^\phi \text{ are diagonal in the mass eigenbasis of fermions}$$

$$+ \frac{\sqrt{2}}{v_{\text{SM}}} \bar{u} V_{ud} (m_d \bar{X}_d^A P_R - m_u \bar{X}_u^A P_L) d H^+ + \frac{\sqrt{2}}{v_{\text{SM}}} \bar{\nu} m_e \bar{X}_e P_R e H^+ + \text{h.c.}$$

	$U_R$	$D_R$	$E_R$	$(a_u, b_u)$	$(a_d, b_d)$	$(a_e, b_e)$	$\bar{X}_u^h$	$\bar{X}_d^h$	$\bar{X}_e^h$	$\bar{X}_u^H$	$\bar{X}_d^H$	$\bar{X}_e^H$	$\bar{X}_u^A$	$\bar{X}_d^A$	$\bar{X}_e^A$
Type-I	-	-	-	$(0, \sqrt{1})$	$(0, \sqrt{1})$	$(0, \sqrt{1})$	$\zeta_h$	$\zeta_h$	$\zeta_h$	$\zeta_H$	$\zeta_H$	$\zeta_H$	$\zeta_A$	$\zeta_A$	$\zeta_A$
Type-II	-	+	+	$(0, \sqrt{1})$	$(\sqrt{1}, 0)$	$(\sqrt{1}, 0)$	$\zeta_h$	$\xi_h$	$\xi_h$	$\zeta_H$	$\xi_H$	$\xi_H$	$\zeta_A$	$\xi_A$	$\xi_A$
Type-X	-	-	+	$(0, \sqrt{1})$	$(0, \sqrt{1})$	$(\sqrt{1}, 0)$	$\zeta_h$	$\zeta_h$	$\xi_h$	$\zeta_H$	$\zeta_H$	$\xi_H$	$\zeta_A$	$\zeta_A$	$\xi_A$
Type-Y	-	+	-	$(0, \sqrt{1})$	$(\sqrt{1}, 0)$	$(0, \sqrt{1})$	$\zeta_h$	$\xi_h$	$\zeta_h$	$\zeta_H$	$\xi_H$	$\zeta_H$	$\zeta_A$	$\xi_A$	$\zeta_A$

$$\zeta_h = \left(1 - \frac{3}{2}\xi\right) c_\theta + s_\theta \cot \beta, \quad \xi_h = \left(1 - \frac{\xi}{2}\right) c_\theta - s_\theta \tan \beta,$$

$$\zeta_H = -\left(1 - \frac{3}{2}\xi\right) s_\theta + c_\theta \cot \beta, \quad \xi_H = -\left(1 - \frac{\xi}{2}\right) s_\theta - c_\theta \tan \beta,$$

$$\zeta_A = \left(1 + \frac{\xi}{2}\right) \cot \beta, \quad \xi_A = -\left(1 - \frac{\xi}{2}\right) \tan \beta.$$

Ex. in all Types:

$$\kappa_t = g_{htt} / g_{htt}^{\text{SM}} = \bar{X}_u^h = \zeta_h$$

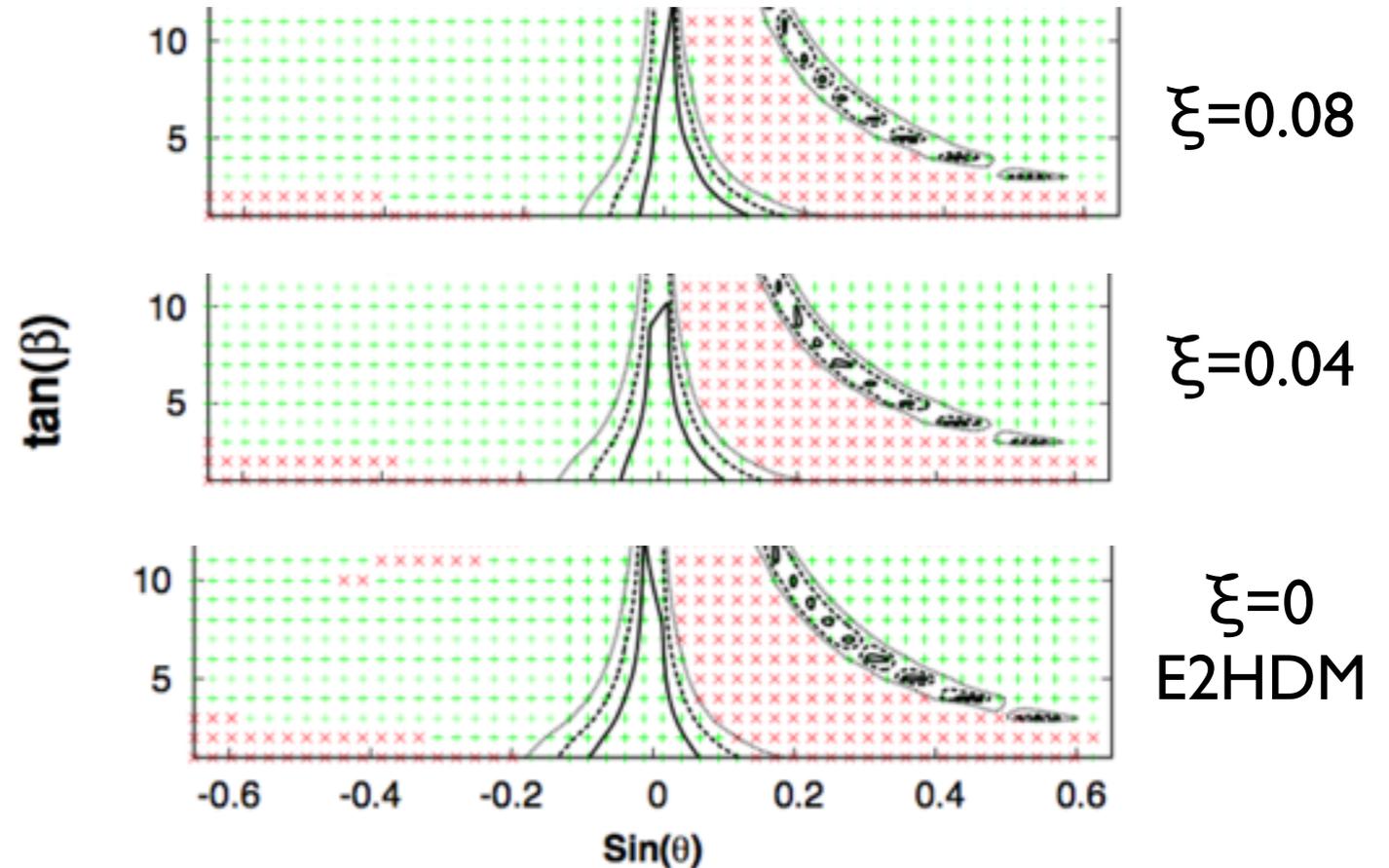
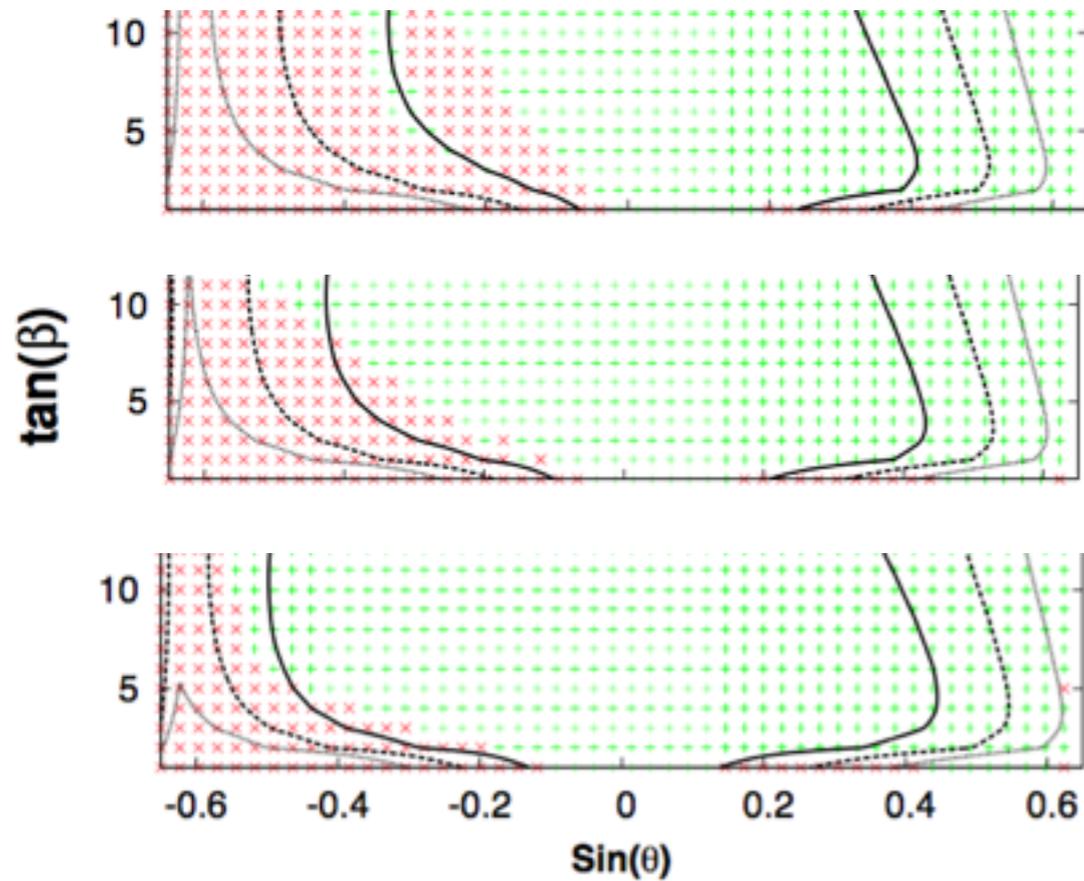
corrections  $\mathcal{O}(\xi)$  are predominately negative

# Present collider bounds for the C2HDM Type-I and Type-II

$$m_A = m_{H^\pm} = m_H = M = 500 \text{ GeV} \quad m_h = 125 \text{ GeV}$$

C2HDM Type-I excluded/allowed regions

C2HDM Type-II excluded/allowed regions



green/red regions are 95%CL  
 allowed/excluded from  
 LEP, Tevatron, LHC data by using  
 HiggsBounds package

— 68%CL  $\Delta\chi^2$ -contours by  
 - - - 95%CL HiggsSignal  
 . . . . . 99%CL package

Type-I reveals a better compliance with the LHC data  
 Type-II disfavoured for  $|\sin\theta| > 0.2$  and  $\tan\beta > 10$   
 Type-X and Type-Y very similar to Type-II

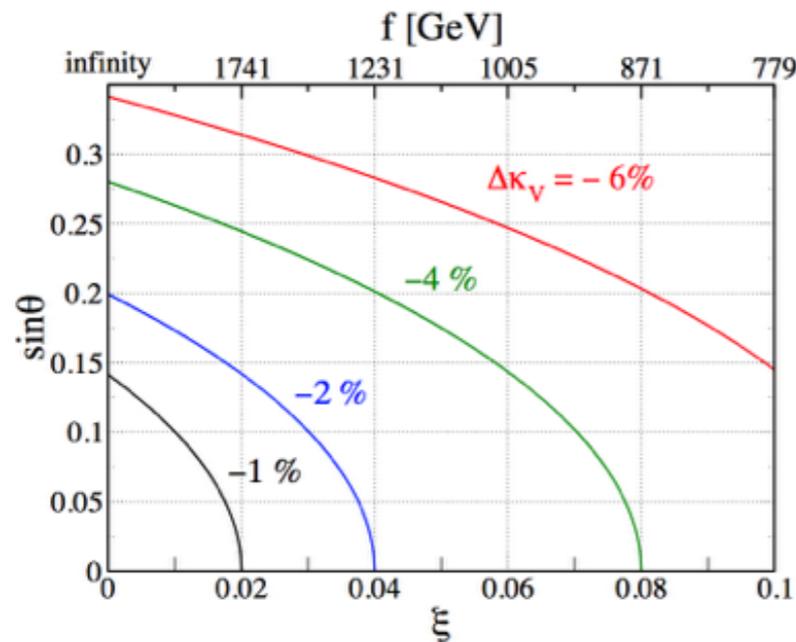
$\xi$  dependence is only marginally evident for Type-I

Choose:  $\xi \leq 0.08$   $|\sin\theta| \leq 0.2$  and small  $\tan\beta$   
 also compliant with unitarity and stability  
 bounds with  $m_\Phi = 500 \text{ GeV}$

