Electromagnetic Probes in a Coarse-Graining Approach

Hendrik van Hees

Goethe University Frankfurt

November 26, 2018







Hendrik van Hees (GU Frankfurt)

Dileptons in HICs

Outline

Heavy-ion collisions on one slide

Electromagnetic probes

- Chiral symmetry and QCD phase diagram
- Electromagnetic radiation from hot/dense QCD matter
- Hadronic many-body theory

Bulk-medium evolution with transport and coarse graining

- coarse-graining in UrQMD
- Dileptons in heavy-ion collisions
 - Dielectrons (SIS/HADES)
 - Dimuons (SPS/NA60)
 - Dielectrons at RHIC
 - Dielectrons at FAIR/RHIC-BES
- Signatures of the QCD-phase structure?
- Conclusions and Outlook

Heavy-Ion collisions in a Nutshell

- theory of strong interactions: Quantum Chromo Dynamics, QCD
- GSI SIS: pp, dp, pA, AA collisions at low energies ($E_{kin} = 1.25-3.5 \text{ GeV}$) Dielectrons from HADES
- CERN SPS: AA collisions with $E_{kin} = 158 \text{ GeV}$ per nucleon on a fixed target (center-mass energy: $\sqrt{s_{NN}} = 17.3 \text{ GeV}$) dileptons (particularly $\mu^+\mu^-$ in In-In collisions from NA60)
- BNL RHIC: Au Au collisions with center-mass energy of $\sqrt{s_{NN}} = 200 \text{ GeV}$; "beam-energy scan" $\sqrt{s_{NN}} = 7.7-39 \text{ GeV}$ dileptons from STAR and PHENIX; direct photons from PHENIX
- CERN LHC: Pb-Pb collisions at $\sqrt{s} = 2.76$ TeV per nucleon direct photons from ALICE
- future experiments at CBM/FAIR and NICA: high $\mu_{\rm B}$



Electromagnetic probes theory perspective

Vacuum Baseline: $e^+e^- \rightarrow$ hadrons



- probes all hadrons with quantum numbers of γ^*
- $R_{\text{QM}} = N_c \sum_{f=u,d,s} Q_f^2 = 3 \times [(2/3)^2 + (-1/3)^2 + (-1/3)^2] = 2$
- Our aim pp $\rightarrow \ell^+ \ell^-$, pA $\rightarrow \ell^+ \ell^-$, AA $\rightarrow \ell^+ \ell^-$ ($\ell = e, \mu$)

Hadron phenomenology and chiral symmetry

- QCD in light-quark sector (u, d, (s)): chiral symmetry
- in vacuum: Spontaneous breaking of chiral symmetry because $\langle \overline{q}q \rangle \neq 0$
- \Rightarrow mass splitting of chiral partners



The QCD-phase diagram

- hot and dense matter: quarks and gluons close together
- highly energetic collisions ⇒ "deconfinement"
- quarks and gluons relevant dof \Rightarrow quark-gluon plasma
- still strongly interacting \Rightarrow fast thermalization!



The QCD-phase diagram

- at high temperature/density: restoration of chiral symmetry
- lattice QCD: $T_c^{\chi} \simeq T_c^{\text{deconf}}$





- two main theoretical ideas
 - "dropping masses": $m_{
 m had} \propto \left< \overline{\psi} \psi \right>$
 - "melting resonances": broadening of spectra through medium effects
 - More theoretical question: realization of chiral symmetry in nature?

pert. QCD

Dropping Masses?

pert. QCD

Melting Resonances?

Mass

Electromagnetic probes in heavy-ion collisions





Fig. by A. Drees

Electromagnetic probes from thermal source

- photon and dilepton thermal emission rates given by same electromagnetic-current-correlation function $(J_{\mu} = \sum_{f} Q_{f} \overline{\psi_{f}} \gamma_{\mu} \psi_{f})$
- McLerran-Toimela formula [МТ85, GK91]

$$q_{0} \frac{\mathrm{d}N_{\gamma}}{\mathrm{d}^{4} x \mathrm{d}^{3} \vec{q}} = -\frac{\alpha_{\mathrm{em}}}{2\pi^{2}} g^{\mu\nu} \mathrm{Im} \left. \prod_{\mu\nu}^{(\mathrm{ret})}(q, u) \right|_{q_{0} = |\vec{q}|} f_{B}(q \cdot u)$$
$$\frac{\mathrm{d}N_{e^{+}e^{-}}}{\mathrm{d}^{4} x \mathrm{d}^{4} q} = -g^{\mu\nu} \frac{\alpha^{2}}{3q^{2}\pi^{3}} \mathrm{Im} \left. \prod_{\mu\nu}^{(\mathrm{ret})}(q, u) \right|_{q^{2} = M_{e^{+}e^{-}}^{2}} f_{B}(q \cdot u)$$

