

# MCSTHAR++, implementation of the Statistical Hadronization Model in HERWIG

-

## Preliminary results

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Modeling of the Parton-Hadron Phase Transition

Villasimius

23-24 September 2010

# Outline

- ➊ Hadronization models and Event Generators
- ➋ Microcanonical hadronization
- ➌ MCSTHAR++: code description
- ➍ MCSTHAR++: preliminary results
- ➎ Conclusions

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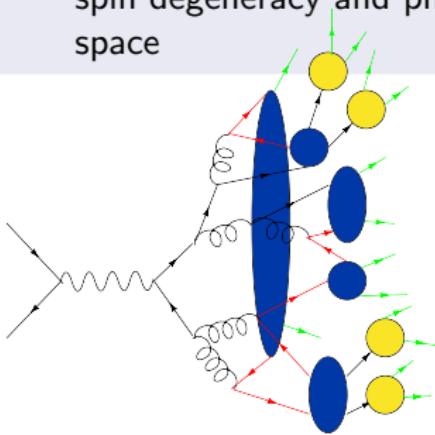
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# Hadronization models (I)

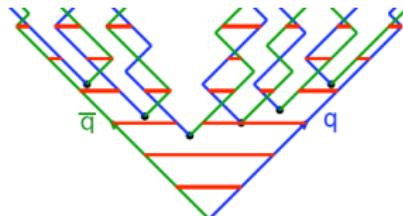
## Cluster model

- Implemented in [HERWIG](#) and [SHERPA](#)
- Final state quarks and antiquarks are coupled to build colorless "clusters"
- The clusters decay (mostly) into two hadrons according to spin degeneracy and phase space



## String model

- Implemented in [PYTHIA](#)
- A color string is supposed to connect final state quarks, antiquarks and gluons (linear potential)
- Hadrons come from  $q\bar{q}$  produced from the vacuum via string fragmentation



# Hadronization models (II)

WHAT ABOUT THE STATISTICAL MODEL???

MCSTHAR++

Monte Carlo SStatistical HAtronization in high energy  
Reactions

In collaboration with

- F. Becattini
- F. Piccinini
- MCnet: Stefan Gieseke, Karlsruhe University  
(Implementation of MCSTHAR++ in Herwig++)

References:

- Cluster model: [HERWIG](#) G. Corcella et al., JHEP 0101 (2001) 010
- String model: [PYTHIA](#) T. Sjöstrand et al., JHEP 05 (2006) 026
- Modified cluster model: [SHERPA](#) J.C. Winter et al., Eur. Phys. J. C35 (2004) 381

# The statistical hadronization model

## Basic ideas

- In a high-energy collision there is the production of pre-hadronic extended object called **clusters** or **fireballs**
- Each of them has well defined physical quantities

$$P, Q, S, B, C, \dots$$

is **colour neutral** and hadronizes according to a **pure statistical law**

## Microcanonical description

Every **localized** multi-hadronic state within the cluster compatible with the conservation laws is equally likely

## Probability to observe the final state $| f \rangle$

$$p_f \propto \langle f | P_i P_V P_i | f \rangle \quad P_i = P_P P_{Q,S,B} \quad P_V = \sum_{h_V} | h_V \rangle \langle h_V |$$

# Model features and free parameters

## Main features

- Bose-Einstein and Fermi-Dirac correlations
- Interactions among the hadrons

## Strange particles suppression

$$\langle f | P_i P_V P_i | f \rangle \Rightarrow \gamma_s^{N_s} \langle f | P_i P_V P_i | f \rangle$$

## Free parameters of the model

- ①  $\gamma_s$  Strangeness suppression parameter
- ②  $\rho$  Energy density of the clusters

PYTHIA: 15 parameters

HERWIG: 7 parameters

SHERPA: 15 parameters

## References:

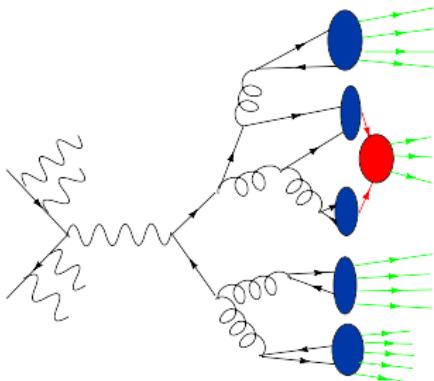
- R. Hagedorn, Nuovo Cim. Suppl. 3 (1965) 147
- F. Becattini, Z. Phys. C 69 (1996) 485
- F. Becattini, U. W. Heinz, Z. Phys. C 76 (1997) 269.
- J. Bernstein, R. Dashen, S. Ma, Phys. Rev. 187 (1969) 1