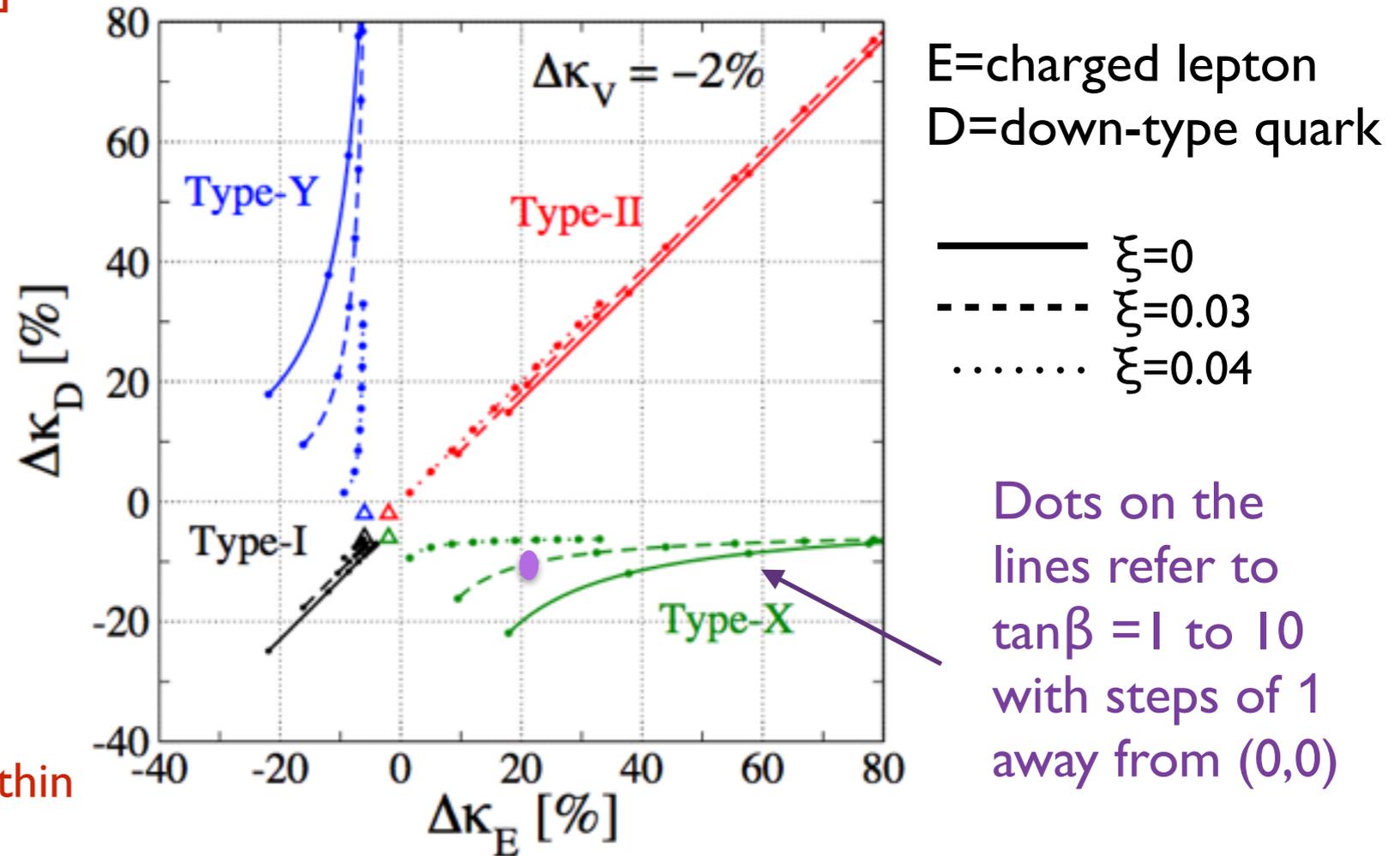
# Deviations in Higgs boson couplings

$$\Delta\kappa_X = g_{hXX} / g_{hXX}^{\text{SM}} - 1 \quad \text{DC, Moretti, Yagyu, Yildirim 1610.02087}$$

Suppose a deviation  $\Delta\kappa_V$  is measured at the LHC, it is an indirect evidence for a non-minimal Higgs sector



$|\Delta\kappa_V| > 2\%$  difficult to be explained within E2HDM because of the theor. and exp. bounds on  $\sin\Theta$ , but possible in C2HDM

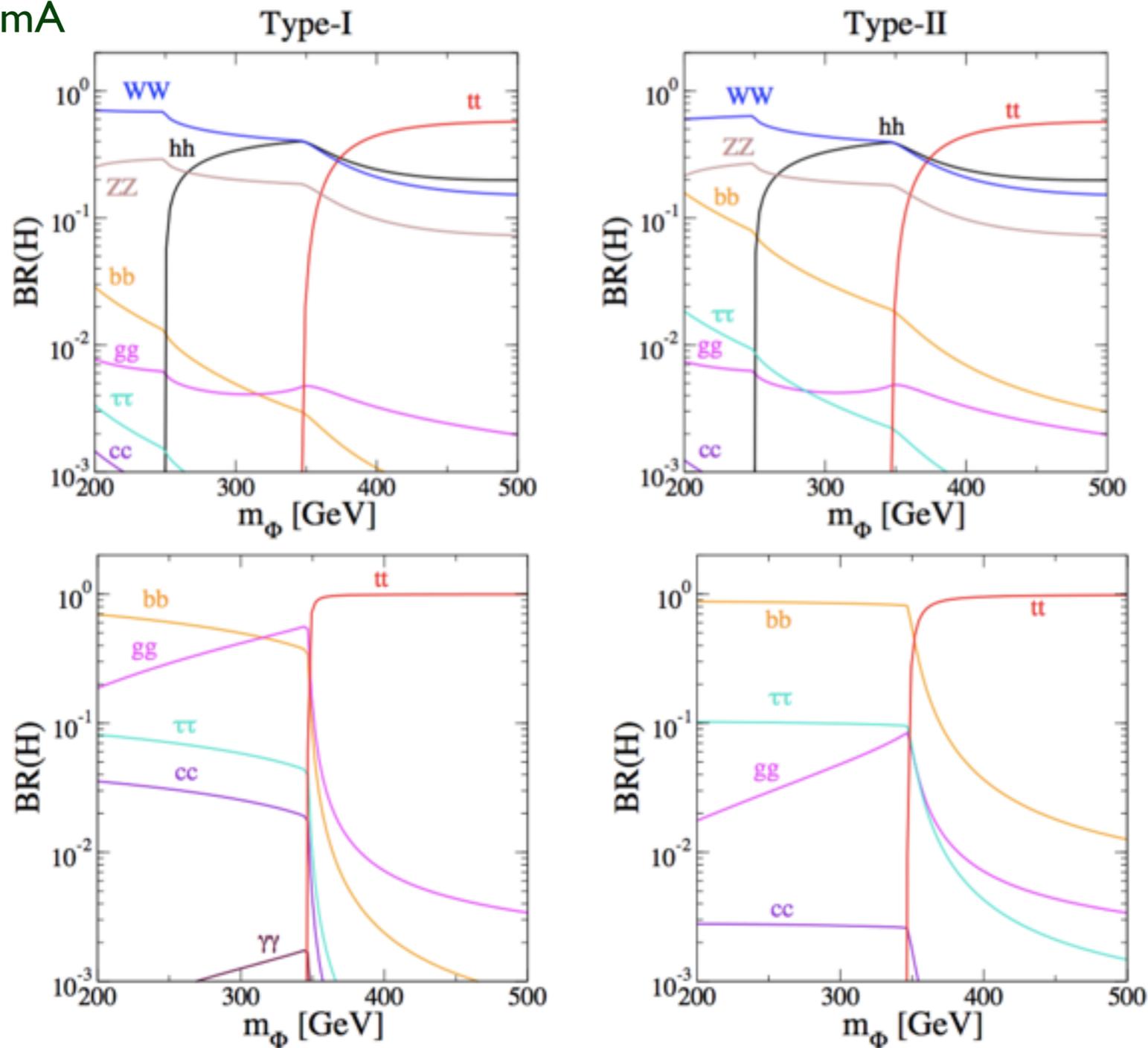


If  $|\Delta\kappa_V| \lesssim 2\%$  by looking at the pattern of the deviations in  $\Delta\kappa_E$  and  $\Delta\kappa_D$  we can discriminate between E2HDM and C2HDM and among the four Types of Yukawa interactions

Ex: if  $\Delta\kappa_V = -2\%$ ,  $\Delta\kappa_D = -10\%$ ,  $\Delta\kappa_E = 20\%$  then  $\rightarrow$  Type-X C2HDM with  $\tan\beta = 2$  and  $\xi = 0.03$

# Decays of the extra-Higgs boson H

$m_\phi = m_H = m_{H^\pm} = m_A$   
 $M = 0.8m_A$ ,  
 $\tan\beta = 2$



$$\Delta k_V = -2\%$$

E2HDM  
 $(\sin\Theta = -0.2, \xi = 0)$

C2HDM  
 $(\sin\Theta = 0, \xi = 0.04)$

Below the  $tt$  threshold,  $H \rightarrow hh, WW, ZZ$  are the dominant channels in E2CHM while they are absent in the C2HDM with  $\sin\Theta = 0$  (in all the 4 Yukawa Types)

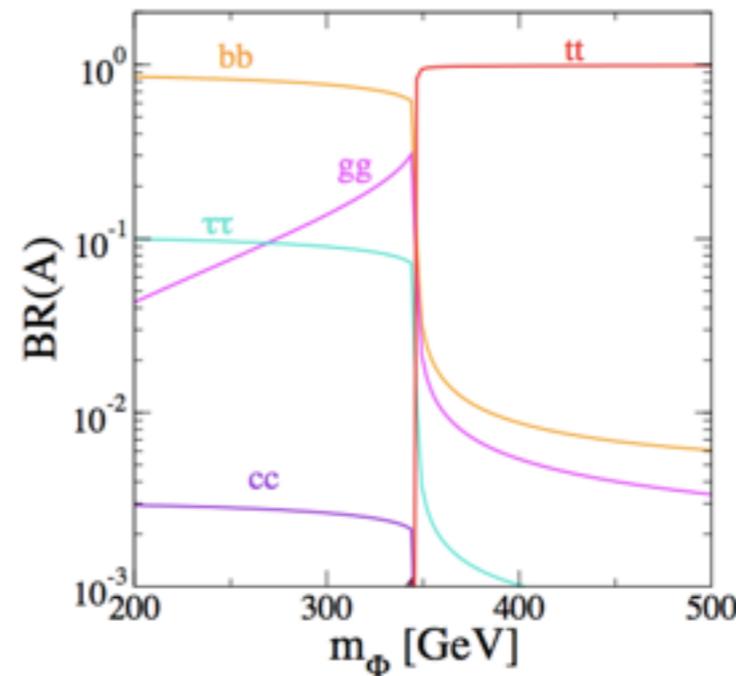
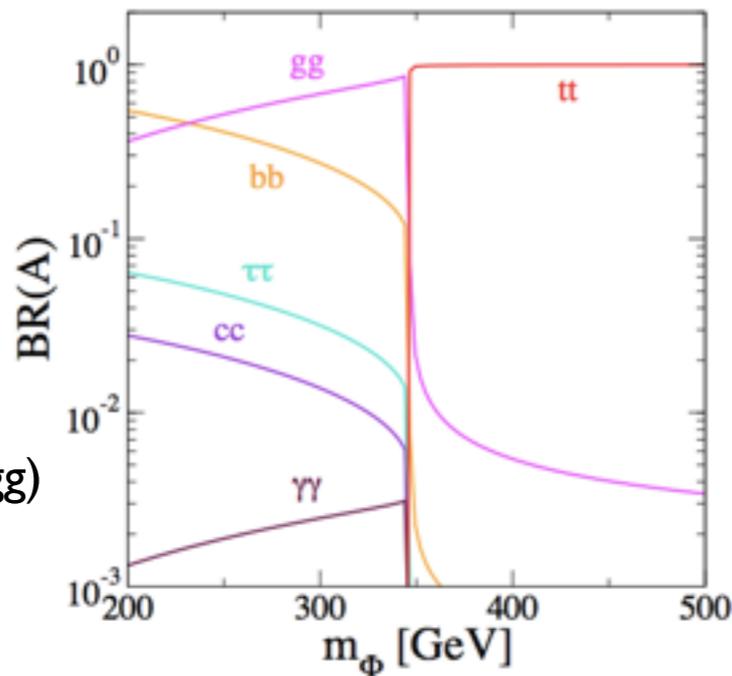
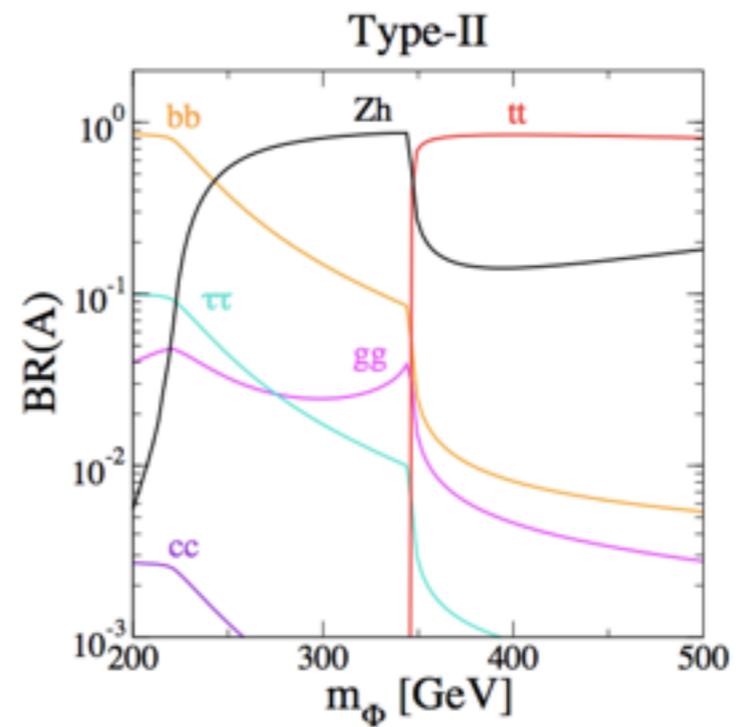
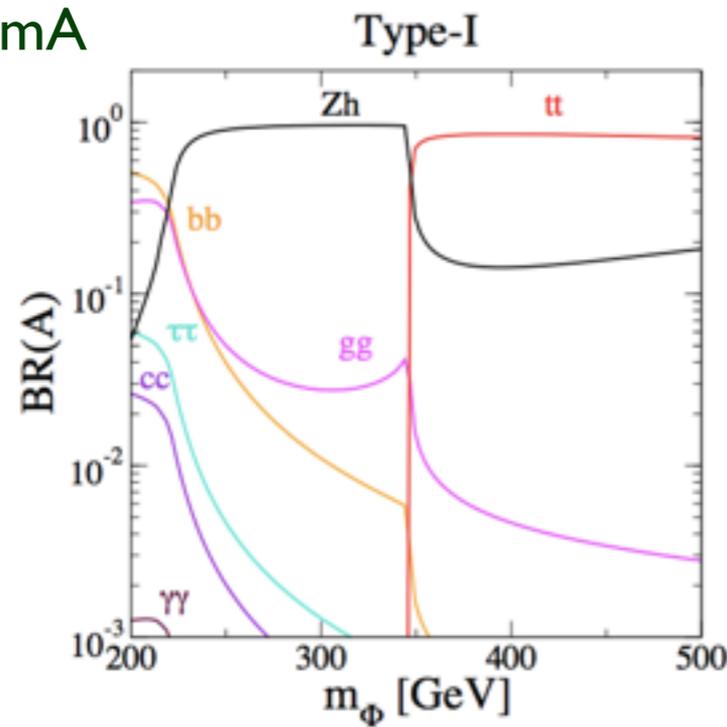
# Decays of the extra-Higgs boson A

$$m_\phi = m_H = m_{H^\pm} = m_A$$

$$M = 0.8m_A, \quad \tan\beta = 2$$

the three body decay  
 $A \rightarrow Z^*h \rightarrow f\bar{f}h$   
 is taken into account  
 for  $m_A < m_Z + m_h$