- Lorentz covariant (dependent on four-velocity of fluid cell, *u*)
- $q \cdot u = E_{cm}$: Doppler blue shift of q_T spectra!
- to lowest order in α : $4\pi \alpha \Pi_{\mu\nu} \simeq \Sigma_{\mu\nu}^{(\gamma)}$
- vector-meson dominance model:

$$\Sigma^{\gamma}_{\mu\nu} =$$

0

• $\ell^+\ell^-$ -inv.-mass spectra

 \Rightarrow in-med. spectral functions of vector mesons (ρ , ω , ϕ)!

Radiation from thermal QGP: $q\bar{q}$ annihilation

• General: McLerran-Toimela formula

$$\frac{\mathrm{d}N_{l+l-}^{(\mathrm{M1})}}{\mathrm{d}^4 x \mathrm{d}^4 q} = -\frac{\alpha^2}{3\pi^3} \frac{L(M^2)}{M^2} g_{\mu\nu} \mathrm{Im} \sum_i \Pi_{\mathrm{em},i}^{\mu\nu} (M,\vec{q}) f_B(q \cdot u)$$

- *i* enumerates partonic/hadronic sources of em. currents
- in-medium em. current-current correlation function

$$\Pi_{\mathrm{em},i}^{\mu\nu} = \mathrm{i} \int \mathrm{d}^4 x \, \exp(\mathrm{i} q \, x) \Theta(x^0) \left\langle \left[j_{\mathrm{em},i}^{\mu}(x), j_{\mathrm{em},i}^{\nu}(0) \right] \right\rangle$$

- in QGP phase: $q\bar{q}$ annihilation
- hard-thermal-loop improved em. current-current correlator

Radiation from thermal sources: ρ decays

• model assumption: vector-meson dominance

$$\frac{\rho}{d^{M}} \frac{\gamma^{*}}{\rho \to l^{+}l^{-}} = \frac{M}{q^{0}} \Gamma_{\rho \to l^{+}l^{-}}(M) \frac{dN_{\rho}}{d^{3}\vec{x}d^{4}q}$$
$$= -\frac{\alpha^{2}}{3\pi^{3}} \frac{L(M^{2})}{M^{2}} \frac{m_{\rho}^{4}}{g_{\rho}^{2}} g_{\mu\nu} \operatorname{Im} D_{\rho}^{\mu\nu}(M,\vec{q}) f_{B}\left(\frac{q \cdot u - 2\mu_{\pi}(t)}{T(t)}\right)$$

- special case of McLerran-Toimela (MT) formula
- $M^2 = q^2$: invariant mass, *M*, of dilepton pair
- $L(M^2) = (1 + 2m_l^2/M^2)\sqrt{1 4m_l^2/M^2}$: dilepton phase-space factor
- $D_{\rho}^{\mu\nu}(M, \vec{q})$: (four-transverse part of) in-medium ρ propagator at given $T(t), \mu_{\text{meson/baryon}}(t)$
- analogous for ω and ϕ

Transition form factors: "ho mesons" via VMD



- vector mesons have "vacuum spectral shapes"
- propagated as "on-shell particles" of finite lifetime and variable mass
- Dalitz decay: 1 particle → 3 particles
- $V: \omega \to \pi + \gamma^* \to \pi + \ell^+ + \ell^-$
- $P, S: \pi, \eta \to \gamma + \gamma^* \to \gamma + \ell^+ + \ell^-$
- *R*: Baryon resonances $\Delta, N^* \rightarrow N + V \rightarrow N + \gamma^* \rightarrow N + \ell^+ + \ell^-$
- vector-meson dominance





GiBUU: " ρ meson" in pp

• production through hadron resonances $NN \rightarrow NR \rightarrow NN\rho$, $NN \rightarrow N\Delta \rightarrow NN\pi\rho$