# MCSTHAR++: code description (I)

## MCSTHAR++

### Monte Carlo SStatistical HAdron Reaction

- MCSTHAR++ implements the **statistical model** in the **microcanonical formulation**
- It is an **Object Oriented C++** code (with a little bit of **ROOT**) performing the hadronization step taking as **input** a set of (**HERWIG's**) clusters and giving in **output** the primary hadrons
- If needed a **reclusterization** is performed



- HERWIG's showers and hard scattering
- HERWIG's clustering
- MCSTHAR++'s reclusterizing
- MCSTHAR++'s hadronization

- The final decay of the unstable hadrons is performed by HERWIG itself

## MCSTHAR++: code description (II)

We need to normalize the weight associated to the decay of each cluster



Knowledge of the partition function is mandatory

### Microcanonical Partition Function

$$\Omega(M, \gamma_s, \rho, S, Q, B, C, Bt) = \sum_i^{N_{ch}} \Omega_i(M, \gamma_s, \rho, S, Q, B, C, Bt)$$

- The possible solution is the construction of a grid of partition functions for the different possible values of:
  - ① Charges (more than 100 configurations)
  - ② Mass (from  $2M_{\pi^0}$  to about 10 GeV)
  - ③  $\gamma_s$  and  $\rho$  (needed only to perform the tuning)
- The information on  $\Omega$  is obtained at runtime by interpolation on  $M$ ,  $\gamma_s$  and  $\rho$

# Free parameters and generator tuning

- The statistical model needs only 2 (+1) parameters:  $\gamma_s$  and  $\rho$  (and the cluster low mass cut  $M_{cut}$ )...
- ...but there is a strong interplay with some of HERWIG's free parameters, since MCSTHAR++ uses its clusters:
  - quark masses
  - gluon mass
  - quark and gluon virtuality cut
  - $\Lambda_{QCD}$
- All these parameters are involved into the QCD shower: they regulate the clusters mass, flavour composition and phase space distribution

For a fine tuning of the generator is necessary to understand the interplay between the two sets of parameters and make a global minimization

...but for the present...

# Preliminary results @LEP

- A preliminary tuning on LEP data has been performed on MCSTHAR++'s parameters  $\gamma_S$ ,  $\rho$  and  $M_C$ .
- The optimal parameter configuration has been obtained considering the  $\chi^2$  values for a set of event shape and single particle distributions and for the multiplicities of 41 hadrons.