Similar to H with  
 $BR(A \rightarrow gg) > BR(H \rightarrow gg)$



$$\Delta k_V = -2\%$$

E2HDM  
 ( $\sin\Theta = -0.2, \xi = 0$ )

C2HDM  
 ( $\sin\Theta = 0, \xi = 0.04$ )

Below the  $t\bar{t}$  threshold,  $A \rightarrow Zh$  can be the dominant channels in E2HDM while it is absent in the C2HDM with  $\sin\Theta = 0$  (in all the 4 Yukawa Types)

# Productions of the extra-Higgs bosons at the LHC

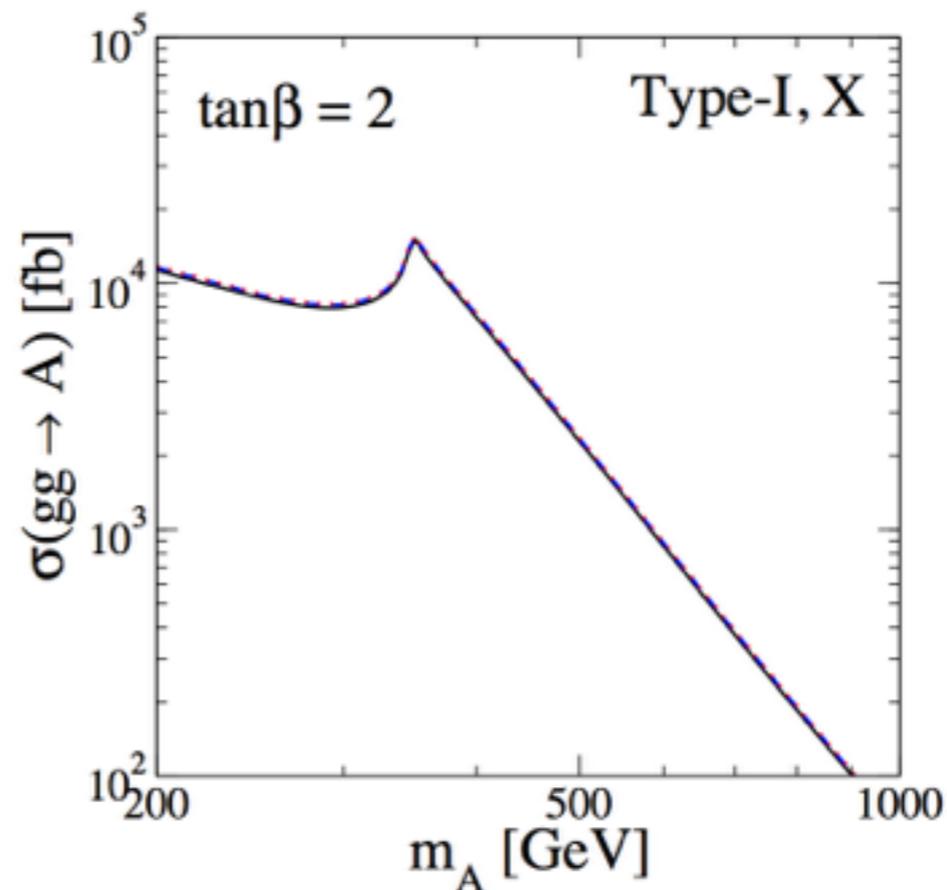
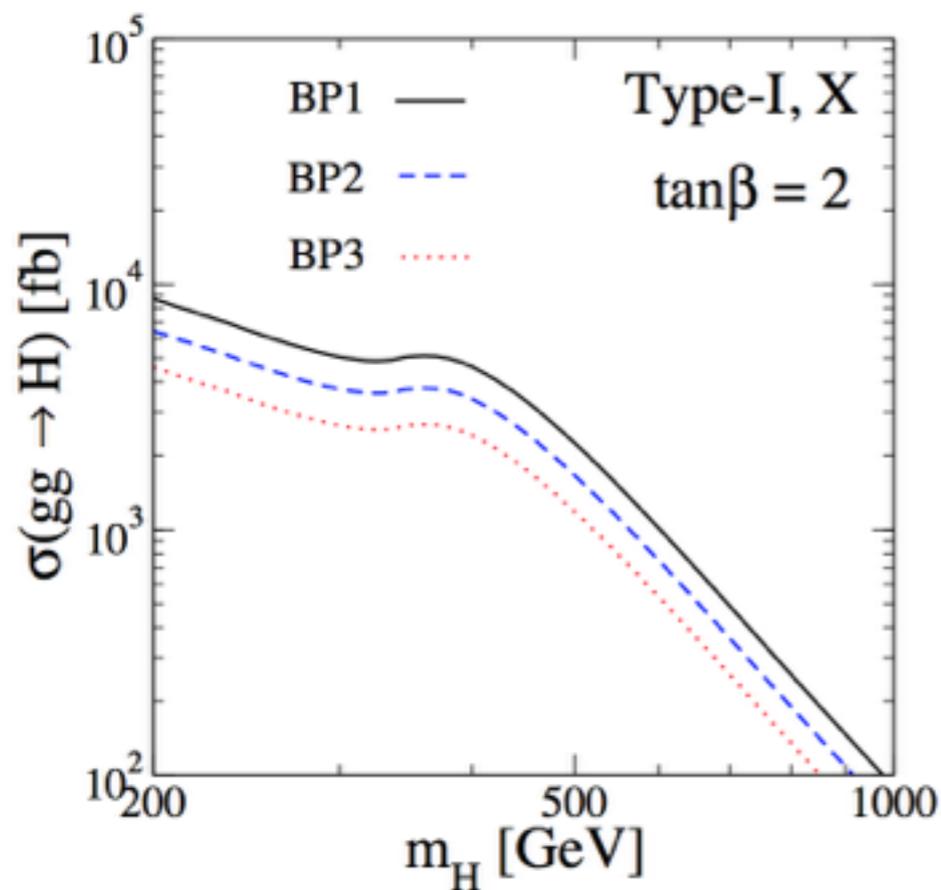
$$\sigma (gg \rightarrow H/A)$$

$$\sigma(gg \rightarrow \phi^0) = \frac{\Gamma(\phi^0 \rightarrow gg)}{\Gamma(h_{\text{SM}} \rightarrow gg)} \times \sigma(gg \rightarrow h_{\text{SM}}), \quad (\phi^0 = H \text{ or } A),$$

with the mass of  $h_{\text{SM}}$  artificially set at  $m_{\phi^0}$

E2HDM: BP1 ( $\sin\Theta = -0.2, \xi = 0$ )

C2HDM: BP2 ( $\sin\Theta = -0.1, \xi = 0.03$ ), BP3 ( $\sin\Theta = 0, \xi = 0.04$ )



Similar for Type-II, Y  
differences for large  
 $\tan\beta \sim 10$

$\sqrt{s} = 13$  TeV

Sizeable differences between E2HDM and C2HDM in gluon fusion H production

For the A production the differences are marginal

mainly due to the  $\sin\Theta$   
dependence in the top  
Yukawa couplings

$$\rightarrow \zeta_H = - \left( 1 - \frac{3}{2}\xi \right) s_\theta + c_\theta \cot \beta \quad \zeta_A = \left( 1 + \frac{\xi}{2} \right) \cot \beta,$$

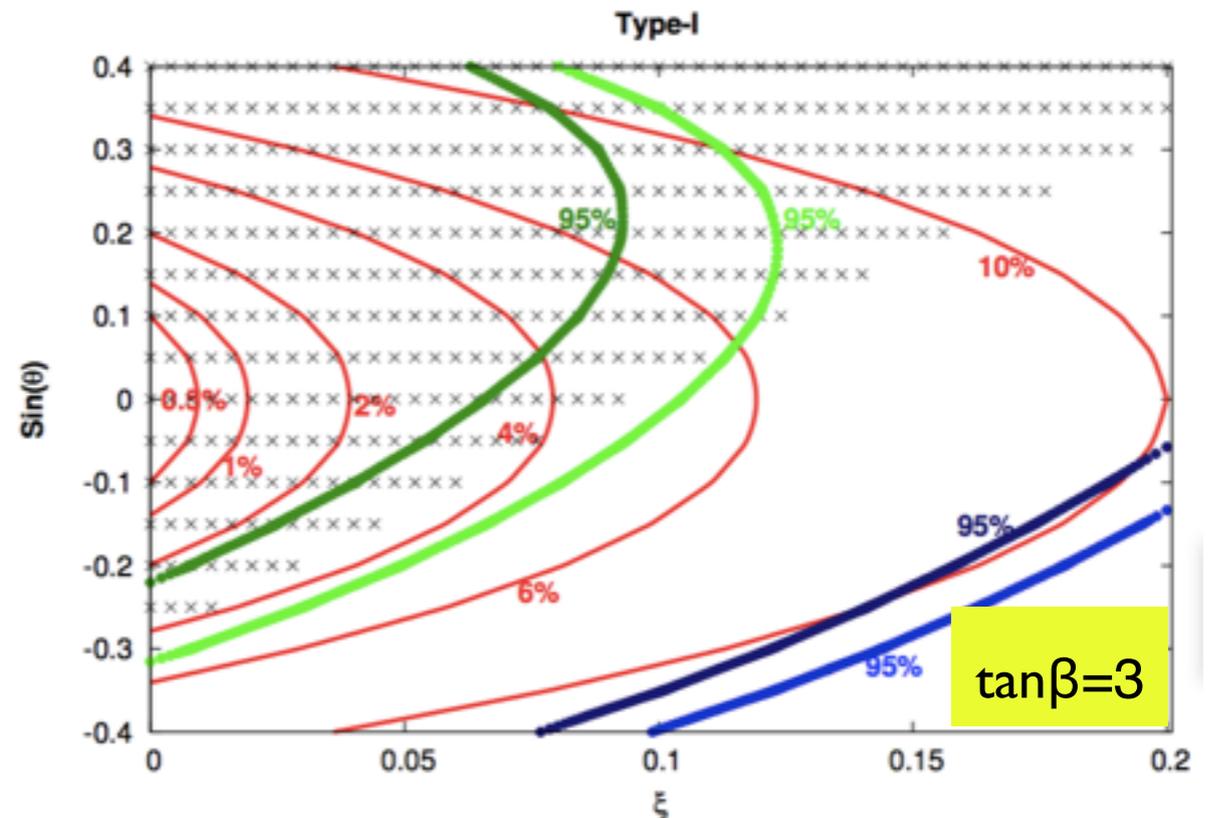
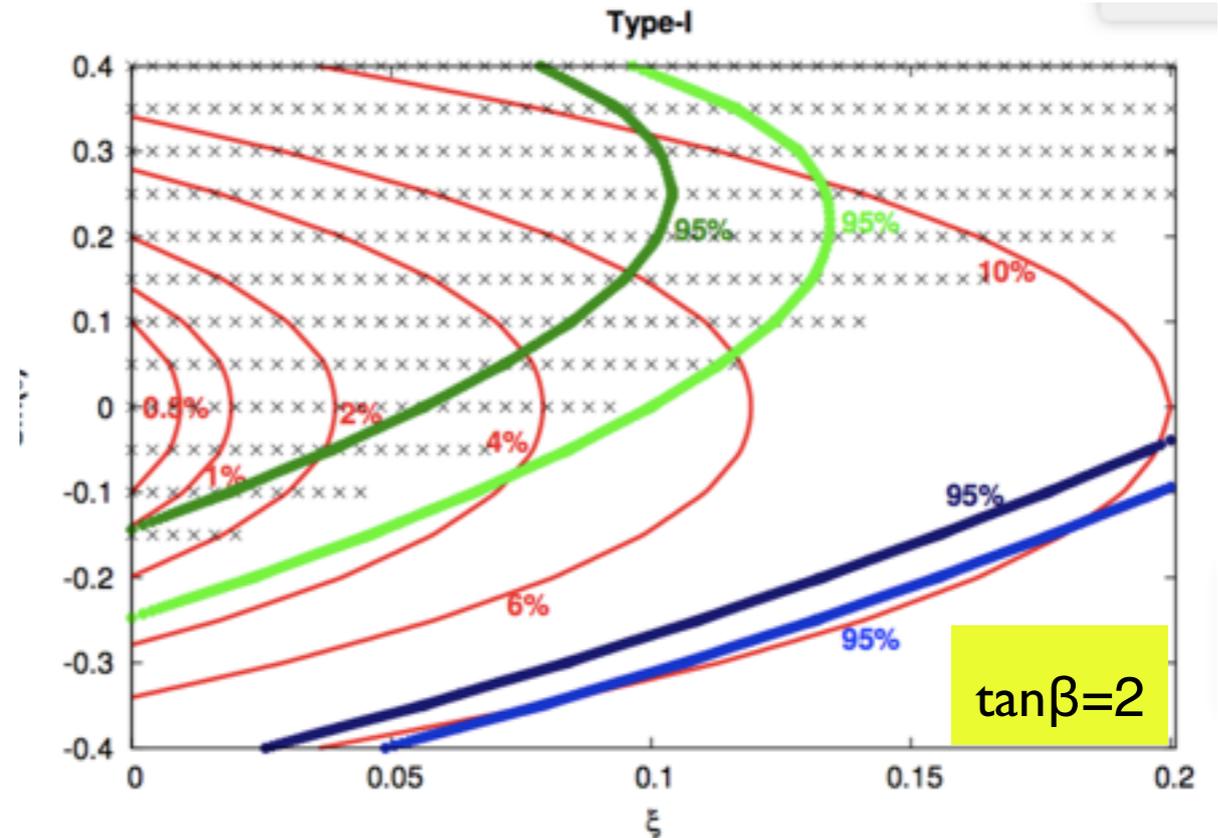
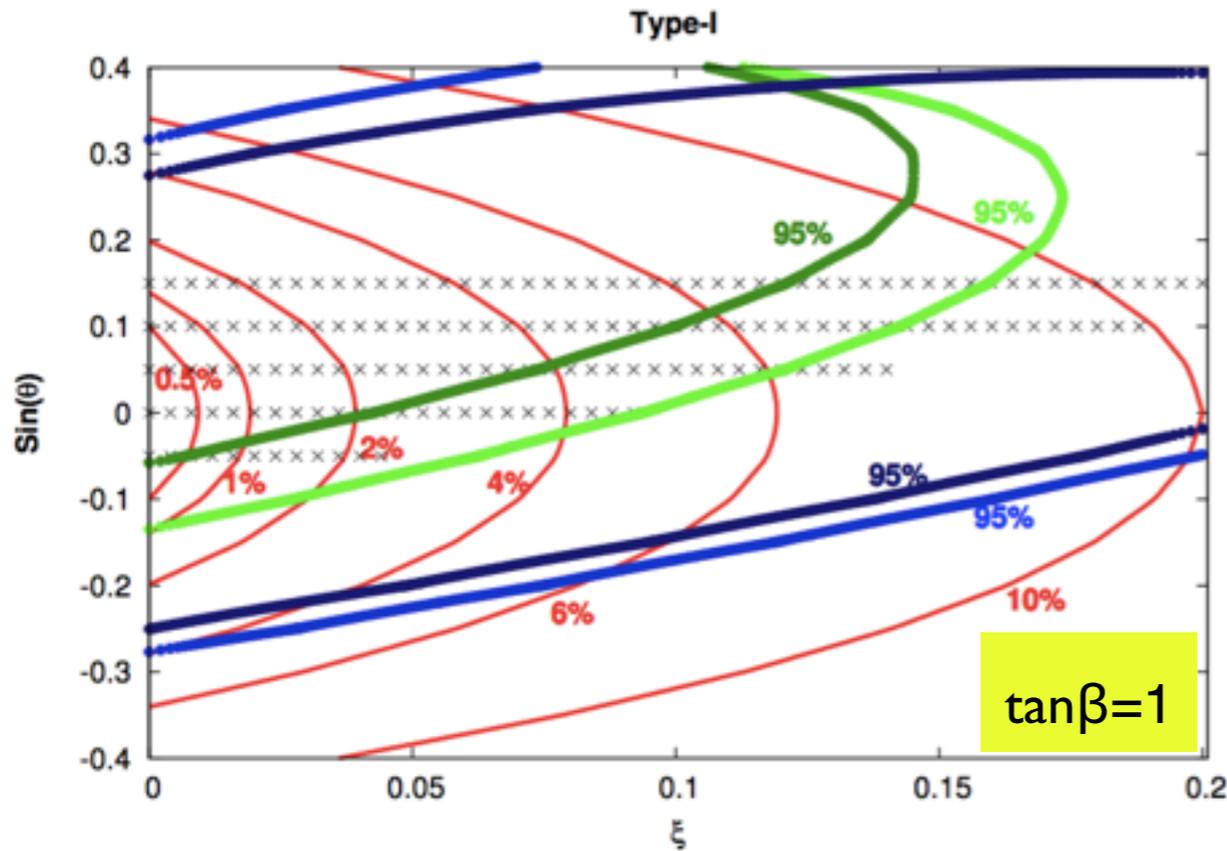
- ☑ **SCENARIO 1:** A deviation in the  $hVV$  and/or  $hff$  couplings is established during the Run2 of the LHC, then an investigation of the 2HDM is called for
- ✓ If  $|\Delta k_V| > 2\%$  then E2HDM unlikely could explain it **because of the theor. and exp. bounds on  $\sin\Theta$** , but it could be possible within the C2HDM
  - ✓ If  $|\Delta k_V| \lesssim 2\%$  a dedicated scrutiny of the decay patterns of all potentially accessible heavy Higgs states could enable to **separate the E2HDM from the C2HDM** through the **combination** of the **differences** in the **BRs** and **production cross sections**