- plots: J. Weil et al [WHM12, ABB⁺14]
- VMD model ⇔ em. transition form factors of baryon resonances!
- " ρ "-line shape "modified" already in elementary hadronic reactions
- due to production mechanism via resonances

Dileptons in HICs

Hadronic many-body theory

- hadronic many-body theory (HMBT) for vector mesons [Ko et al, Chanfray et al, Herrmann et al, Rapp et al, ...]
- $\pi\pi$ interactions and baryonic excitations
- effective hadronic models, implementing symmetries
- parameters fixed from phenomenology (photon absorption at nucleons and nuclei, $\pi N \rightarrow \rho N$)
- evaluated at finite temperature and density
- self-energies \Rightarrow mass shift and broadening in the medium



• Baryons important, even at low **net** baryon density $n_B - n_{\bar{B}}$

• reason: $n_B + n_{\bar{B}}$ relevant (CP inv. of strong interactions)

Meson contributions



In-medium spectral functions and baryon effects



[RW99]

- baryon effects important
 - large contribution to broadening of the peak
 - responsible for most of the strength at small M

Dilepton rates: Hadron gas \leftrightarrow QGP

- in-medium hadron gas matches with QGP
- similar results also for γ rates
- "quark-hadron duality"?



[Rap13]

Bulk-medium evolution

Bulk evolution with transport and coarse graining

- established transport models for bulk evolution
 - e.g., UrQMD, GiBUU, BAMPS, (p)HSD,...
 - solve Boltzmann equation for hadrons and/or partons
- dilemma: need medium-modified dilepton/photon emission rates
- usually available only in equilibrium QFT calculations
- ways out:
 - use (ideal) hydrodynamics ⇒ local thermal equilibrium
 ⇒ use equilibrium rates
 - use transport-hydro hybrid model: treat early stage with transport, then coarse grain ⇒ switch to hydro
 - \Rightarrow switch back to transport (Cooper-Frye "particlization")
- here: UrQMD transport for entire bulk evolution
 - \Rightarrow use coarse graining in space-time cells \Rightarrow extract $T, \mu_B, \mu_{\pi}, \dots$
 - \Rightarrow use equilibrium rates locally

- problem with medium modifications of spectral functions/interactions
- only available in equilibrium many-body QFT models
- use "in-medium cross sections" naively: double counting?!?
- way out: map transport to local-equilibrium fluid
- use ensemble of UrQMD runs with an equation of state
- space-time grid with $\Delta t = 0.2 \text{ fm}/c$, $\Delta x = 0.8 \text{ fm}$
- fit temperature, chemical potentials, flow-velocity field from anisotropic energy-momentum tensor [FMRS13]

$$T^{\mu\nu} = (e + P_{\perp})u^{\mu}u^{\nu} - P_{\perp}g^{\mu\nu} - (P_{\parallel} - P_{\perp})V^{\mu}V^{\nu}$$

- thermal rates from partonic/hadronic QFT become applicable
- here: extrapolated lattice QGP and Rapp-Wambach HMBT
- caveat: consistency between EoS, matter content of QFT model/UrQMD!



• pressure anisotropy (for In+In @ SPS; NA60)



- energy/baryon density \Rightarrow *T*, $\mu_{\rm B}$ (for In+In @ SPS; NA60)
- central "fluid" cell!



Dielectrons (SIS/HADES)

- coarse-graining method works at low energies!
- UrQMD-medium evolution + RW-QFT rates



- dielectron spectra from Ar + KCl(1.76 AGeV) \rightarrow e⁺e⁻ (SIS/HADES)
- m_t spectra
- $M_{\rm ee} < 0.13 \, {
 m GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV) \rightarrow e⁺e⁻ (SIS/HADES)
- m_t spectra
- $0.13 \, \text{GeV} M_{ee} < 0.3 \, \text{GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV) \rightarrow e⁺e⁻ (SIS/HADES)
- m_t spectra
- $0.3 \, {\rm GeV} M_{\rm ee} < 0.45 \, {\rm GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV) \rightarrow e⁺e⁻ (SIS/HADES)
- m_t spectra
- $0.45 \, \text{GeV} M_{ee} < 0.65 \, \text{GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV) \rightarrow e⁺e⁻ (SIS/HADES)
- m_t spectra
- $M_{\rm ee} > 0.65 \, {\rm GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV) \rightarrow e⁺e⁻ (SIS/HADES)
- m_t spectra
- rapidity spectrum ($M_{ee} < 0.13 \text{ GeV}$)