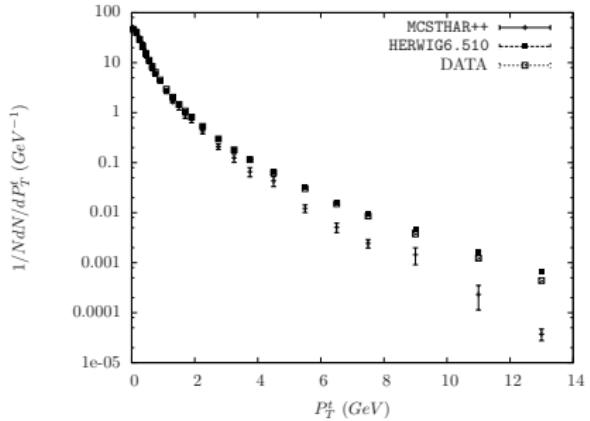
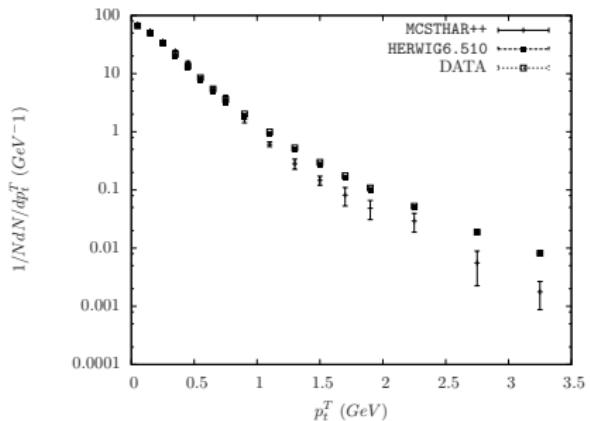
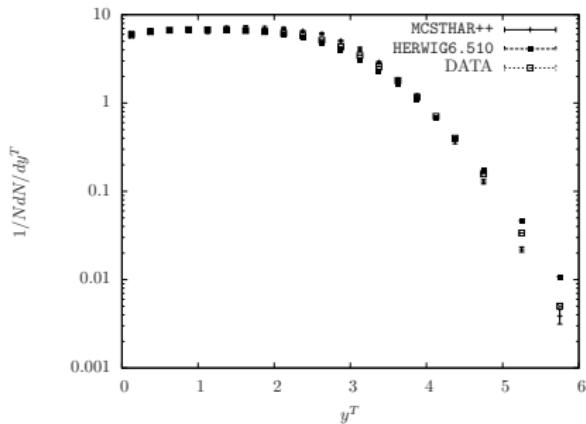
$M_C (GeV)$	$\gamma_S$	$\rho(GeV/fm^3)$	$\chi^2_{red}$ (ES)	$\chi^2_{red}$ (SP)	$\chi^2_{red}$ (PM)	$\chi^2_{red}$
1.4	0.65	0.25	12.43	6.93	16.52	10.04
1.4	0.65	0.35	16.45	7.35	18.01	12.24
1.4	0.65	0.45	36.00	21.29	6.50	27.57
1.6	0.65	0.25	21.38	7.85	21.49	15.00
1.6	0.65	0.35	14.59	6.46	16.04	10.83
1.6	0.65	0.45	9.95	7.48	18.15	9.20
1.8	0.65	0.25	31.34	8.04	17.23	19.63
1.8	0.65	0.35	20.23	7.26	19.30	14.06
1.8	0.65	0.45	17.66	8.75	10.18	13.08
1.6	0.60	0.35	16.41	6.55	18.44	11.86
1.6	0.65	0.35	14.59	6.46	16.04	10.83
1.6	0.70	0.35	31.01	12.90	8.72	21.34
1.6	0.55	0.45	11.25	6.94	25.63	9.94
1.6	0.675	0.45	11.85	5.88	20.17	9.45
1.6	0.70	0.45	18.92	6.15	14.41	12.67

- "Best fit" parameter configuration:  $M_C = 1.6 \text{ GeV}$ ,  $\gamma_S = 0.65$  and  $\rho = 0.45 \text{ GeV}/fm^3$ .

# Preliminary results @LEP: Event shape

- Comparison among MCSTHAR++, HERWIG6.510 and DELPHI data (Z. Phys. C **73** (1996) 11)

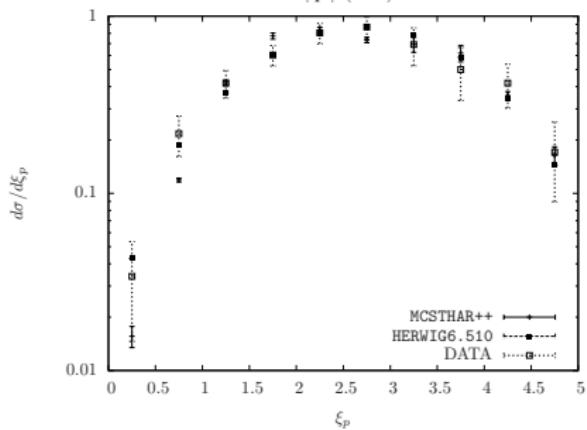
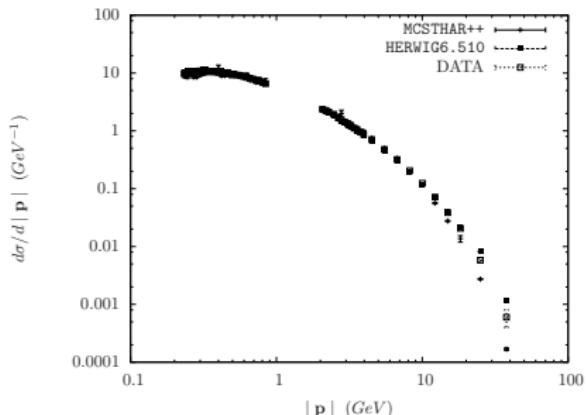
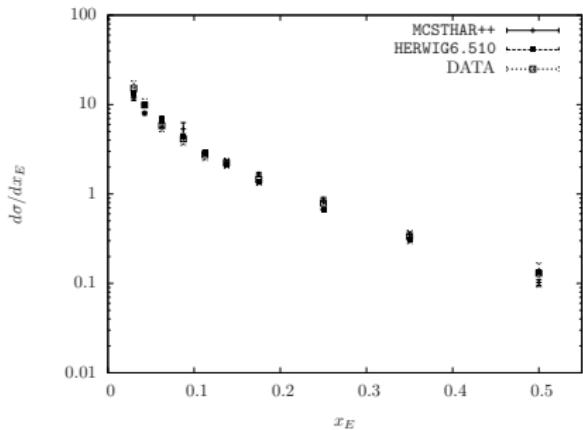
$$\bullet T = \max_{\vec{n}} \frac{\sum_{j=1}^{N_P} |\vec{p}_i \cdot \vec{n}|}{\sum_{j=1}^{N_P} |\vec{p}_i|}$$
$$\bullet y^T = \frac{1}{2} \cdot \log \frac{E + p_T}{E - p_T}$$