- ☑ **SCENARIO 2:** 😞 No additional Higgs states will have been discovered at the LHC, neither after  $3000 \text{ fb}^{-1}$ , nor deviations in the Higgs couplings
- ✓  $e^+e^-$  colliders will have a great task. The Higgs boson  $h$  discovered at the LHC **will be produced in single-mode** (via Higgs-strahlung  $ee \rightarrow Zh$ , Vector Boson Fusion  $ee \rightarrow eeh$  and associated production via top quarks  $ee \rightarrow tth$ ) **and double-mode** (via  $ee \rightarrow Zhh$ ,  $ee \rightarrow eehh$ ,  $ee \rightarrow tthh$ )
  - ✓ Because of the small background, the **Higgs boson couplings** will be measured with an **extremely good accuracy**  $\sim 0.5\%$  ( $2.5\%$ ) for  $hZZ(htt)$  at ILC(500,500)

Future  $e^+e^-$  machines will have the potential to discriminate between the E2HDM and C2HDM by studying the SM- $h$  cross-sections

# Present and future LHC bounds for the C2HDM Type-I

$m_A = m_{H^\pm} = m_H = 500 \text{ GeV}$     $M = 0.8 m_A$     $m_h = 125 \text{ GeV}$

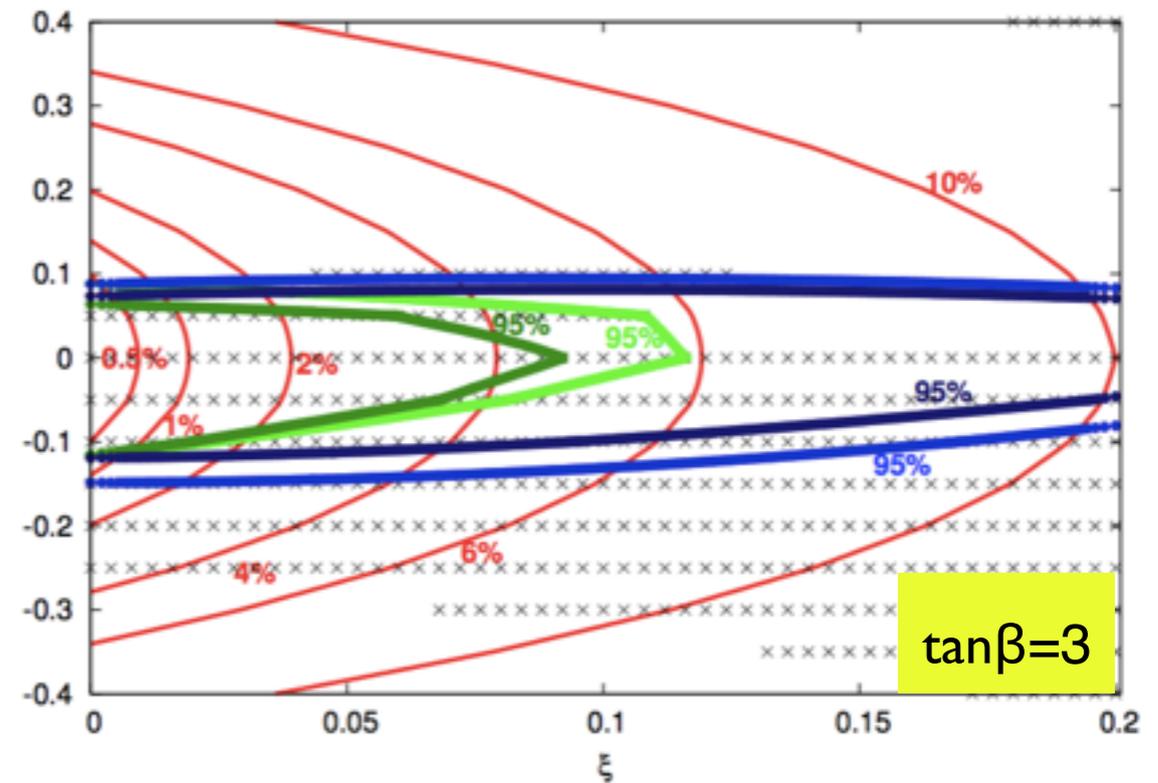
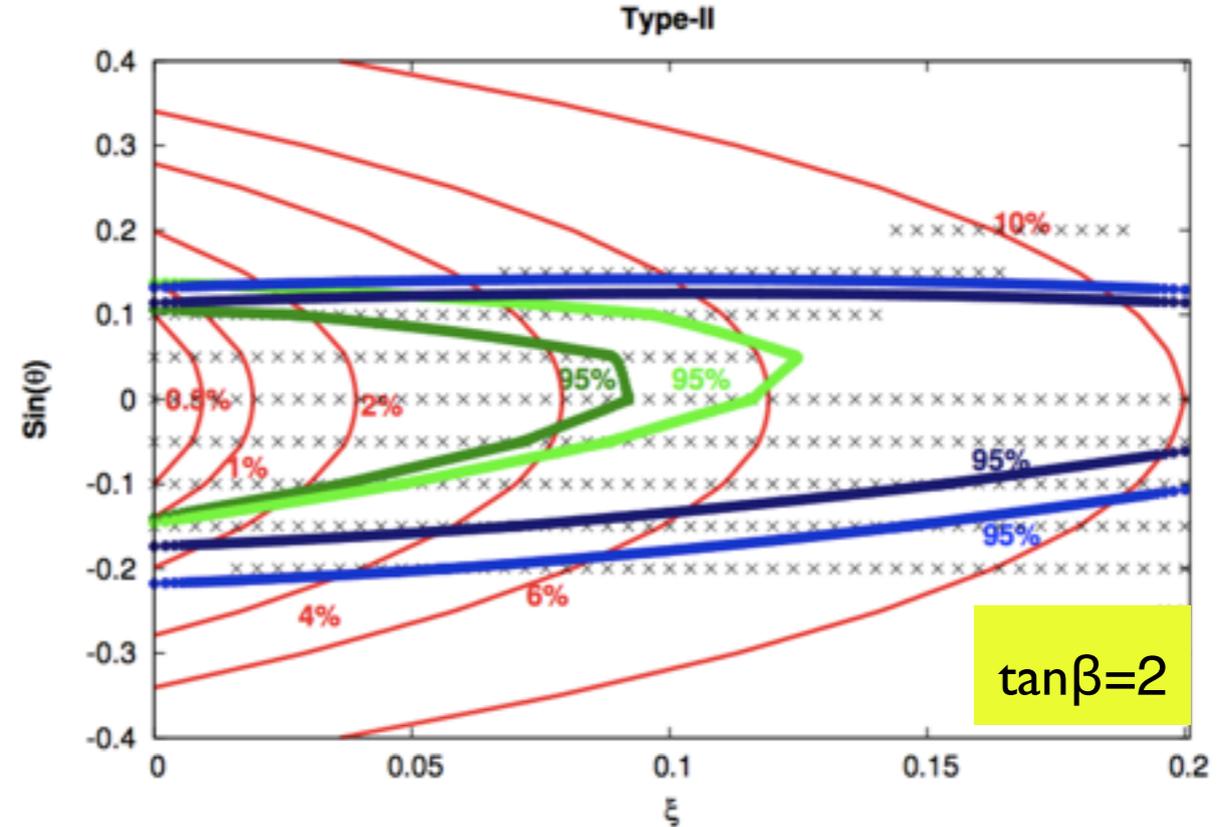
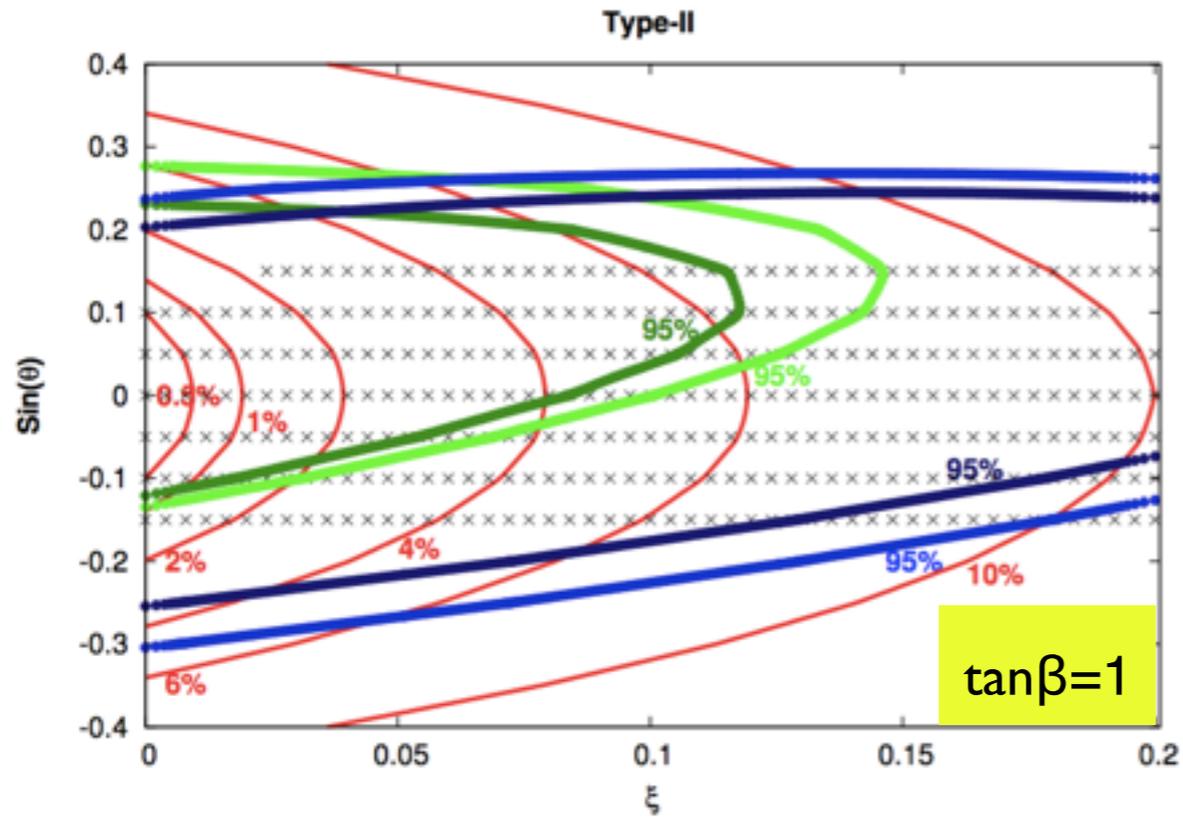


