Gauss's Law Some Figures for Lecture PHYS-208

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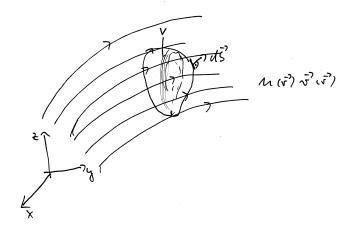
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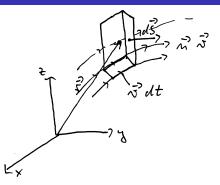


Fluid Flow



Flow of a fluid with particle density, n and velocity field \vec{v} through a volume, V.

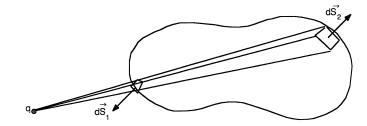
Particle Flux through Surface Element



- ▶ In time interval dt all particles inside the volume element $dV = \vec{v}(\vec{r}) d\vec{S} dt$ flow through surface.
- number of those particles: $dN = n(\vec{r})dV$
- ▶ total number of particles per time, flowing out of V:

$$\frac{\mathrm{d}N}{\mathrm{d}t} = \mathsf{flux} = \int_{\partial V} \mathrm{d}\vec{S} \; n(\vec{r})\vec{v}(\vec{r}), \quad \partial V: \text{ boundary of } V$$

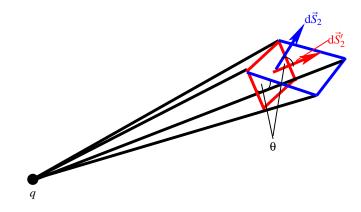
Gauss's Law (Proof for point particle outside $V \mid$)



- split ∂V in rectangular surface elements
- draw cone through surface elements $\mathrm{d}ec{S}_1$ and $\mathrm{d}ec{S}_2$

Figure from: W. H. Bassichis, DON'T PANIC, Vol. II, 5th Edition, OR Publishing (2005)

Gauss's Law (Proof for point particle outside $V | I \rangle$



► Surface element from ∂V (blue) with its cone (black) compared to intersection of cone with sphere (red)

$$|\mathrm{d}\vec{S}_2'| = \vec{i}_r \mathrm{d}\vec{S}_2' = |\mathrm{d}\vec{S}_2|\cos\theta = \vec{i}_r \mathrm{d}\vec{S}_2$$