# Preliminary results @LEP: Single particle

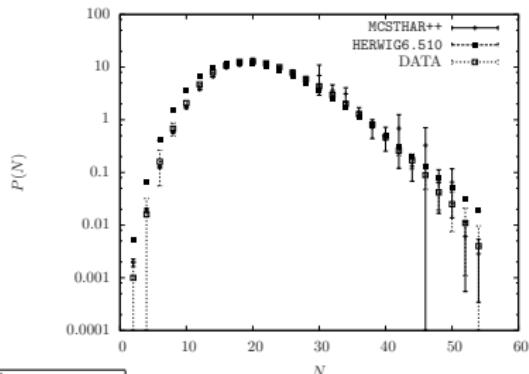
- Comparison among MCSTHAR++, HERWIG6.510 and OPAL data  
(Z. Phys. C 63 (1994) 181)  
(Eur. Phys. J. C 5 (1998) 411)

- $|\mathbf{p}| \rightarrow \pi^\pm$
- $\xi_p = -\log(2|\mathbf{p}|/\sqrt{s}) \rightarrow \rho^\pm$
- $x_E = 2E/\sqrt{s} \rightarrow \omega$



# Preliminary results @LEP: Multiplicities

- Comparison among MCSTHAR++, HERWIG6.510 and LEP data  
(Eur. Phys. J. C **56** (2008) 493)  
(Z. Phys. C **53** (1992) 539)
- $P(N) \rightarrow$  Charged particle number

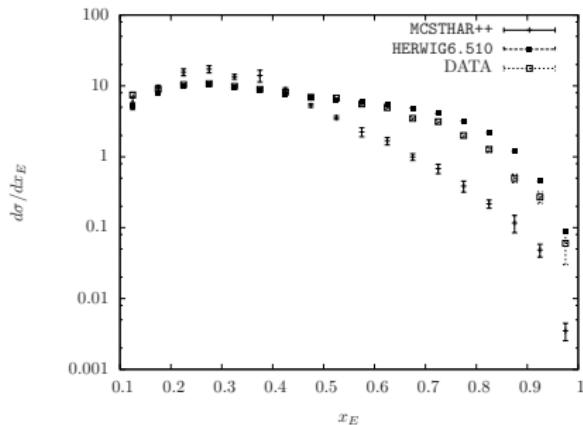
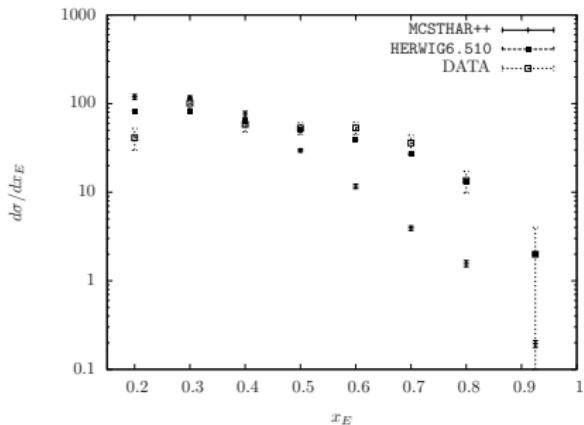