××× = regions 95%CL allowed by current collider data (HiggsBounds tool)

compatibility with the observed Higgs signals (SM) extrapolated at  $300 \text{ fb}^{-1}$   $3000 \text{ fb}^{-1}$

contours of  $|\Delta k_V| = |g_{hVV}^{\text{C2HDM}} / g_{hVV}^{\text{SM}} - 1|$

# Same analysis for the C2HDM Type-II

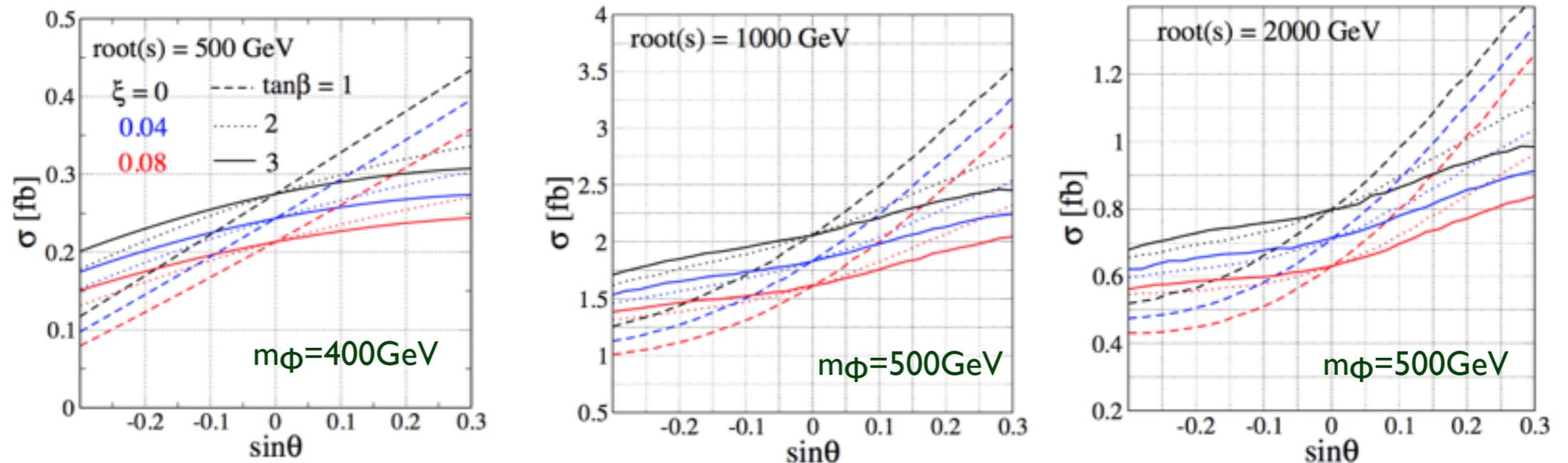
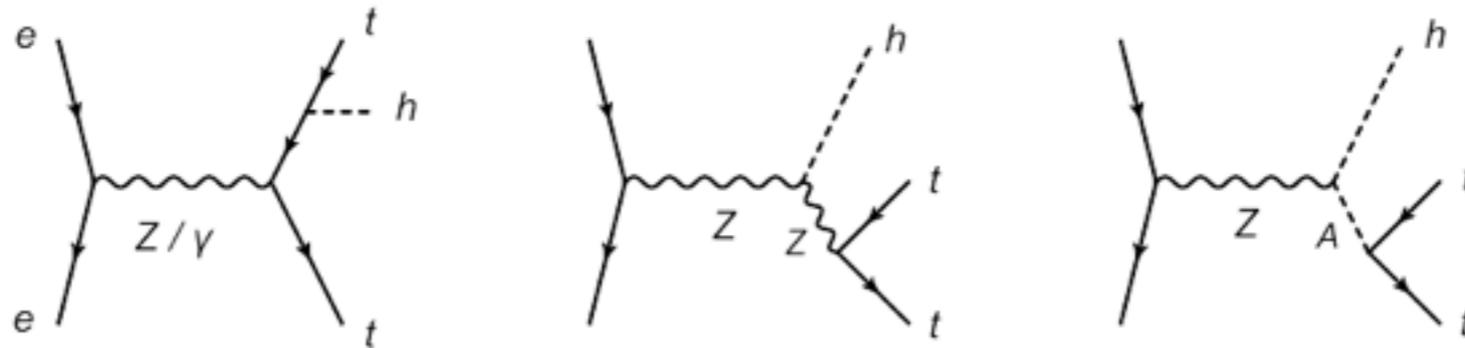


Assumption: no new Higgs boson detected and the properties of SM-like one are greatly constrained

After HL-LHC there remains scope to distinguish C2HDM from E2HDM ( $\xi=0$ ) at future  $e^+e^-$  colliders

# Associated Higgs Boson production with top quarks

## $e^+e^- \rightarrow t\bar{t}h$



At  $\sqrt{s}=1,2$  TeV the on-shell production of  $A$  is realised and the cross section get enhanced. The  $\xi$  dependence acts like an overall rescaling with **negative deviations  $>20\%$  for  $\xi=0.08$**

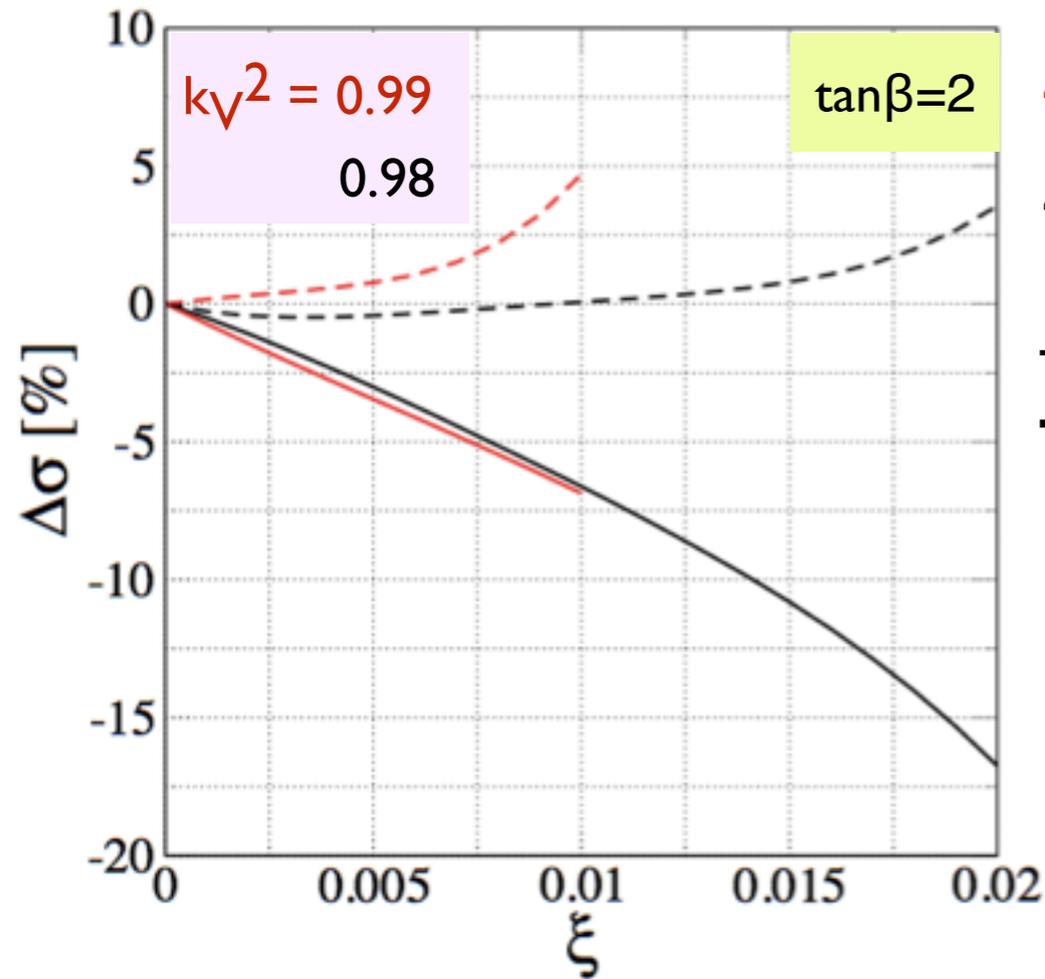
The C2HDM predicts cross sections for  $e^+e^- \rightarrow t\bar{t}h$  that **cannot be realised in the E2HDM**

# Differences in $e^+e^- \rightarrow t\bar{t}h$ cross-section for fixed $k_V^2 = 0.99, 0.98$

$\sqrt{s} = 1000 \text{ GeV}$ ,  $m_A = m_{H^\pm} = m_H = 500 \text{ GeV}$ ,  $M = 0.8$ ,  $m_A = m_h = 125 \text{ GeV}$

$$\Delta\sigma = (\sigma_{\text{C2HDM}} / \sigma_{\text{E2HDM}} - 1)$$

$$k_V = g_{hVV} / g_{hVV}^{\text{SM}}$$



$\Delta k_V = -0.5\%$

$\Delta k_V = -1\%$

-----  $\sin\Theta < 0$

————  $\sin\Theta > 0$

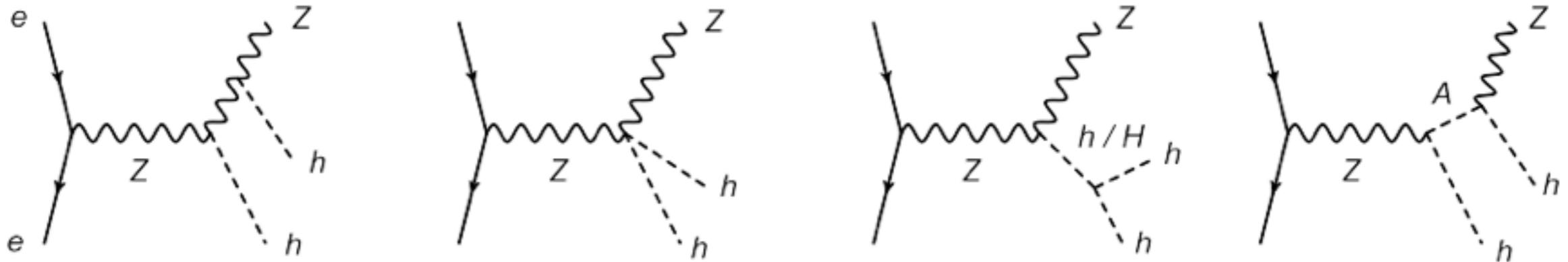
the sign of  $\sin\Theta$  not determined by measuring  $k_V$

the lines correspond to values of Type-I C2HDM parameters **allowed by unitarity and stability bounds** and **after 3000  $\text{fb}^{-1}$  at the LHC**

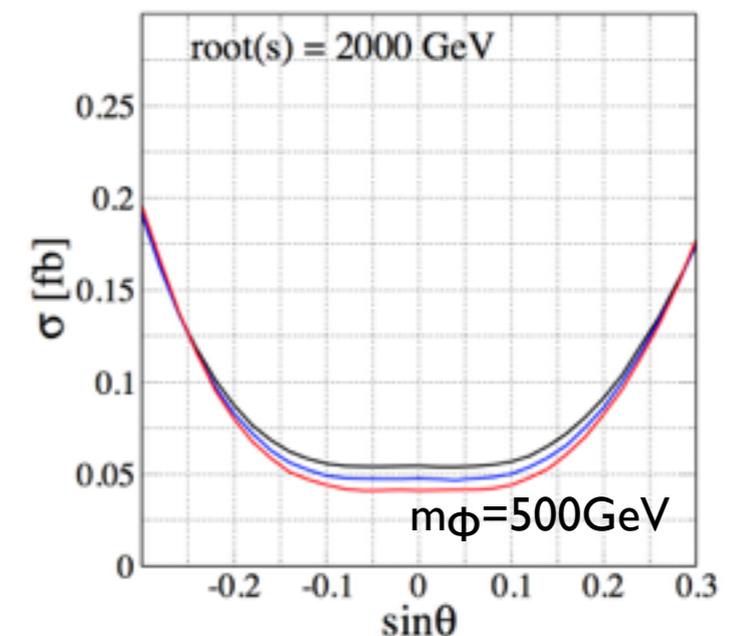
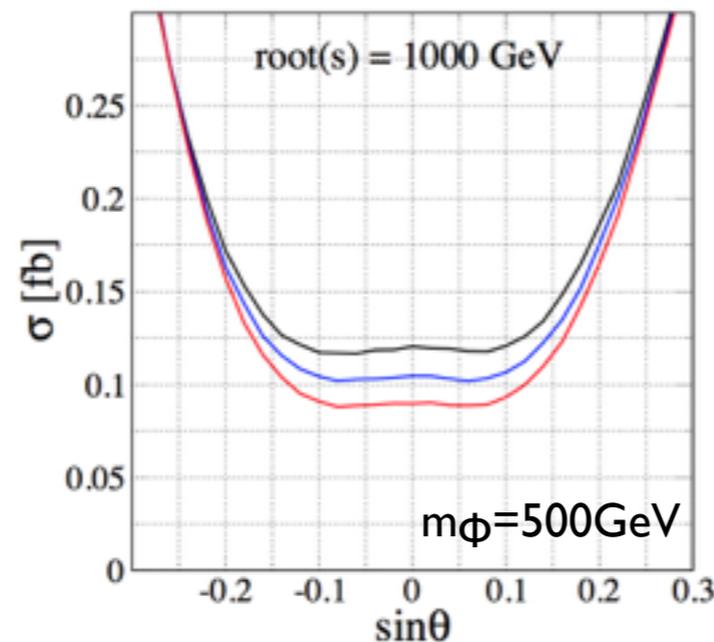
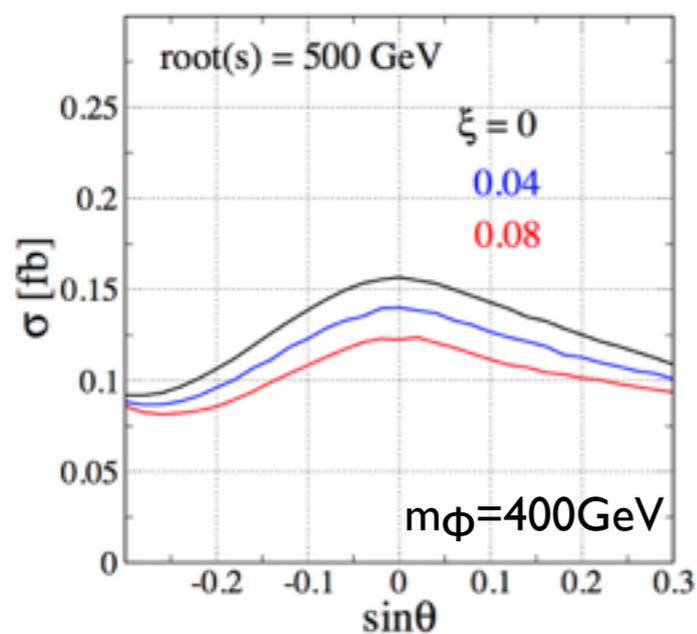
Even with very small deviations in  $k_V$  precisely determined via HS and VBF, the **differences between E2HDM and C2HDM in  $e^+e^- \rightarrow t\bar{t}h$  cross section can be  $\sim 15\%$**

