Collisional energy loss of heavy quarks

by Alex Meistrenko

with A. Peshier (Cape Town), J. Uphoff (Frankfurt) and C. Greiner (Frankfurt)

reference: arXiv:1204.2397v1

transport group meeting 03.05.2012





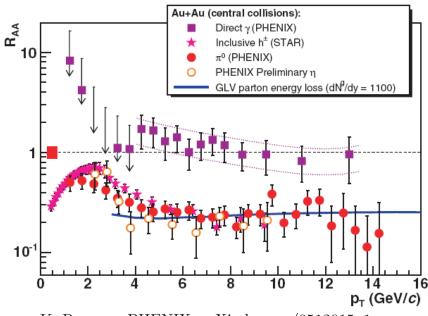


Abstract: elastic energy loss model

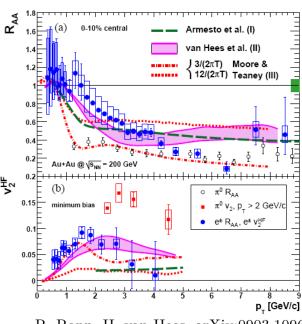
- elastic dE/dx of heavy quarks in the case of a non-static thermalized QGP
- pQCD transition matrix approach with
 - quantum distribution functions
 - running coupling
 - effective screening mass adjusted to HTL calculations
 - Peterson fragmentation and meson decay with Pythia
- comparison with RHIC data for electorn yields from heavy flavor decays
 - linear scaling of the binary cross section seems not sufficient

Experimental data

RAA and v2 from experiments at RHIC:



K. Reygers, PHENIX, arXiv:hep-ex/0512015v1



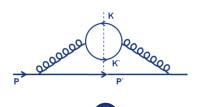
R. Rapp, H. van Hees, arXiv:0903.1096

energy loss and strong coupling (to the medium) of light and heavy (!) quarks

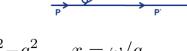
Mean energy loss in the QGP

interaction rate: Σ is evaluated at the energy $p_0 = E + i\epsilon$:

$$\Gamma_{i}\left(E\right)=-\frac{1}{2E}\left(1-n_{F}\left(E\right)\right)\operatorname{tr}\left[\left(\gamma^{\mu}P_{\mu}+M\right)\operatorname{Im}\Sigma\left(P\right)\right]\,,\quad\frac{dE_{i}}{dx}=\frac{1}{v}\int d\omega\,\frac{\partial\Gamma_{i}}{\partial\omega}\omega$$



contribution from $|t| < |t^*|$ with $m_D^2 \ll |t^*| \ll T^2$:



$$\frac{dE_i}{dx} = \frac{K(C_F, \alpha)}{v^2} \int_{t^*}^0 dt \, (-t) \int_{-v}^v dx \frac{x}{(1 - x^2)^2} \left[\rho_L + \left(v^2 - x^2 \right) \rho_T \right] \,, \quad t = \omega^2 - q^2 \,, \quad x = \omega/q$$

spectral functions and HTL propagators:

$$\rho_{L,T}\left(\omega,q\right):=-\frac{1}{\pi}\mathrm{Im}\left[\Delta_{L,T}\left(\omega+i\epsilon,q\right)\right]\,,\quad\Delta_{L}\left(\omega,q\right)=\frac{1}{q^{2}+\Pi_{L}\left(x\right)}\,,\quad\Delta_{T}\left(\omega,q\right)=\frac{1}{\omega^{2}-q^{2}-\Pi_{T}\left(x\right)}$$

with the self-energies:

$$\Pi_L(x) = m_D^2 \left[1 - Q(x) \right], \quad \Pi_T(x) = \frac{m_D^2}{2} x \left(1 - x^2 \right) Q'(x), \quad Q(x) := \frac{x}{2} \ln \frac{x+1}{x-1}$$