	MCSTHAR++	HERWIG6.510	LEP data	$\Delta_{MCSTHAR++}$
$\pi^0$	$10.98 \pm 0.13$	9.56	$9.61 \pm 0.29$	4.33
$\pi^+$	$9.33 \pm 0.15$	8.16	$8.50 \pm 0.10$	4.55
$\eta$	$1.18 \pm 0.04$	0.63	$1.059 \pm 0.086$	1.26
$\rho^+$	$1.16 \pm 0.03$	0.97	$1.20 \pm 0.22$	-0.18
$\rho^0$	$1.42 \pm 0.04$	1.00	$1.40 \pm 0.13$	0.13
$\omega$	$1.29 \pm 0.03$	0.97	$1.024 \pm 0.059$	4.10
$\eta'$	$0.13 \pm 0.01$	0.10	$0.166 \pm 0.047$	-0.61
$K^+$	$1.11 \pm 0.02$	1.05	$1.127 \pm 0.026$	-0.31
$K^0$	$1.07 \pm 0.11$	0.942	$1.0376 \pm 0.0096$	0.30
$K^{*+}$	$0.34 \pm 0.04$	0.273	$0.357 \pm 0.022$	-0.37
$K^{*0}$	$0.33 \pm 0.02$	0.274	$0.370 \pm 0.013$	-1.92
$p$	$0.45 \pm 0.02$	0.762	$0.519 \pm 0.018$	-2.79
$D^+$	$0.22 \pm 0.01$	0.287	$0.238 \pm 0.024$	0.53
$D^0$	$0.54 \pm 0.04$	0.577	$0.559 \pm 0.022$	0.33
$D_S$	$0.110 \pm 0.009$	0.112	$0.116 \pm 0.036$	0.18
$\Lambda_C$	$0.13 \pm 0.01$	0.036	$0.079 \pm 0.022$	2.19

- Almost perfect agreement for  $P(N)$  distribution
- $\Delta_{MCSTHAR++} \leq 3$  for the 70% of the species.
- Please, no questions about bottomed hadrons...

# Preliminary results @LEP: Bad news...

- $D^0$  and  $D^*$  scaled energy distributions shown a wrong behavior...



- Some multiplicities shown a large disagreement...

	MCSTHAR++	HERWIG6.510	LEP data	$\Delta_{MCSTHAR++}$
$\phi$	$0.167 \pm 0.007$	0.1278	$0.0977 \pm 0.0058$	7.16
$\Lambda$	$0.128 \pm 0.004$	0.322	$0.1943 \pm 0.0038$	-11.43
$\Sigma^-$	$0.0233 \pm 0.0007$	0.0548	$0.0410 \pm 0.0037$	-4.68
$\Sigma^{*+}$	$0.0176 \pm 0.0006$	0.0551	$0.0118 \pm 0.0011$	4.62
$\Xi^-$	$0.0040 \pm 0.0001$	0.0391	$0.01319 \pm 0.00050$	-17.7
$\Omega$	$(1.09 \pm 0.04) \times 10^{-4}$	$4.94 \times 10^{-3}$	$(6.2 \pm 1.0) \times 10^{-4}$	-5.11
$n$	$0.51 \pm 0.01$	0.683	$0.991 \pm 0.054$	-8.49

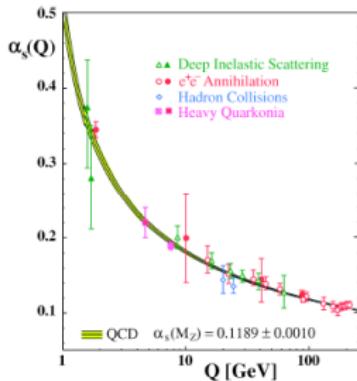
# Conclusions

- ① Different models are implemented in the available MC event generators
- ② It is worth to have an independent model available for the hadronization:
  - MC generators are tuned on data at energy lower than the one of LHC (LEP and Tevatron)
  - The availability of independent models gives reliability to the theoretical predictions and their uncertainties
- ③ The statistical hadronization models have some interesting properties:
  - Small number of parameters
  - "Advanced" features: quantum statistics and interactions
- ④ The tuning of [MCSTHAR++](#) with [HERWIG](#) and [Herwig++](#) on LEP data is now a work in progress