# Double Higgs Boson production: $e^+e^- \rightarrow Zhh$

sensitive to triple-Higgs couplings and to the extra Higgs boson exchanges



$M=0.8m_\phi \quad \tan\beta=2$

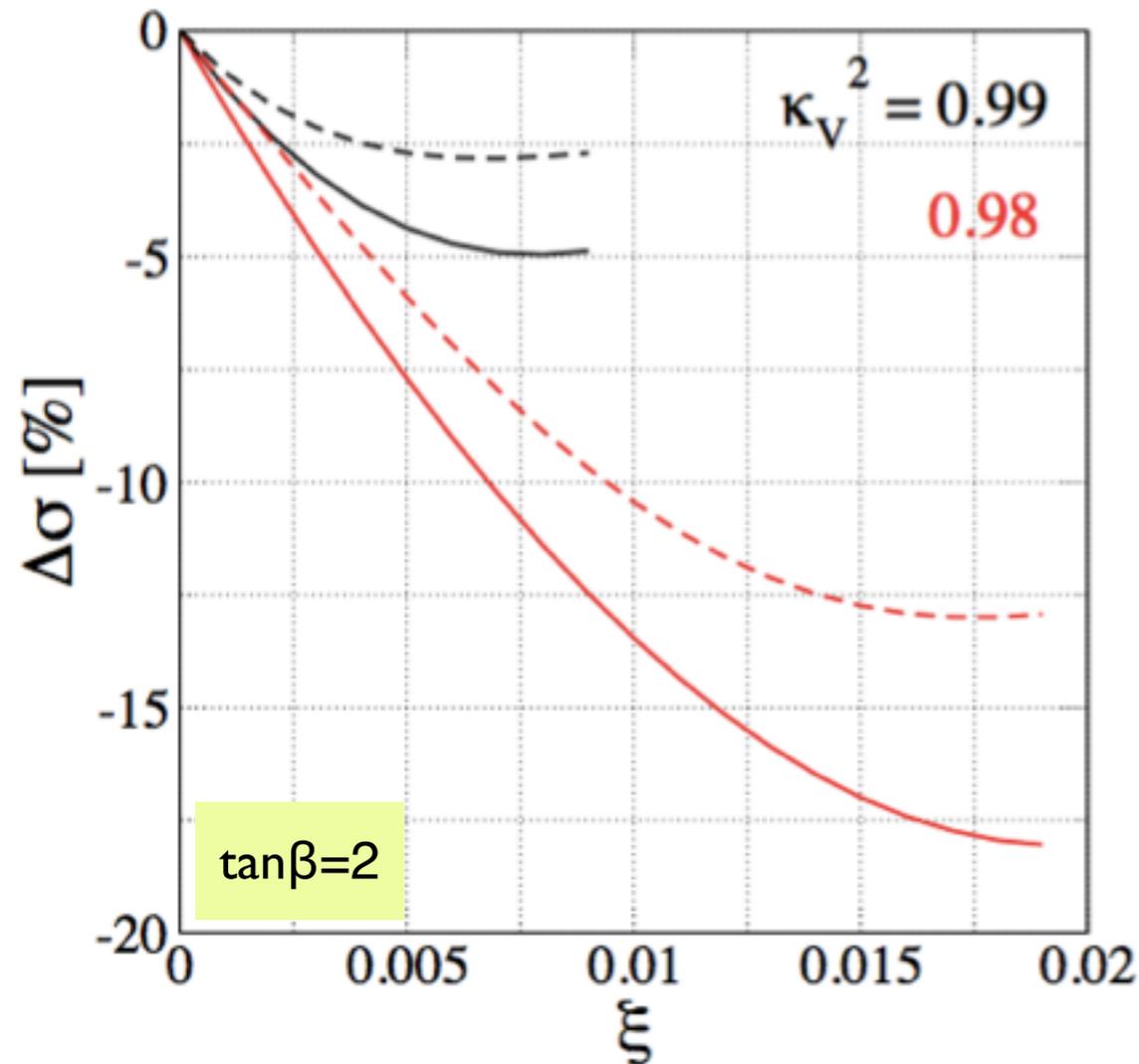


At  $\sqrt{s}=1,2\text{TeV}$  the on-shell production of  $H,A$  is realised, followed by  $H \rightarrow hh$  and  $A \rightarrow Zh$  respectively, both proportional to  $\sin\Theta$

The  $\xi$  dependence remains comparable at all energies being in the 20-30% range

# Differences in cross section for $e^+e^- \rightarrow Zhh$

$\sqrt{s}=1000\text{GeV}$   $m_A=m_{H^\pm}=m_H=500\text{GeV}$   $M=0.8$   $m_A$   $m_h=125\text{GeV}$



$$\Delta\sigma = (\sigma_{\text{C2HDM}}/\sigma_{\text{E2HDM}} - 1)$$

$$k_V = g_{hVV}/g_{hVV}^{\text{SM}}$$

—  $\sin\Theta > 0$

$\Delta\kappa_V = -0.5\%$

- - -  $\sin\Theta < 0$

$\Delta\kappa_V = -1\%$

the lines correspond to values of Type-I C2HDM parameters **allowed by unitarity and stability bounds** and **after 3000 fb<sup>-1</sup> at the LHC**

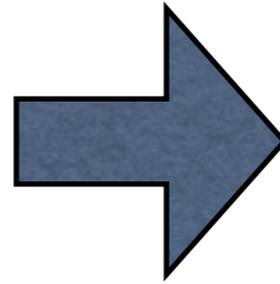
**Large negative differences between C2HDM and E2HDM are predicted also for  $\approx 1\%$  deviations in the  $hVV$  coupling**

# Summary and Conclusions

- ✓ C2HDM amplitudes grow with  $\sqrt{s}$  in bosonic scattering processes. Perturbative unitarity is broken at a certain energy scale depending on the compositeness scale  $f$ . However for LHC ( $e^+e^-$ ) energies and  $m\Phi \lesssim 500\text{GeV}$ , UV completion is not necessary for Higgs studies
- ✓ In presence of a deviation in  $hVV$  couplings from SM prediction, E2HDM would require non-zero mixing case, while C2HDM could achieve this with zero mixing case
- ✓ If deviations are measured at collider experiments, we have indirect evidence for a non-minimal Higgs sector possible belonging to a E2HDM or C2HDM
- ✓ Differences in the decay BR's and production cross sections for the extra Higgs bosons could enable us to distinguish a C2HDM from E2HDM at both hadron and lepton colliders

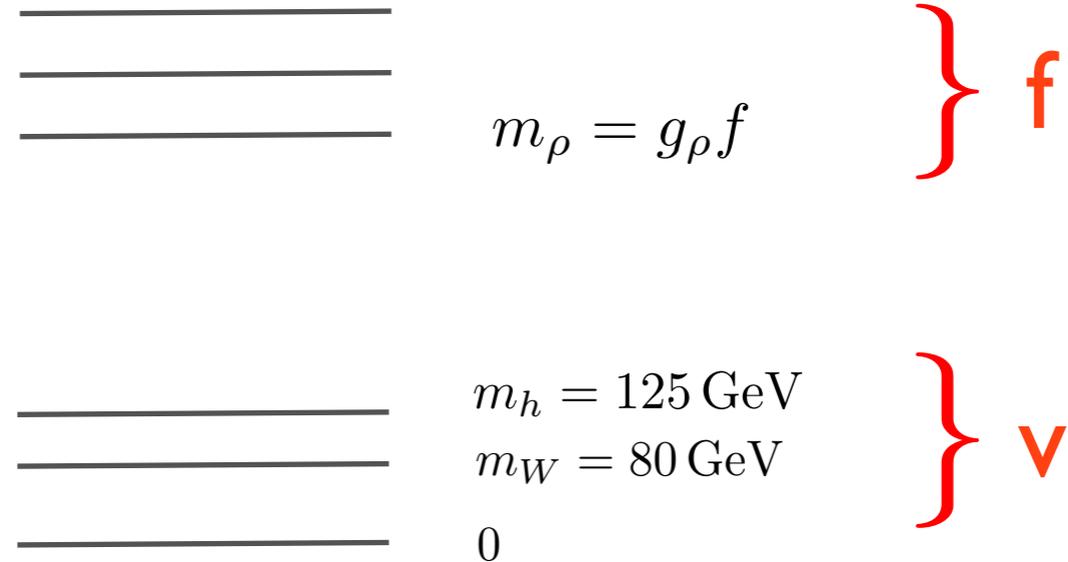
**BACKUP SLIDES**

Strong sector:  
resonances +  
Higgs bound state



Extra particle content:  
• Spin 1 resonances  
• Spin 1/2 resonances

Spectrum:



$g_\rho =$  strong coupling

## Linear elementary-composite couplings (partial compositeness)

$$\Delta_R \bar{q}_R \mathcal{O}_L + \Delta_L \bar{q}_L \mathcal{O}_R + Y \bar{\mathcal{O}}_L H \mathcal{O}_R$$

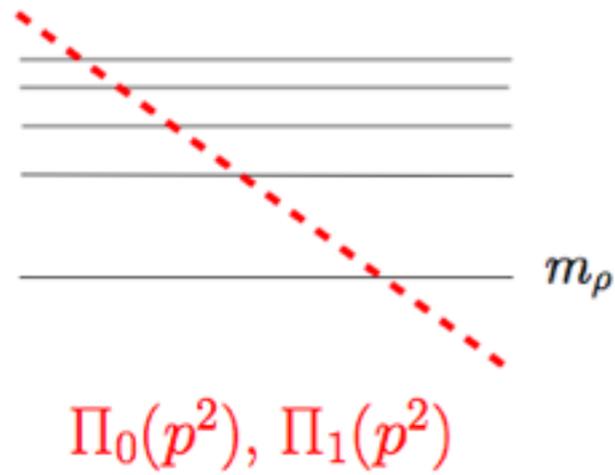
$$y_{SM} = \epsilon_L \cdot Y \cdot \epsilon_R \quad \epsilon = \frac{\Delta}{m_Q}$$

SM hierarchies are generated by the mixings:  
light quarks elementary, top strongly composite

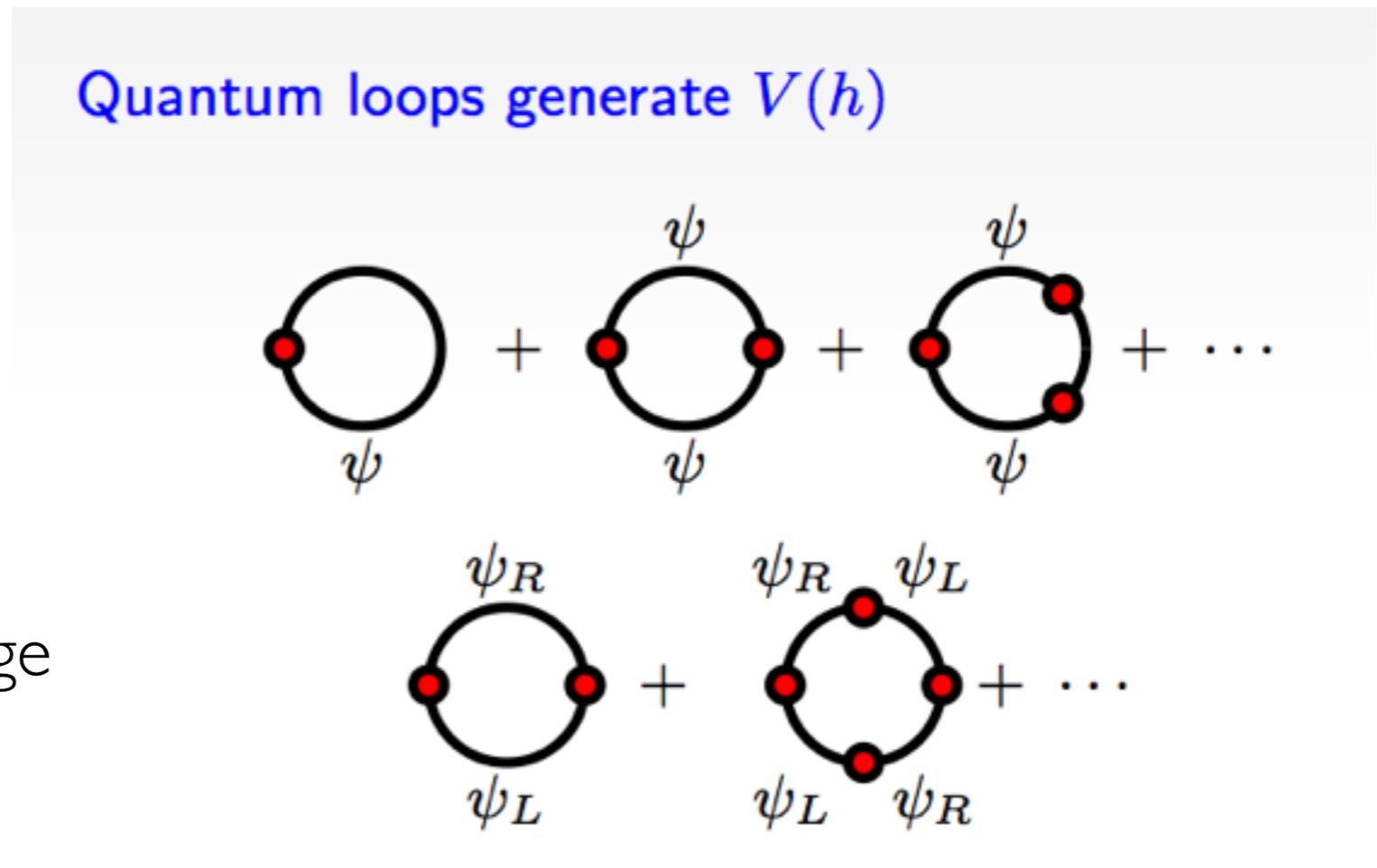
$$m_t \sim \frac{v}{\sqrt{2}} \frac{\Delta_{tL}}{m_\psi} \frac{\Delta_{tR}}{m_\chi} \frac{Y_T}{f}$$