Mean energy loss in the QGP

contribution from $|t| > |t^*|$ with $\int_k := \int d^3k/(2\pi)^3$:

$$\frac{dE_{i}}{dx} = \frac{1}{2Ev} \int_{k} \frac{n_{i}(k)}{2k} \int_{k'} \frac{\overline{n}_{i}}{2k'} \int_{p'} \frac{1}{2E'} (2\pi)^{4} \delta^{(4)} \left(P + K - P' - K'\right) \frac{1}{d} \sum_{spin,color} \left| \mathcal{M}_{i} \right|^{2} \omega$$

in the limit $E \to \infty$ and E >> T:

$$\frac{dE_i}{dx} = d_i \int_k \frac{n_i(k)}{2k} \int_{t_{min}}^{t^*} dt (-t) \frac{d\sigma_i}{dt}$$

both contributions from $|t| < |t^*|$ and $|t| > |t^*|$ lead to the NLL formula:

$$\frac{dE}{dx} = \frac{4\pi\alpha_s^2 T^2}{3} \left[\left(1 + \frac{n_f}{6} \right) \ln \frac{ET}{m_D^2} + \frac{2}{9} \ln \frac{ET}{M^2} + c(n_f) \right] \quad \text{with} \quad c(n_f) \approx 0.146 \cdot n_f + 0.050$$

and for running coupling:

$$\frac{dE}{dx} = \frac{4\pi T^2}{3} \alpha_s(m_D^2) \alpha_s(ET) \left[\left(1 + \frac{n_f}{6} \right) \ln \frac{ET}{m_D^2} + \frac{2}{9} \frac{\alpha_s(M^2)}{\alpha_s(m_D^2)} \ln \frac{ET}{M^2} + c(n_f) + \mathcal{O}\left(\alpha_s(m_D^2) \ln \frac{ET}{m_D^2}\right) \right]$$

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Mean energy loss with QGP flow

replace Bose and Fermi by the Jüttner distribution functions:

$$n_{BJ} = \frac{1}{e^{\gamma(E_k - \vec{\beta} \cdot \vec{k})/T} - 1}, \qquad n_{FJ} = \frac{1}{e^{\gamma(E_k - \vec{\beta} \cdot \vec{k})/T} + 1}.$$

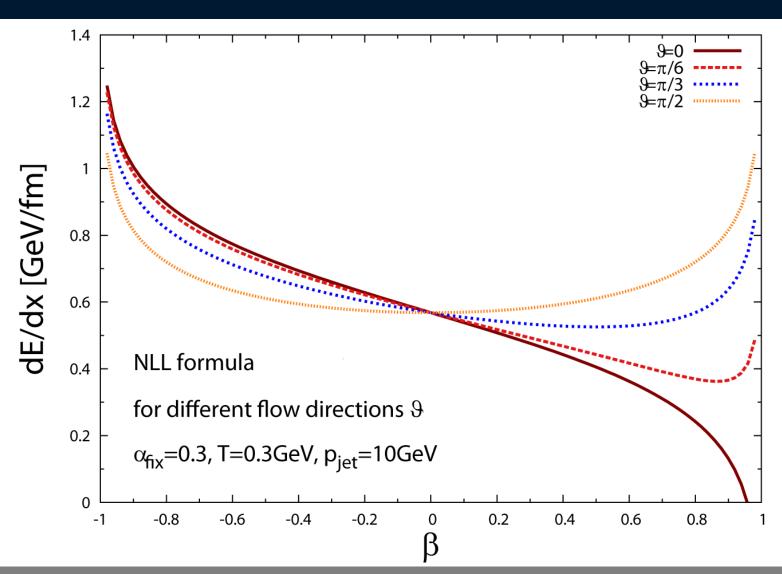
in the parallel case $(\vec{\beta} || \vec{p})$:

$$\left. \frac{dE}{dx} \right|_{\parallel}^{fix} = \frac{4\pi\alpha_s^2 T^2}{3} \left[\left(1 + \frac{n_f}{6} \right) \ln \frac{E\gamma \left(1 - \beta \right) T}{m_D^2} + \frac{2}{9} \ln \frac{E\gamma \left(1 - \beta \right) T}{M^2} + c \left(n_f \right) \right]$$

in general:

$$\frac{dE}{dx} = \frac{4\pi\alpha_s^2 T^2}{3} \left[\left(1 + \frac{n_f}{6} \right) \ln \frac{p_\mu \beta^\mu T}{m_D^2} + \frac{2}{9} \ln \frac{p_\mu \beta^\mu T}{M^2} + c(n_f) \right]$$