# Thank You!

# Hadronization and QCD coupling constant

## Why do we need a hadronization model?



- The behaviour of the QCD coupling constant is such that at  $E \approx 1 \text{ GeV}$  perturbative calculations are not possible anymore
- A **phenomenological model** is needed to describe the **hadronization** process

S. Bethke, Prog. Part. Nucl. Phys. **58** (2007) 351

## Main hadronization models

- Cluster model: [HERWIG](#) G. Corcella et al., JHEP 0101 (2001) 010
- String model: [PYTHIA](#) T. Sjöstrand et al., JHEP 05 (2006) 026
- Modified cluster model: [SHERPA](#) J.C. Winter et al., Eur. Phys. J. C35 (2004) 381
- Statistical model: not yet available in any MC event generator

# Strong coupling constant

- In 1-loop approximation the QCD coupling constant is given by

$$\alpha_s(Q^2) = \frac{\alpha_s(\mu^2)}{1 + \alpha_s(\mu^2) \beta_0 \ln \frac{Q^2}{\mu^2}}$$

- Where  $\beta_0 = \frac{33 - 2N_f}{12\pi}$

# SHM transition probability

Probability to observe the decay  $| (N_j) ; p_1, \dots, p_N \rangle$

$$p ((N_j) ; p_1, \dots, p_N) = \frac{\frac{V^N}{(2\pi)^{3N}} \prod_{i=1}^N (2J_i + 1) \delta^4(P_0 - \hat{P}) \delta_{\mathbf{Q}_0 \hat{\mathbf{Q}}_{f'}}}{\sum_{(N'_j)} \frac{V^{N'}}{(2\pi)^{3N'}} \left( \prod_{i=1}^{N'} \sum_{\sigma_i} \int d^3 p_i \right) \delta^4(P_0 - \hat{P}) \delta_{\mathbf{Q}_0 \hat{\mathbf{Q}}_{f'}}}$$

Probability to observe the decay  $| (N_j) ; p_1, \dots, p_N \rangle$  (Quantum statistics)

$$\prod_{j=1}^K \left[ \sum_{r_j} \frac{\chi(r_j)^{b_j}}{N_j!} \sum_{\sigma_1, \dots, \sigma_{N_j}} \prod_{i_j=1}^{N_j} \frac{\delta_{\sigma_{i_j} \sigma_{r_j(i_j)}}}{(2\pi)^3} \int_A d^3 x e^{-i(\mathbf{p}_{i_j} - \mathbf{p}_{r_j(i_j)}) \cdot \mathbf{x}} \right] \times \delta^4(P_0 - \hat{P}) \delta_{\mathbf{Q}_0 \hat{\mathbf{Q}}_{f'}}$$

- Quantum correlations give corrections of about 20% on the microcanonical weight for the single channel ( $6\pi$  channel and cluster mass  $M = 5$  GeV)

# Interacting hadron gas

- How to take into account the **interactions** between the confined hadrons?

## Gas of hadrons and resonances

Retaining only the **resonant** part of the interaction, the microcanonical partition function is that of a **gas of free hadrons and resonances with distributed mass**

## References:

J. Bernstein, R. Dashen, S. Ma,  
Phys. Rev. **187** (1969) 1



To include the (leading) interactions **all the resonances must be included** in the hadron samplings with **Breit-Wigner distributed mass**

- Interactions give corrections of about **-2%** on the microcanonical weight for the single channel  
( $4\rho$  channel and cluster mass  $M = 4$  GeV)

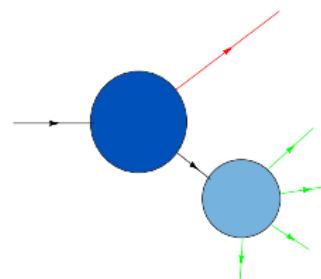
## MCSTHAR++: code description (III)

- Each cluster is hadronized according to the microcanonical model
- Exact conservation of
  - ① Strangeness
  - ② Electric charge
  - ③ Baryonic number
  - ④ Charm
  - ⑤ Beauty
  - ⑥ Energy-Momentum

- Light flavour clusters ( $C = 0$  and  $B = 0$ ): the decay channel is sampled using a multipoisson distribution

- Heavy flavour clusters: the **heavy hadron** is sampled using an exponential distribution

$$P(h) \propto \exp\left(-\frac{m_h}{T}\right)$$



- At this point the hadronization channel is chosen... **but what about the weight???**