# And the Higgs mass?

Integrate out the composite sector and get a low-energy Lagrangian with form-factors Agashe, Contino, Pomarol '04



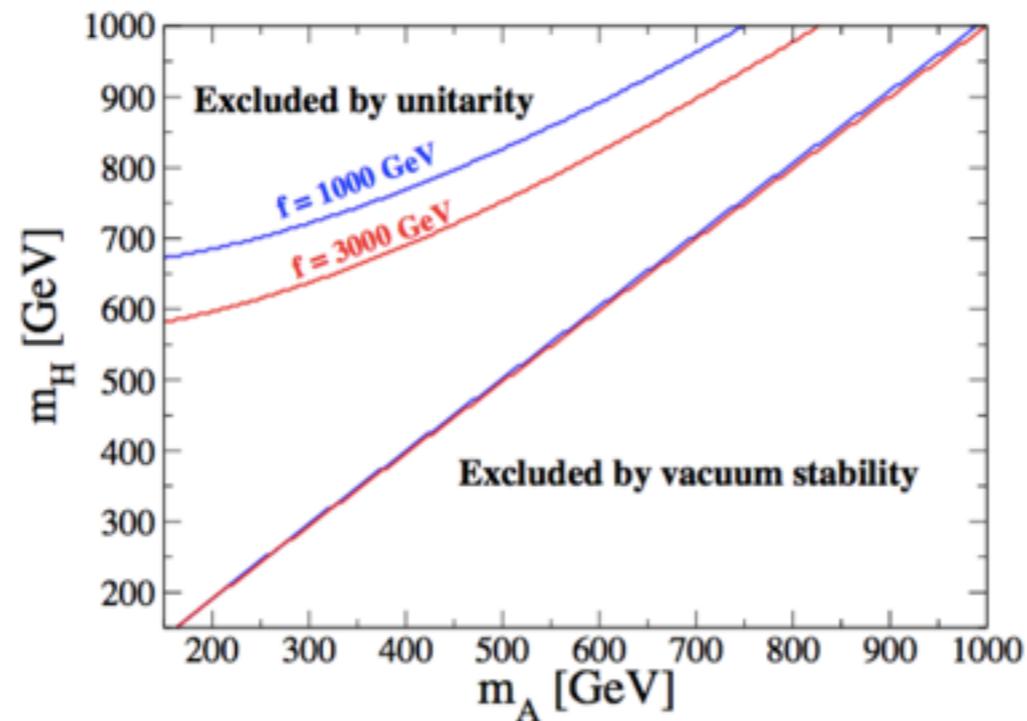
Contribution from the gauge loops subleading



$$m_H \sim 0.3 y_t \frac{m}{f} v$$

# Perturbative Unitarity in the inert C2HDM

- ☑ In the inert model ( $C_2$  symm) there is no  $m_3$  term in the potential ( $M=0$ ) and  $\langle \Phi_2 \rangle = 0$ .  $H$  is the inert Higgs, not coupled to quarks and leptons



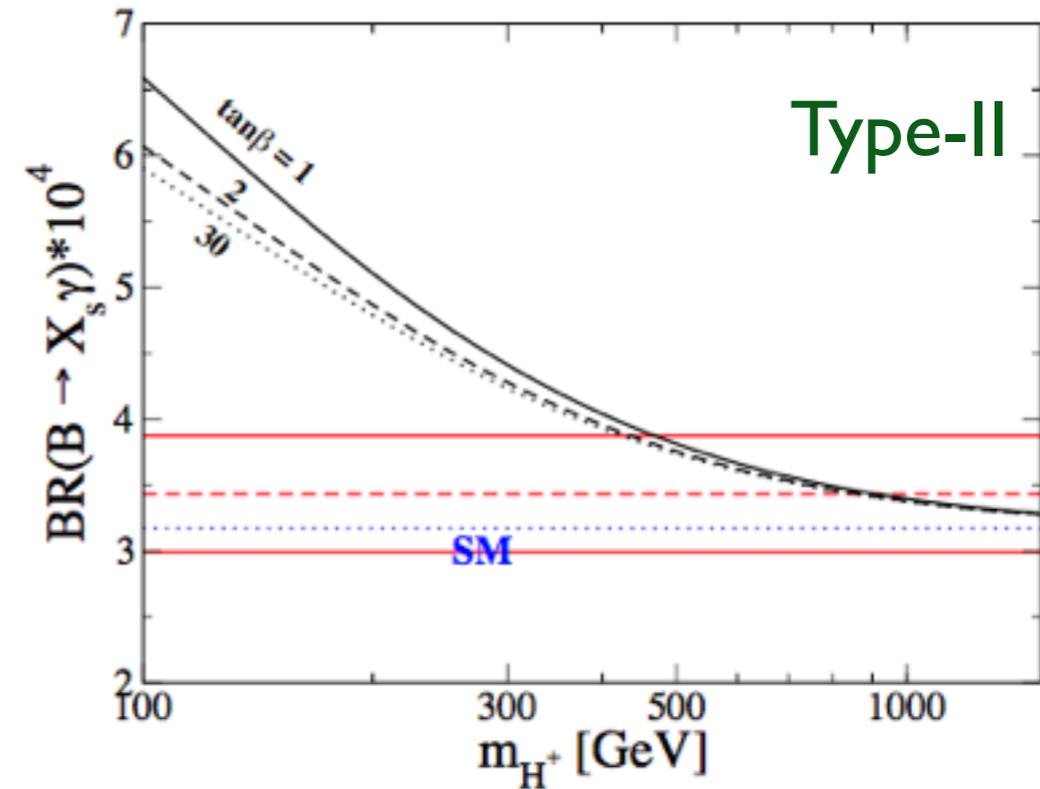
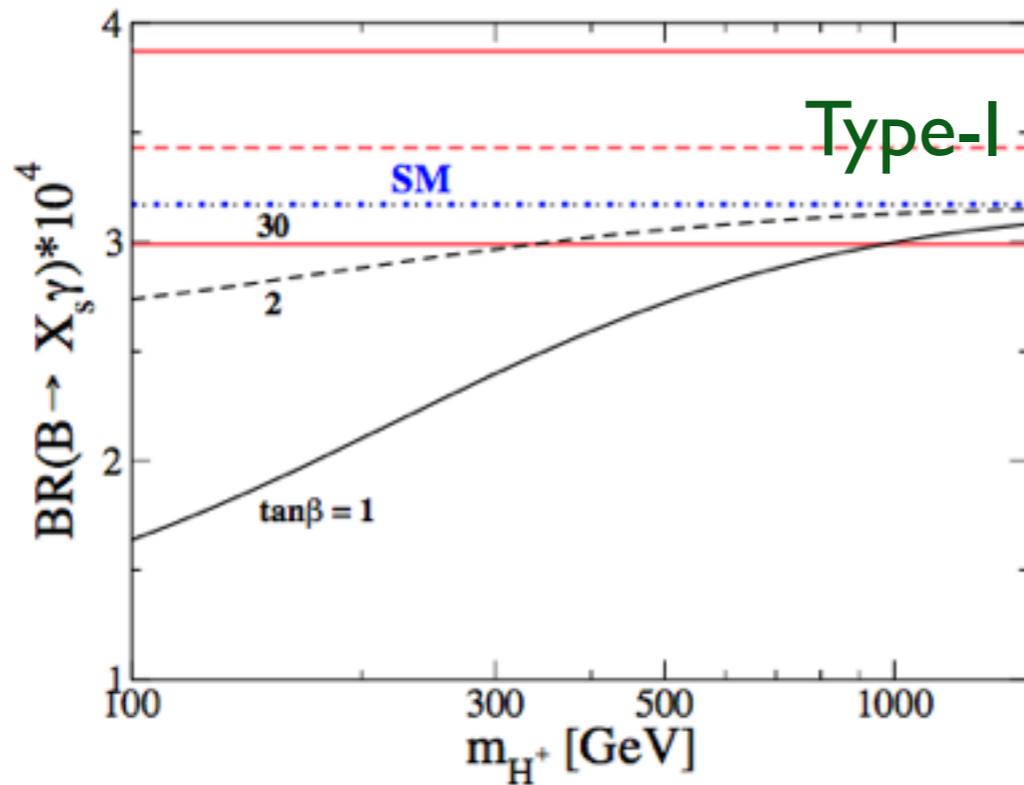
$\sqrt{s} = 3000 \text{ GeV}$   
 $m_{H^\pm} = m_A = m_2$   
 $\lambda_2 = 0.1$   
 $m_h < m_A$

- ☑ A different choice of parameters leading to a different mass spectrum with  $m_H < m_h$  is possible  
 Ex. for  $m_H = m_2 = 100 \text{ GeV}$  the upper limit from unitarity on  $m_{H^\pm} = m_A$  is about  $700 \text{ GeV}$

A dark-matter-motivated scenario is available as it is consistent with the unitarity bounds derived

# Constraints on 2HDM from $B \rightarrow X_s \gamma$

A.G.Akeroyd et al.1605.05881



Predictions for  $\text{Br}(B \rightarrow X_s \gamma)$  at NLO QCD within the **SM** and the 2HDM for  $\tan\beta = 1, 3, 30$

The **red lines** delimit the  $2\sigma$  allowed region from exp. results

**95%CL bounds from NNLO calculation (M.Misiak et al.1503.01789)**

Type-I (Type-X):  $M_{H^+} > 100(200)\text{GeV}$  for  $\tan\beta = 2.5(2)$ , no bound for  $\tan\beta > 3$

Type-II (Type-Y):  $M_{H^+} > 480\text{GeV}$  for  $\tan\beta > 2$

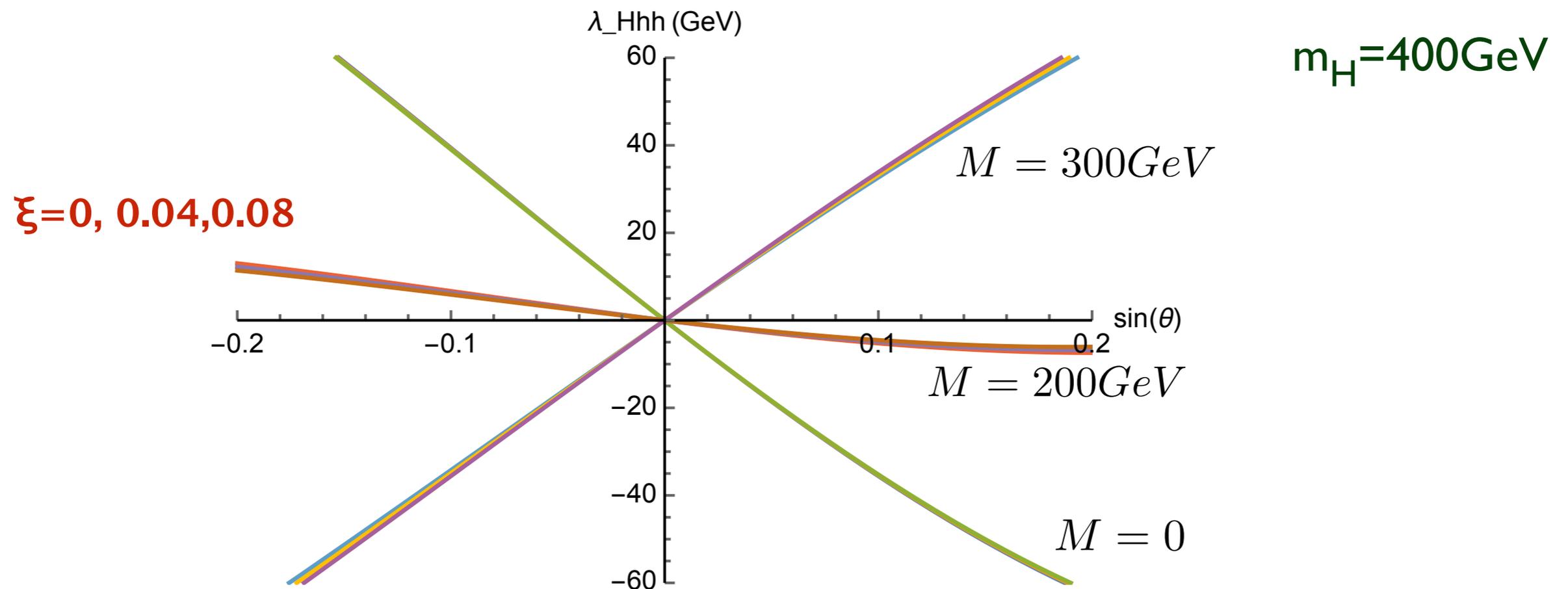
**Loose bounds on  $m_{H^+}$  in Type-I for  $\tan\beta \geq 2$**