CGUrQMD: Au+Au (1.23 AGeV) (SIS/HADES)



[T. Galtyuk, Quark Matter 2017 talk]

- good agreement between models and data
- consistency between two independent coarse-grained-UrQMD simulations
- based on same Rapp-Wambach in-medium rates

Dimuons (SPS/NA60)

- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- ۲
- min-bias data $(dN_{ch}/dy = 120)$ higher IMR: provides averaged true temperature

 $\langle T \rangle_{1.5 \,\text{GeV} \leq M \leq 2.4 \,\text{GeV}} = 205-230 \,\text{MeV}$

• clearly above $T_c \simeq 150-160 \text{ MeV}$

(no blueshifts in the invariant-mass spectra!)



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]
- min-bias data $(dN_{ch}/dy = 120)$
- $p_T < 0.2 \text{ GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $0.2 \, \text{GeV} < p_T < 0.4 \, \text{GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $0.4 \, \text{GeV} < p_T < 0.6 \, \text{GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $0.6 \,\text{GeV} < p_T < 0.8 \,\text{GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $0.8 \,\text{GeV} < p_T < 1.0 \,\text{GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- min-bias data (dN_{ch}/dy = 120)
 1.0 GeV < p_T < 1.2 GeV
 - 1.0 < p₋ < 1.2 GeV 10⁻¹⁰ 0.2 0.4 0.6 0.8 1.2 1.4 Invariant Mass M [GeV]

- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $1.2 \, \text{GeV} < p_T < 1.4 \, \text{GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $1.4 \text{ GeV} < p_T < 1.6 \text{ GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $1.6 \,\mathrm{GeV} < p_T < 1.8 \,\mathrm{GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- $1.8 \,\text{GeV} < p_T < 2.0 \,\text{GeV}$



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- 2.0 GeV $< p_T < 2.2$ GeV



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+ \mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)
- 2.2 GeV $< p_T < 2.4$ GeV



- dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]
- min-bias data ($dN_{ch}/dy = 120$)



• dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]

• min-bias data ($dN_{ch}/dy = 120$)



• dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]

• min-bias data ($dN_{ch}/dy = 120$)



• dimuon spectra from In + In(158 AGeV) $\rightarrow \mu^+\mu^-$ (NA60) [EHWB15]

• min-bias data ($dN_{ch}/dy = 120$)



Dielectrons at RHIC





Dielectrons at RHIC-BES/FAIR/NICA

$CGUrQMD: Au+Au (E_{lab} = 2-35 AGeV)$



NB: also photon spectra [EHB16b]

Signatures of the QCD-phase structure?

QCD phase structure from em. probes?

- hadronic observables like *p_T* spectra:
 "snapshot" of the stage after kinetic freezeout
- particle abundancies: chemical freezeout
- em. probes: emitted during the whole medium evolution life time of the medium ⇒ "four-volume of the fireball"
- use CGUrQMD to study system-size dependence
- study AA collisions for different A [EHWB15]
- "excitation functions":

systematics of $\ell^+\ell^-$ (and γ) emission vs. beam energy [EHB16b, RH16] similar study in [GHR⁺16]

• caveat: phase transition not really implemented!!!

Scaling behavior of thermal-dilepton yield

• central collisions from C+C to Au+Au at $E_{kin} = 1.76 AGeV$



- thermal-dilepton yield roughly $\propto V_{\rm therm}^{(4)} \propto A^{4/3} \propto A t_{\rm therm} \propto N_{\pi^0}^{4/3}$

Mass-temperature relation in dilepton emission

- interplay between increasing volume and decreasing temperature of fireball
- in IMR ($T < m_{\phi} < M_{\ell^+\ell^-} < m_{J/\psi}$) biased towards early hot stages
- only "background": correlated $D\overline{D}$ decays, some Drell-Yan
- otherwise emission from thermal QGP and hadronic sources
- invariant-mass slope \Leftrightarrow true invariant space-time averaged temperature
- no blueshift due to radial flow as in p_t spectra (e.g., photons)



Dilepton systematics in the beam-energy scan

- thermal-fireball model [RH16, EHB16a]
- invariant-mass slope in IMR \Rightarrow true temperature!
- no blue shift from radial flow as in p_T/m_T spectra



Dilepton systematics in the beam-energy scan

- thermal-fireball model [RH16]
- beam-energy scan at RHIC and lower energies at FAIR and
- dilepton yield as fireball-lifetime clock