Mean energy loss with QGP flow

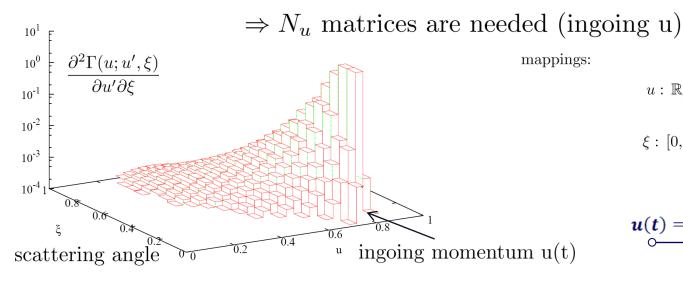


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MC-simulation: transition matrix

thermalized medium with quarks and gluons: $\tau = 0.6 - 0.8 \, fm/c$

$$P_{ij} \approx \Delta t \sum_{k=1}^{n} \frac{\Delta u' \Delta \xi}{n} \cdot \frac{\partial^{2} \Gamma(u; u'_{i,k}, \xi_{j,k})}{\partial u' \partial \xi}, \quad 0 \le i < N_{u}, \ 0 \le j < N_{\xi}$$



$$u: \mathbb{R}_0^+ \longrightarrow [0,1), p' \longmapsto u(p') = \frac{e^{p'/p_0} - 1}{e^{p'/p_0} + 1}$$
$$\xi: [0,\pi] \longrightarrow [0,1], \vartheta \longmapsto \xi = \left(\frac{1 - \cos \vartheta}{2}\right)^{\frac{1}{4}}$$

$$u(t + \Delta t) = u'$$

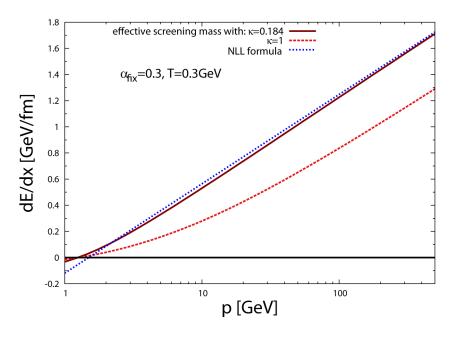
$$u(t) = u$$

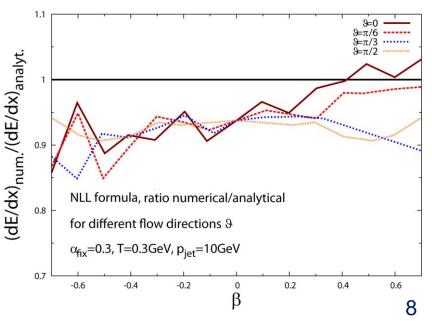
as input: available partonic or hydro models for the background medium, $T_{cell}(\vec{x},t)$, $\vec{v}_{cell}(\vec{x},t)$

Effective screening mass and numerics

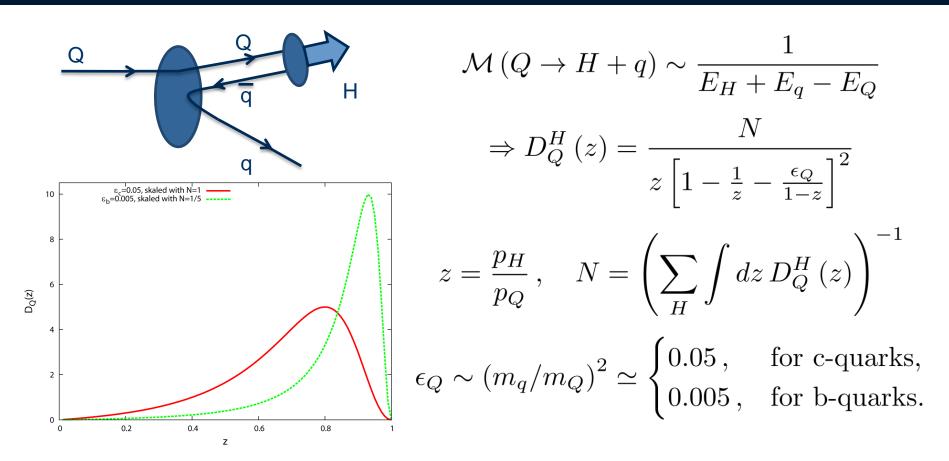
no convergence for the Debye screening mass (soft part of $\partial\Gamma/\partial\omega$ has to be screened): $\frac{dE}{dx}\Big|_{num.} \neq \frac{dE}{dx}\Big|_{analyt.}$ effective screening mass for the Born cross sections: $\mu^2(t) = \kappa \cdot 4\pi \left(1 + \frac{n_f}{6}\right) \alpha(t) T^2 \Rightarrow \frac{\alpha_s}{t - \Pi_T(\omega, q)} \to \frac{\alpha_s}{t - \mu^2(t)}$ analytical evalution of $\partial\Gamma/\partial\omega$ with $\mu^2(t)$ and comparing with HTL calculation of dE/dx leads to: $\kappa = \frac{1}{2e} \simeq 0.2$