# Trilinear Hhh coupling

$$\lambda_{Hhh} = \frac{s_\theta}{2v_{\text{SM}}s_{2\beta}} \left[ -s_{2(\beta+\theta)}(2m_h^2 + m_H^2) + (s_{2\beta} + 3s_{2(\beta+\theta)})M^2 \right] \\ + \frac{\xi}{12v_{\text{SM}}} s_\theta \left[ m_H^2 - 2m_h^2 + (1 + 3c_{2\theta} + 6 \cot 2\beta s_{2\theta})M^2 \right] + \mathcal{O}(\xi^2)$$

nearly independent on  $\tan\beta$  for small  $\Theta$

$\tan\beta=1$

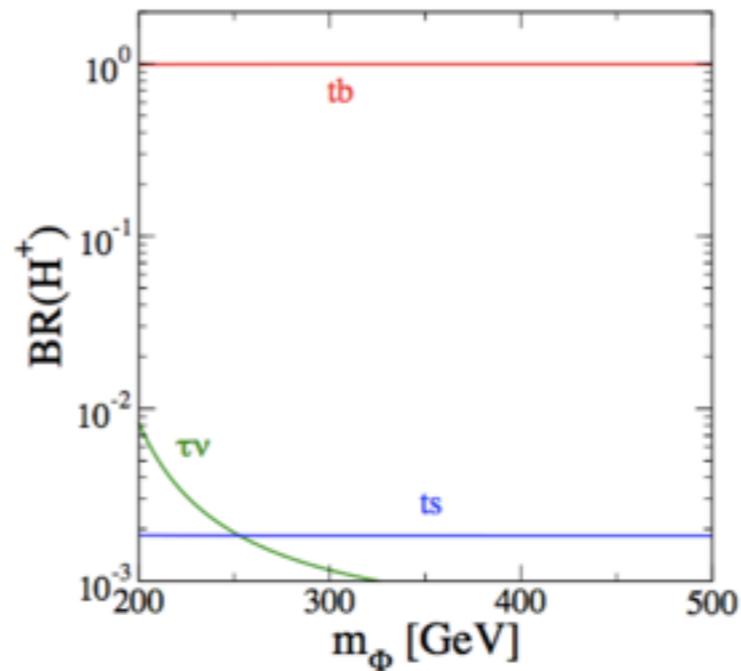
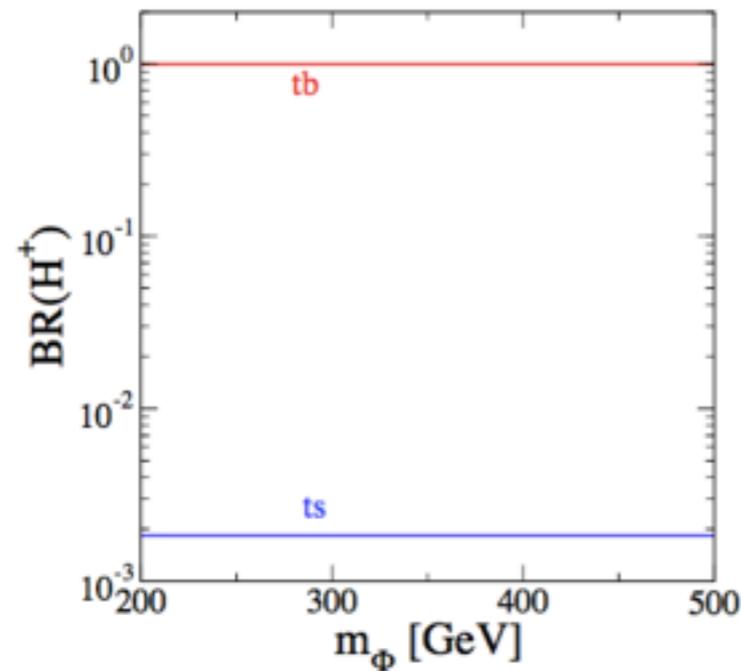
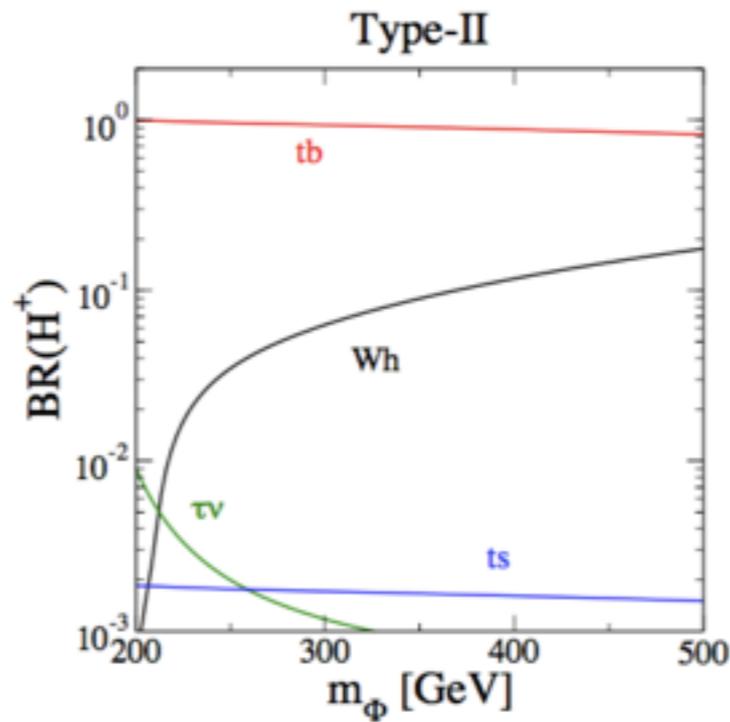
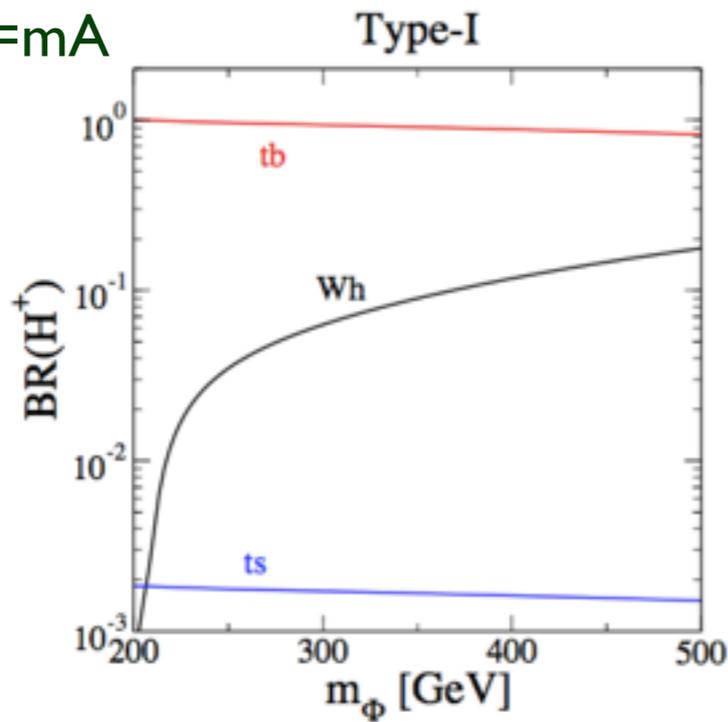


# Decays of the extra-Higgs boson $H^+$

$m_\phi = m_H = m_{H^+} = m_A$

$M = 0.8m_A$ ,

$\tan\beta = 2$



$\Delta k_V = -2\%$

E2HDM  
( $\sin\Theta = -0.2, \xi = 0$ )

C2HDM  
( $\sin\Theta = 0, \xi = 0.04$ )

$H^+ \rightarrow W^+h$  is a relevant channel in E2ChM while it is absent in the C2HDM with  $\sin\Theta = 0$  (in all the 4 Yukawa Types)

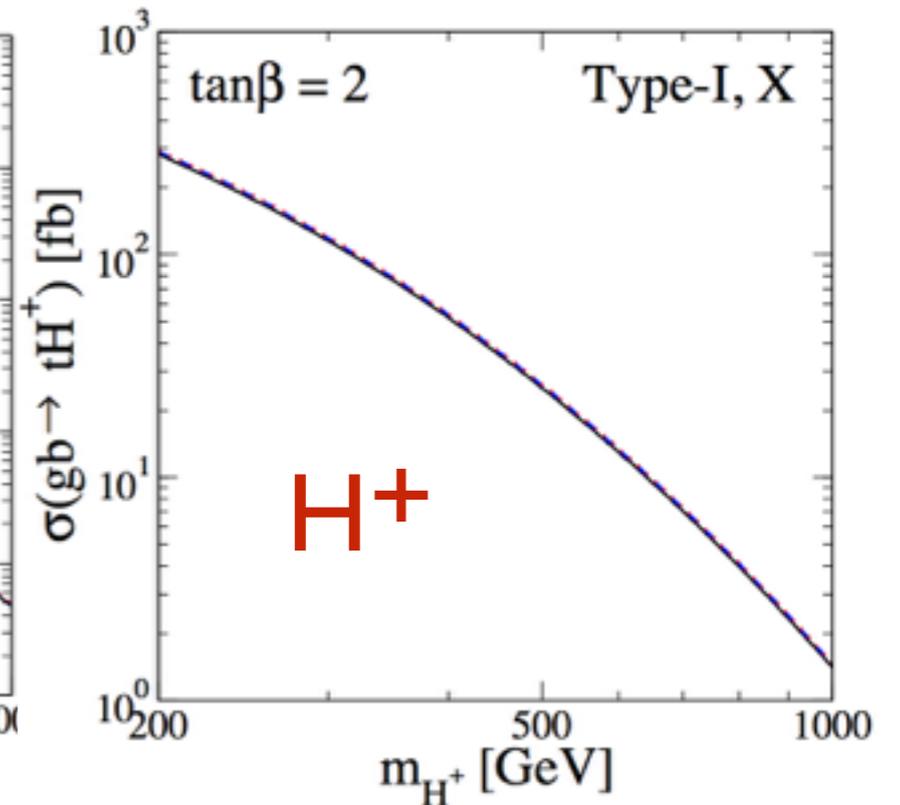
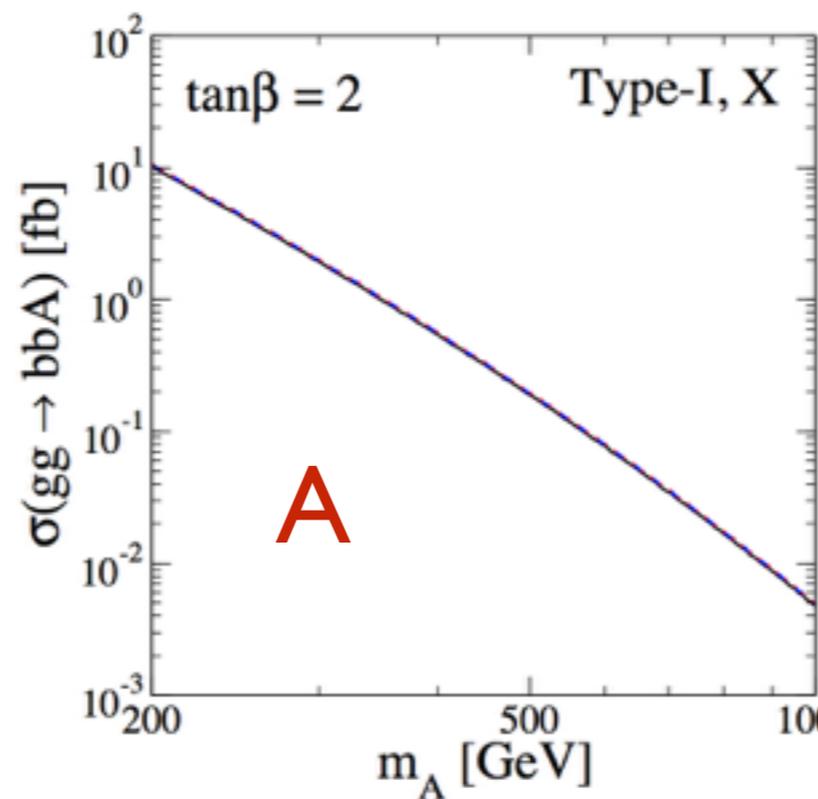
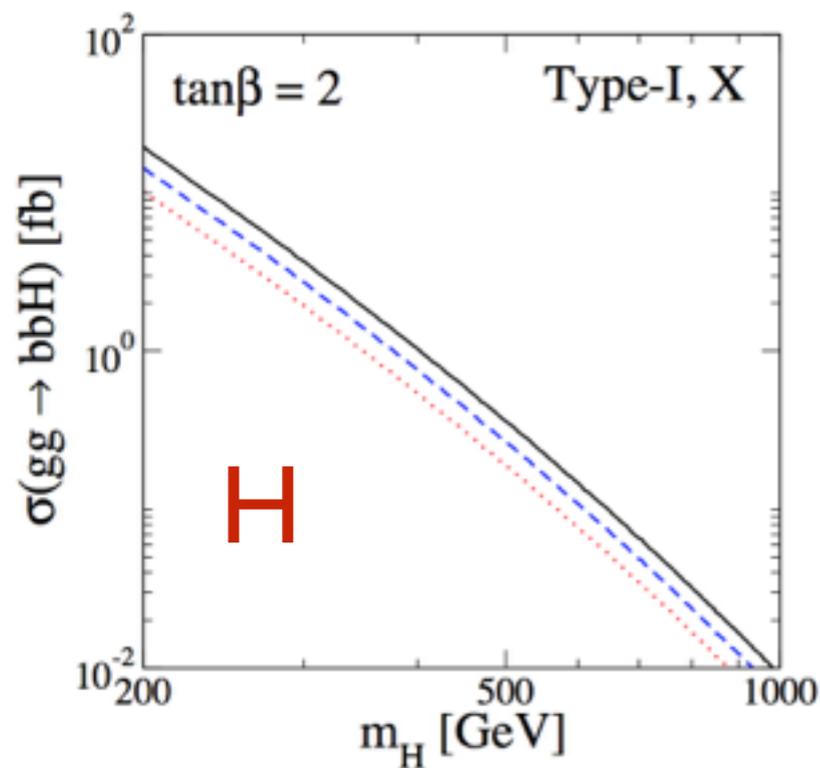
# Productions of the extra-Higgs bosons at the LHC

$$\sigma (gg \rightarrow bbH/A) \quad \text{and} \quad \sigma (gb \rightarrow tH^+)$$

$\sqrt{s}=13 \text{ TeV}$

E2HDM: BP1 ( $\sin\Theta=-0.2, \xi=0$ )

C2HDM: BP2 ( $\sin\Theta=-0.1, \xi=0.03$ ), BP3 ( $\sin\Theta=0, \xi=0.04$ )



Relevant differences between E2HDM and C2HDM only for H production  
(for all Types and all  $\tan\beta$  values)