• General ideas

- em. probes ⇔ in-medium em. current-correlation function
- dual rates around T_c (compatible with χ symmetry restoration)
- medium modifications of ho , ω , ϕ
- importance of baryon-resonance interactions
- Application to dileptons in HICs
 - coarse-grained transport (here: CGUrQMD)
 - allows use of thermal-QFT spectral VM functions
 - applicable also at low collision energies
 - allows use of thermal-QFT models for dilepton rates
 - successful description from SIS to RHIC energies
 - consistent description of M and m_T spectra!
 - effective slope of *M* spectra (1.5 GeV $< M < M_{J/\psi}$) provides $\langle T \rangle$
 - beam-energy scan at RHIC and FAIR ⇒ signature of phase transition?
- Outlook
 - signature of cross-over vs. 1st order (or even critical endpoint)???
 - challenge: phase transition in (coarse-grained) transport???

- [ABB⁺14] G. Agakishiev, et al., Baryon resonance production and dielectron decays in proton-proton collisions at 3.5 GeV, Eur. Phys. J. A 50 (2014) 82.
 https://doi.org/10.1140/epja/i2014-14082-1
- [EHB16a] S. Endres, H. van Hees, M. Bleicher, Energy, centrality and momentum dependence of dielectron production at collider energies in a coarse-grained transport approach, Phys. Rev. C 94 (2016) 024912. https://doi.org/10.1103/PhysRevC.94.024912
- [EHB16b] S. Endres, H. van Hees, M. Bleicher, Photon and dilepton production at the Facility for Proton and Anti-Proton Research and beam-energy scan at the Relativistic Heavy-Ion Collider using coarse-grained microscopic transport simulations, Phys. Rev. C 93 (2016) 054901. https://doi.org/10.1103/PhysRevC.93.054901

Bibliography II

[EHWB15] S. Endres, H. van Hees, J. Weil, M. Bleicher, Dilepton production and reaction dynamics in heavy-ion collisions at SIS energies from coarse-grained transport simulations, Phys. Rev. C 92 (2015) 014911. https://doi.org/10.1103/PhysRevC.92.014911

- [FMRS13] W. Florkowski, M. Martinez, R. Ryblewski, M. Strickland, Anisotropic hydrodynamics, Nucl. Phys. A 904-905 (2013) 803c. https://doi.org/10.1016/j.nuclphysa.2013.02.138
- [GHR⁺16] T. Galatyuk, P. M. Hohler, R. Rapp, F. Seck, J. Stroth, Thermal Dileptons from Coarse-Grained Transport as Fireball Probes at SIS Energies, Eur. Phys. J. A 52 (2016) 131. https://doi.org/10.1140/epja/i2016-16131-1

[GK91] C. Gale, J. I. Kapusta, Vector dominance model at finite temperature, Nucl. Phys. B **357** (1991) 65. https://doi.org/10.1016/0550-3213(91)90459-B

Bibliography III

- [MT85] L. D. McLerran, T. Toimela, Photon and Dilepton Emission from the Quark-Gluon Plasma: Some General Considerations, Phys. Rev. D 31 (1985) 545. https://doi.org/10.1103/PhysRevD.31.545
- [Rap13] R. Rapp, Dilepton Spectroscopy of QCD Matter at Collider Energies, Adv. High Energy Phys. 2013 (2013) 148253. https://doi.org/10.1155/2013/148253
- [RG99] R. Rapp, C. Gale, ρ properties in a hot meson gas, Phys. Rev. C 60 (1999) 024903. https://doi.org/10.1103/PhysRevC.60.024903
- [RH16] R. Rapp, H. van Hees, Thermal Dileptons as Fireball Thermometer and Chronometer, Phys. Lett. B 753 (2016) 586. https://doi.org/10.1016/j.physletb.2015.12.065
- [RW99] R. Rapp, J. Wambach, Low mass dileptons at the CERN-SPS: Evidence for chiral restoration?, Eur. Phys. J. A 6 (1999) 415. https://doi.org/10.1007/s100500050364

[WHM12] J. Weil, H. van Hees, U. Mosel, Dilepton production in proton-induced reactions at SIS energies with the GiBUU transport model, Eur. Phys. J. A 48 (2012) 111. https://doi.org/10.1140/epja/i2012-12111-9