 \Rightarrow convergence of the numerical results against the analytic NLL formula





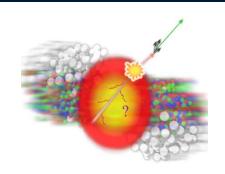
Peterson fragmentation

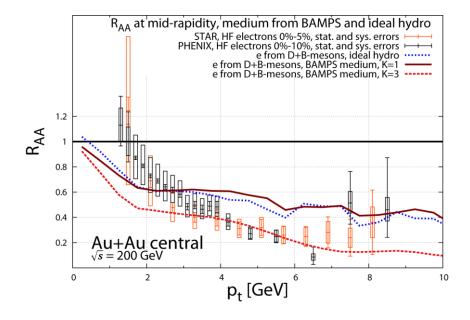


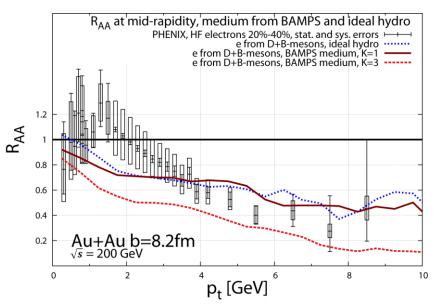
the following stage of heavy meson decays to electrons is calculated with PYTHIA 8.1

Results: nuclear modification factor

$$R_{AA} = \frac{d^2 N_{AA}/dp_T dy}{N_{b.coll.} d^2 N_{NN}/dp_T dy} \simeq \frac{d^2 N_{AA}^{final}/dp_T dy}{d^2 N_{AA}^{initial}/dp_T dy}$$



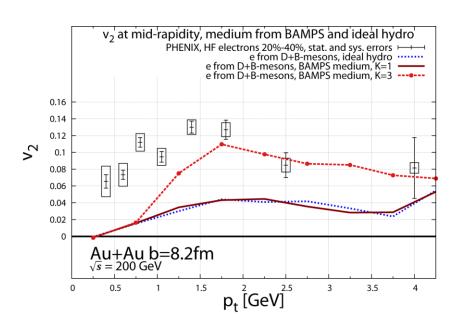


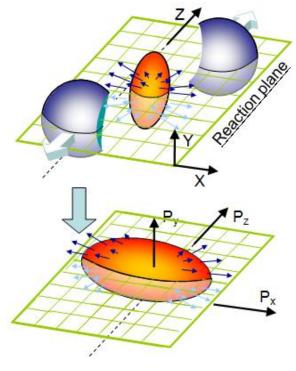


Results: elliptic flow

$$v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_T^2} \right\rangle = \left\langle \cos(2\varphi) \right\rangle = \frac{1}{\frac{d^2N}{p_T dp_T dy}} \int d\varphi \frac{d^3N}{p_T dp_T d\varphi dy} \cos(2\varphi)$$

from
$$E\frac{d^3N}{d^3p} = \frac{d^2N}{2\pi p_T dp_T dy} \left(1 + \sum_{n=1}^{\infty} 2v_n \cos(n\varphi)\right)$$





Conclusion

- more realistic scenario
 - quantum statistics, running coupling, effective screening mass, light quarks and gluons, fragmentation, decay of mesons, different background media
- significant contribution of elastic processes
 - RAA can be reproduced up to a factor of 2
 - v₂ can be reproduced up to a factor of 3
 - discrepancy could be an effect of radiative energy loss and/or uncertain initial conditions
- possible modifications:
 - different initial conditions
 - hadronization of the medium particles
 - implementation of bremsstrahlung

Thank you for your attention!

